

Package ‘viking’

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Title State-Space Models Inference by Kalman or Viking

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Description Inference methods for state-space models, relying on the Kalman Filter or on Viking (Variational Bayesian Varlance tracKING). See J. de Vilmarest (2022) <<https://theses.hal.science/tel-03716104/>>.

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expectation_maximization
Expectation-Maximization

Description

`expectation_maximization` is a method to choose hyper-parameters of the linear Gaussian State-Space Model with time-invariant variances relying on the Expectation-Maximization algorithm.

Usage

```
expectation_maximization(
  X,
  y,
  n_iter,
  Q_init,
  sig_init = 1,
  verbose = 1000,
  lambda = 10^-9,
  mode_diag = FALSE,
  p1 = 0
)
```

Arguments

X	explanatory variables
y	time series
n_iter	number of iterations of the EM algorithm
Q_init	initial covariance matrix on the state noise
sig_init	(optional, default 1) initial value of the standard deviation of the observation noise
verbose	(optional, default 1000) frequency for prints
lambda	(optional, default 10^{-9}) regularization parameter to avoid singularity
mode_diag	(optional, default FALSE) if TRUE then we restrict the search to diagonal matrices for Q
p1	(optional, default 0) deterministic value of $P_1 = p1 \ I$

Details

E-step is realized through recursive Kalman formulae (filtering then smoothing).
 M-step is the maximization of the expected complete likelihood with respect to the hyper-parameters.
 We only have the guarantee of convergence to a LOCAL optimum. We fix $P_1 = p1 \ I$ (by default $p1 = 0$). We optimize theta1, sig, Q.

Value

a list containing values for P, theta, sig, Q, and two vectors DIFF, LOGLIK assessing the convergence of the algorithm.

Examples

```
set.seed(1)
### Simulate data
n <- 100
d <- 5
Q <- diag(c(0,0,0.25,0.25,0.25))
sig <- 1

X <- cbind(matrix(rnorm((d-1)*n, sd=1), n, d-1), 1)
theta <- matrix(rnorm(d), d, 1)
theta_arr <- matrix(0, n, d)
for (t in 1:n) {
  theta_arr[t,] <- theta
  theta <- theta + matrix(mvtnorm::rmvnorm(1, matrix(0, d, 1), Q), d, 1)
}
y <- rowSums(X * theta_arr) + rnorm(n, sd=sig)

l <- viking::expectation_maximization(X, y, 50, diag(d), verbose=10)
print(l$Q)
print(l$sig)
```

`iterative_grid_search` *Iterative Grid Search*

Description

`iterative_grid_search` is an iterative method to choose hyper-parameters of the linear Gaussian State-Space Model with time-invariant variances.

Usage

```
iterative_grid_search(
  X,
  y,
  q_list,
  Q_init = NULL,
  max_iter = 0,
  delay = 1,
  use = NULL,
  restrict = NULL,
  mode = "gaussian",
  p1 = 0,
  ncores = 1,
```

```

    train_theta1 = NULL,
    train_Q = NULL,
    verbose = TRUE
)

```

Arguments

X	the explanatory variables
y	the observations
q_list	the possible values of diag(Q) / sig^2
Q_init	(default NULL) initial value of Q / sig^2, if NULL it is set to 0
max_iter	(optional 0) maximal number of iterations. If 0 then optimization is done as long as we can improve the log-likelihood
delay	(optional, default 1) to predict y[t] we have access to y[t-delay]
use	(optional, default NULL) the availability variable
restrict	(optional, default NULL) if not NULL it allows to specify the indices of the diagonal coefficient to optimize
mode	(optional, default gaussian)
p1	(optional, default 0) coefficient for P1/sig^2 = p1 I
ncores	(optional, default 1) number of available cores for computation
train_theta1	(optional, default NULL) training set for estimation of theta1
train_Q	(optional, default NULL) time steps on which the log-likelihood is computed
verbose	(optional, default TRUE) whether to print intermediate progress

Details

We restrict ourselves to a diagonal matrix Q and we optimize Q / sig^2 on a grid. Each diagonal coefficient is assumed to belong to a pre-defined q_list.

We maximize the log-likelihood on that region of search in an iterative fashion. At each step, we change the diagonal coefficient improving the most the log-likelihood. We stop when there is no possible improvement. This doesn't guarantee an optimal point on the grid, but the computational time is much lower.

Value

a list containing values for P, theta, sig, Q, as well as LOGLIK, the evolution of the log-likelihood during the search.

Examples

```

set.seed(1)
### Simulate data
n <- 100
d <- 5
Q <- diag(c(0,0,0.25,0.25,0.25))
sig <- 1

```

```
X <- cbind(matrix(rnorm((d-1)*n, sd=1), n, d-1), 1)
theta <- matrix(rnorm(d), d, 1)
theta_arr <- matrix(0, n, d)
for (t in 1:n) {
  theta_arr[t,] <- theta
  theta <- theta + matrix(mvtnorm::rmvnorm(1, matrix(0, d, 1), Q), d, 1)
}
y <- rowSums(X * theta_arr) + rnorm(n, sd=sig)

l <- viking::iterative_grid_search(X, y, seq(0, 1, 0.25))
print(l$Q)
print(l$sig)
```

kalman_filtering *Kalman Filtering*

Description

Compute the filtered estimation of the parameters theta and P.

Usage

```
kalman_filtering(X, y, theta1, P1, Q = 0, sig = 1)
```

Arguments

X	the explanatory variables
y	the time series
theta1	initial theta
P1	initial P
Q	(optional, default 0) covariance matrix of the state noise
sig	(optional, default 1) variance of the spate noise

Value

a list containing theta_arr and P_arr, the filtered estimation of the parameters theta and P.

kalman_smoothing *Kalman Smoothing*

Description

Compute the smoothed estimation of the parameters theta and P.

Usage

```
kalman_smoothing(X, y, theta1, P1, Q = 0, sig = 1)
```

Arguments

X	the explanatory variables
y	the time series
theta1	initial theta
P1	initial P
Q	(optional, default 0) covariance matrix of the state noise
sig	(optional, default 1) variance of the spate noise

Value

a list containing theta_arr and P_arr, the smoothed estimation of the parameters theta and P.

loglik *Log-likelihood*

Description

loglik computes the log-likelihood of a state-space model of specified Q/sig^2, P1/sig^2, theta1.

Usage

```
loglik(X, y, Qstar, use, p1, train_theta1, train_Q, mode = "gaussian")
```

Arguments

X	explanatory variables
y	time series
Qstar	the ratio Q/sig^2
use	the availability variable
p1	coefficient for P1/sig^2 = p1 I
train_theta1	training set for estimation of theta1
train_Q	time steps on which the log-likelihood is computed
mode	(optional, default gaussian)

Value

a numeric value for the log-likelihood.

plot.statespace *Plot a statespace object*

Description

`plot.statespace` displays different graphs expressing the behavior of the state-space model:

1. Evolution of the Bias: rolling version of the error of the model.
2. Evolution of the RMSE: root-mean-square-error computed on a rolling window.
3. State Evolution: time-varying state coefficients, subtracted of the initial state vector.
4. Normal Q-Q Plot: we check if the observation follows the Gaussian distribution of estimated mean and variance. To that end, we display a Q-Q plot of the residual divided by the estimated standard deviation, against the standard normal distribution.

Usage

```
## S3 method for class 'statespace'  
plot(x, pause = FALSE, window_size = 7, date = NULL, sel = NULL, ...)
```

Arguments

- | | |
|--------------------------|---|
| <code>x</code> | the statespace object. |
| <code>pause</code> | (default FALSE) if set to FALSE then the plots are displayed on a single page, otherwise a new page is created for each plot. |
| <code>window_size</code> | (default 7) the window size of the rolling mean computed on the error to display the bias, and on the mean squared error to display a rolling RMSE. |
| <code>date</code> | (default NULL) defines the values for the x-axis. |
| <code>sel</code> | (default NULL) defines a subset of the data on which we zoom. For instance one can display the evolution of the SSM on a test set and not the whole data set. |
| <code>...</code> | additional parameters |

Value

No return value, called to display plots.

`predict.statespace` *Predict using a statespace object*

Description

`predict.statespace` makes a prediction for a statespace object, in the offline or online setting.

Usage

```
## S3 method for class 'statespace'
predict(
  object,
  newX,
  newy = NULL,
  online = TRUE,
  compute_smooth = FALSE,
  type = c("mean", "proba", "model"),
  ...
)
```

Arguments

<code>object</code>	the statespace object
<code>newX</code>	the design matrix in the prediction set
<code>newy</code>	(default <code>NULL</code>) the variable of interest in the prediction set. If specified it allows to use the state-space model in the online setting. Otherwise the prediction is offline.
<code>online</code>	(default <code>TRUE</code>) specifies if the prediction is made online, that is if the observation at time $t-1$ is used to update the model before predicting at time t .
<code>compute_smooth</code>	(default <code>FALSE</code>) specifies if Kalman Smoothing is also computed.
<code>type</code>	type of prediction. Can be either mean return the mean forecast. proba return a probabilistic forecast (list containing estimation of the mean and standard deviation). model return the updated statespace object (containing also the forecasts). ...

Value

Depending on the type specified, the result is

- a vector of mean forecast if `type='mean'`
- a list of two vectors, mean forecast and standard deviations if `type='proba'`
- a statespace object if `type='model'`

select_Kalman_variances

Select time-invariant variances of a State-Space Model

Description

`select_Kalman_variances` is a function to choose hyper-parameters of the linear Gaussian State-Space Model with time-invariant variances. It relies on the functions `iterative_grid_search` and `expectation_maximization`.

Usage

```
select_Kalman_variances(ssm, X, y, method = "igd", ...)
```

Arguments

ssm	the statespace object
X	explanatory variables
y	time series
method	(optional, default 'igd') it can be either 'igd' <code>iterative_grid_search</code> is called 'em' <code>expectation_maximization</code> is called
...	additional parameters

Value

a new statespace object with new values in `kalman_params`

statespace

Design a State-Space Model

Description

The function `statespace` builds a state-space model, with known or unknown variances. By default, this function builds a state-space model in the static setting, with a constant state (zero state noise covariance matrix) and constant observation noise variance.

Usage

```
statespace(X, y, kalman_params = NULL, viking_params = NULL, ...)
```

Arguments

X	design matrix.
y	variable of interest.
kalman_params	(default NULL) list containing initial values for theta, P as well as the variances (Q, sig). If it is not specified, the state-space model is constructed in the static setting (theta=0, P=I, Q=0, sig=1).
viking_params	(default NULL) list of parameters for the Viking algorithm.
...	additional parameters

Value

a statespace object.

Examples

```
set.seed(1)
### Simulate data
n <- 1000
d <- 5
Q <- diag(c(0,0,0.25,0.25,0.25))
sig <- 1

X <- cbind(matrix(rnorm((d-1)*n, sd=1), n, d-1), 1)
theta <- matrix(rnorm(d), d, 1)
theta_arr <- matrix(0, n, d)
for (t in 1:n) {
  theta_arr[t,] <- theta
  theta <- theta + matrix(mvtnorm::rmvnorm(1, matrix(0, d, 1), Q), d, 1)
}
y <- rowSums(X * theta_arr) + rnorm(n, sd=sig)

#####
### Kalman Filter
# Default Static Setting
ssm <- viking::statespace(X, y)
plot(ssm)

# Known variances
ssm <- viking::statespace(X, y, kalman_params = list(Q=Q, sig=sig))
plot(ssm)
```

Description

`viking` is the state-space estimation realized by Viking, generalizing the Kalman Filter to variance uncertainty.

Usage

```
viking(
  X,
  y,
  theta0,
  P0,
  hata0,
  s0,
  hatb0,
  Sigma0,
  n_iter = 2,
  mc = 10,
  rho_a = 0,
  rho_b = 0,
  learn_sigma = TRUE,
  learn_Q = TRUE,
  K = NULL,
  mode = "diagonal",
  thresh = TRUE,
  phi = logt,
  phi1 = logt1,
  phi2 = logt2
)
```

Arguments

X	the explanatory variables
y	the time series
theta0	initial theta
P0	initial P
hata0	initial hata
s0	initial s
hatb0	initial hatb
Sigma0	initial Sigma
n_iter	(optional, default 2) number of alternate steps
mc	(optional, default 10) number of Monte-Carlo samples
rho_a	(optional, default 0) learning rate of a
rho_b	(optional, default 0) learning rate of b
learn_sigma	(optional, default TRUE) asserts the estimation of a
learn_Q	(optional, default TRUE) asserts the estimation of b
K	(optional, default NULL) if not NULL then it is a multiplicative factor of the state in the state update
mode	(optional, default 'diagonal')

thresh	(optional, default TRUE)
phi	(optional, default logt)
phi1	(optional, default logt1)
phi2	(optional, default logt2)

Value

a list composed of the evolving value of all the parameters: `theta_arr`, `P_arr`, `q_arr`, `hata_arr`, `s_arr`, `hatb_arr`, `Sigma_arr`

References

J. de Vilmarest, O. Wintenberger (2021), Viking: Variational Bayesian Variance Tracking. <arXiv:2104.10777>

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