

# Package ‘stfit’

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**Type** Package

**Title** Spatio-Temporal Functional Imputation Tool

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**Description** A general spatiotemporal satellite image imputation method based on sparse functional data analytic techniques. The imputation method applies and extends the Functional Principal Analysis by Conditional Estimation (PACE). The underlying idea for the proposed procedure is to impute a missing pixel by borrowing information from temporally and spatially contiguous pixels based on the best linear unbiased prediction.

**BugReports** <https://github.com/mingsnu/stfit/issues>

**License** GPL-3

**LazyData** true

**Depends** R (>= 3.5.0)

**Imports** Rcpp, Matrix, doParallel, foreach, abind, fda, raster,  
rasterVis, RColorBrewer

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stfit-package*stfit: Spatial-Temporal Functional Imputation Tool*

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**Description**

The stfit package provides functions to impute missing values for a sequence of observed images for the same location using functional data analysis technique

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ARE*Absolute relative error*

---

**Description**

Absolute relative error

**Usage**

```
ARE(y, ypred)
```

**Arguments**

y	vector
ypred	vector

**Value**

numeric number. A measure of difference between y and ypred.

---

epan	<i>Epanicnicov kernel function</i>
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**Description**

Epanicnicov kernel function

**Usage**

epan(x)

**Arguments**

x	numeric vector
---	----------------

**Value**

vector

---

getMask	<i>Get image mask</i>
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---

**Description**

Get image mask

**Usage**

getMask(object, tol = 0.95)

**Arguments**

object	A numeric matrix. Each row is an row stacked image.
tol	If the percentage of missing values for a pixel over time is greater than this value, this pixel is treated as a mask value.

---

getMissingLayers	<i>Get missing layer index</i>
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---

### Description

Get missing layer index

### Usage

```
getMissingLayers(rst.list)
```

### Arguments

rst.list	a RasterStack or RasterBrick object or a list of them
----------	-------------------------------------------------------

### Value

index of the missing layers

---

landsat106	<i>Landsat data example</i>
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### Description

A dataset containing observation values of a 31x31 pixels landsat image observed between year 1982 and 2015.

### Usage

```
landsat106
```

```
landsat2
```

### Format

A data frame with 990 rows and 963 columns:

- year year
- doy day of the year
- pixeli pixel value for the i-th pixel of the image

An object of class `tbl_df` (inherits from `tbl, data.frame`) with 990 rows and 963 columns.

---

<code>landsatVis</code>	<i>Data visualization for landsat data</i>
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---

## Description

Data visualization for landsat data

## Usage

```
landsatVis(
  mat,
  img.nrow = 31,
  byrow = FALSE,
  colthm = rasterTheme(panel.background = list(col = "black"), region = brewer.pal(9,
    "YlOrRd")),
  ...
)
```

## Arguments

<code>mat</code>	A matrix, each row corresponds to a vectorized image pixel values.
<code>img.nrow</code>	number of rows of the image
<code>byrow</code>	logical value indicating whether the pixcel values are stored by row or by column. Default to FALSE
<code>colthm</code>	Color theme for the plot, passing to the <code>par.settings</code> parameter of the <code>levelplot</code> function in the <code>rasterVis</code> package
<code>...</code>	All other options passed to <code>levelplot</code> function in the <code>rasterVis</code> package

## Examples

```
landsatVis(landsat106[landsat106$year == 2015, -c(1:2)],
  names.attr = as.character(landsat106$doy[landsat106$year == 2015]))
```

---

<code>lc_cov_1d</code>	<i>Local constant covariance estimation</i>
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---

## Description

Local constant covariance estimation

## Usage

```
lc_cov_1d(ids, time, resid, W, t1, t2)
```

**Arguments**

<code>ids</code>	a vector indicating subject/group ids
<code>time</code>	integer vector of observed time points, the minimum time unit is 1
<code>resid</code>	vector of residual values used for covariance calculation
<code>W</code>	weight vector, it contains both kernel and bandwidth information in general local polynomial estimation setting up
<code>t1</code>	time point 1
<code>t2</code>	time point 2

`lc_cov_1d_est`*Local constant covariance estimation***Description**

Local constant covariance estimation

**Usage**

```
lc_cov_1d_est(ids, time, resid, W, tt)
```

**Arguments**

<code>ids</code>	a vector indicating subject/group ids
<code>time</code>	integer vector of observed time points, the minimum time unit is 1
<code>resid</code>	vector of residual values used for covariance calculation
<code>W</code>	weight vector, it contains both kernel and bandwidth information in general local polynomial estimation setting up
<code>tt</code>	time vector

`llreg`*Local linear regression***Description**

Local linear regression

**Usage**

```
llreg(x, y, x.eval = x, minimum.num.obs = 4, h = 60, Kern = epan)
```

**Arguments**

x	independent variable
y	response variable
x.eval	dnew data to predict on
minimum.num.obs	minimum number of observations needed to run the regression
h	bandwidth
Kern	Kernel

**Value**

predicted values at 'x.eval'

---

lpreg*Local Polynomial Regression*

---

**Description**

Local Polynomial Regression

**Usage**

```
lpreg(x, y, x.eval, minimum.num.obs = 4, span = 0.3, ...)
```

**Arguments**

x	independent variable
y	response variable
x.eval	vector to predict on
minimum.num.obs	minimum number of observations needed to run the regression
span	see 'loess' function
...	other parameters passed to 'loess' function

**Value**

predicted values at 'x.eval'

---

<b>meanEst</b>	<i>STFIT Mean Estimation</i>
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## Description

The function is used for pixel-wise mean estimation.

## Usage

```
meanEst(
  doy,
  mat,
  doyeval = seq(min(doy), max(doy)),
  msk = rep(FALSE, ncol(mat)),
  outlier.tol = 0.5,
  minimum.num.obs = 4,
  cluster = NULL,
  redo = TRUE,
  clipRange = c(-Inf, Inf),
  clipMethod = c("truncate", "nnr"),
  img.nrow = NULL,
  img.ncol = NULL
)
```

## Arguments

<code>doy</code>	vector of day of year (DOY) index
<code>mat</code>	data matrix. Each row contains a row stacked image pixel values.
<code>doyeval</code>	a vector of DOY on which to get the mean imputation
<code>msk</code>	an optional logistic vector. TRUE represent the corresponding pixel is always missing.
<code>outlier.tol</code>	the tolerance value in defining an image as outlier. The percent of outlier pixels in an image exceed this value is regarded as outlier image which will not be used in temporal mean estimation.
<code>minimum.num.obs</code>	minimum number of observations needed for mean estimation. Too few observations may lead to big estimation error.
<code>cluster</code>	an optional vector defining clusters of pixels. If NULL, mean estimation is conducted on each pixel, otherwise all pixels from the same cluster are combined for mean estimation.
<code>redo</code>	whether to recalculate the mean estimation if there is an outlier (only redo once).
<code>clipRange</code>	vector of length 2, specifying the minimum and maximum values of the prediction value
<code>clipMethod</code>	"nnr" or "truncate". "nnr" uses average of nearest neighbor pixels to impute; "truncate" use the clipRange value to truncate.

```



```

## Details

There are several predefined methods for mean estimation: `smooth_spline`, `llreg`, `lpreg` and `spreg`. User can use `opt$get()` to check the current registered method and use `opt$set()` function to set the method. For example, one can run `opt$set(smooth_spline)` first and then run the `meanEst` function to use smoothing spline regression for mean estimation. User can also customize the methods for mean estimation. For example, mean estimation through fourier basis expansion:

```

.X = fda::eval.basis(1:365, fda::create.fourier.basis(rangeval=c(0,365), nbasis=11))
customfun <- function(x, y, x.eval=1:365, minimum.num.obs = 10){
  nonna.idx = !is.na(y)
  if(sum(nonna.idx) < minimum.num.obs)
    return(rep(NA, 365))
  ## lmfit = lm.fit(.X[unlist(lapply(x, function(x) which(x == x.eval))),], y[nonna.idx])
  lmfit = lm.fit(.X[x[nonna.idx],], y[nonna.idx])
  return(.X[x.eval,])
}
stfit::opts_stfit$set(temporal_mean_est = customfun)

```

## Value

a list containing the following entries:

- `doyeval`: same as input `doyeval`
- `meanmat`: estimated mean matrix, with number of rows equals length of `doyeval` and number of columns equal `ncol(mat)`
- `idx`: a list of image indexes
  - `idx.allmissing`: completely missing image indexes,
  - `idx.partialmissing`: partially observed image indexes,
  - `idx.fullyobserved`: fully observed image indexes,
  - `idx.outlier`: outlier image indexes.
- `outlier`: a list of image outliers information
  - `outidx`: index of the outlier image
  - `outpct`: percentage of outlier pixels corresponding to `outidx`,
  - `outlst`: a list of the same length as `outidx`, with each list the missing pixel index.

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NMSE

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*Normalized Mean Square Estimation*

---

### Description

Normalized Mean Square Estimation

### Usage

`NMSE(y, ypred)`

### Arguments

y	vector
ypred	vector

### Value

numeric number. A measure of difference between y and ypred.

---

`opts_stfit`

---

*Options for stfit*

---

### Description

Options for stfit

### Usage

`opts_stfit`

### Format

An object of class `list` of length 3.

---

outlier	<i>Image Outlier Detection</i>
---------	--------------------------------

---

**Description**

Image Outlier Detection

**Usage**

```
outlier(mat)
```

**Arguments**

mat data matrix. Each row is a row stacked image.

**Value**

a list containing the following entries:

- outidx: index of the outlier image
- outpct: percentage of outlier pixels corresponding to outidx,
- outlst: a list of the same length as outidx, with each list the missing pixel index.

**Examples**

```
dfB = landsat106[landsat106$year >= 2000,]  
matB = as.matrix(dfB[,-c(1:2)])  
outlier(matB)
```

---

pctMissing	<i>Missing value percentages</i>
------------	----------------------------------

---

**Description**

Missing value percentages

**Usage**

```
pctMissing(x, mc.cores)
```

**Arguments**

x	A RasterStack object
mc.cores	Numer of cores to use

**Value**

A vector of percent of missing values for each layer

---

**rmOutlier***Remove outlier*

---

**Description**

An outlier is defined as points outside the whiskers of the boxplot over the time domain (DOY).

**Usage**

```
rmOutlier(rst)
```

**Arguments**

**rst**                  a \*Raster object

**Value**

a \*Raster object

---

**RMSE***Root Mean Square Estimation*

---

**Description**

Root Mean Square Estimation

**Usage**

```
RMSE(y, ypred)
```

**Arguments**

**y**                  vector  
**ypred**              vecotr

**Value**

numeric number. A measure of difference between y and ypred.

---

<i>seffEst</i>	<i>STFIT Spatial Effect Estimation</i>
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---

**Description**

STFIT Spatial Effect Estimation

**Usage**

```
seffEst(
  rmat,
  img.nrow,
  img.ncol,
  h.cov = 2,
  h.sigma2 = 2,
  weight.cov = NULL,
  weight.sigma2 = NULL,
  nnr,
  method = c("lc", "emp"),
  partial.only = TRUE,
  pve = 0.99,
  msk = NULL,
  msk.tol = 0.95,
  var.est = FALSE
)
```

**Arguments**

<code>rmat</code>	residual matrix
<code>img.nrow</code>	image row dimension
<code>img.ncol</code>	image column dimension
<code>h.cov</code>	bandwidth for spatial covariance estimation; ignored if <code>weight.cov</code> is supplied
<code>h.sigma2</code>	bandwidth for sigma2 estimation
<code>weight.cov</code>	weight matrix for spatial covariance estimation
<code>weight.sigma2</code>	weight vector for spatial variance estimation
<code>nnr</code>	maximum number of nearest neighbor pixels to use for spatial covariance estimation
<code>method</code>	"lc" for local constant covariance estimation and "emp" for empirical covariance estimation
<code>partial.only</code>	calculate the spatial effect for partially observed images only, default is TRUE
<code>pve</code>	percent of variance explained of the selected eigen values. Default is 0.99.
<code>msk</code>	an optional logistic vector. TRUE represent the corresponding pixel is always missing.

<code>msk.tol</code>	if 'msk' is not given, the program will determine the mask using <code>getMask</code> function. If the percentage of missing values for a pixel over time is greater than this
<code>var.est</code>	Whether to estimate the variance of the temporal effect. Default is FALSE.

**Value**

List of length 3 with entries:

- `seff_mat`: estimated spatial effect matrix of the same shape as `rmat`.
- `seff_var_mat`: estimated spatial effect variance matrix of the same shape as `rmat`.
- `idx`: a list of two entries:
  - `idx.allmissing`: index of the completely missing images.
  - `idx.imputed`: index of the partially observed images, where spatial effects are estimated.

<code>smooth_spline</code>	<i>Smoothing spline regression</i>
----------------------------	------------------------------------

**Description**

Smoothing spline regression

**Usage**

```
smooth_spline(x, y, x.eval = x, minimum.num.obs = 4, ...)
```

**Arguments**

<code>x</code>	independent variable
<code>y</code>	response variable
<code>x.eval</code>	vector to predict on
<code>minimum.num.obs</code>	minimum number of observations needed to run the regression
<code>...</code>	other parameters to be passed to <code>smooth.spline</code> function

**Value**

predicted values at '`x.eval`'

---

spreg	<i>spline regression</i>
-------	--------------------------

---

## Description

spline regression

## Usage

```
spreg(  
  x,  
  y,  
  x.eval,  
  minimum.num.obs = 4,  
  basis = c("fourier", "bspline"),  
  rangeval = c(min(x.eval) - 1, max(x.eval)),  
  nbasis = 11,  
  ...  
)
```

## Arguments

x	independent variable
y	response variable
x.eval	vector to predict on
minimum.num.obs	minimum number of observations needed to run the regression
basis	what basis to use, "fourier" and "bspline" are available
rangeval	see <code>fda::create.basis</code>
nbasis	see <code>fda::create.basis</code>
...	arguments passed to <code>fad::create.basis</code> functions

## Value

predicted values at 'x.eval'

---

stfit_landsat	<i>STFIT for Landsat data</i>
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---

### Description

This function is used for Landsat data imputation, which includes five steps: mean estimation, outlier detection, temporal effect estimation, spatial effect estimation and imputation. In real application, one can use this as a template to create a five steps imputation procedure depending on the real data structure.

### Usage

```
stfit_landsat(
  year,
  doy,
  mat,
  img.nrow,
  img.ncol,
  doyeval = 1:365,
  h.tcov = 100,
  h.tsigma2 = 300,
  h.scov = 2,
  h.ssigma2 = 2,
  nnr = 10,
  outlier.action = c("keep", "remove"),
  outlier.tol = 0.2,
  intermediate.save = TRUE,
  intermediate.dir = "./intermediate_output/",
  use.intermediate.result = TRUE,
  teff = TRUE,
  seff = TRUE,
  doy.break = NULL,
  cycle = FALSE,
  t.grid = NULL,
  t.grid.num = 50,
  clipRange = c(0, 1800),
  clipMethod = "nnr",
  var.est = FALSE
)
```

### Arguments

<code>year</code>	vecotr of year
<code>doy</code>	vecotr of DOY (day of the year)
<code>mat</code>	a numeric matrix. Each row contains a row stacked image pixel values.
<code>img.nrow</code>	number of rows of the image

<code>img.ncol</code>	number of columns of the image
<code>doyeval</code>	a vector of DOY on which to get the mean and temporal imputation
<code>h.tcov</code>	bandwidth for temporal covariance estimation
<code>h.tsigma2</code>	bandwith for temporal variance estimation
<code>h.scov</code>	bandwidth for spatial covariance estimation
<code>h.ssigma2</code>	bandwidth for spatial variance estimation
<code>nrr</code>	maximum number of nearest neighbor pixels to use for spatial covariance estimation
<code>outlier.action</code>	"keep" to keep outliers; "remove" to replace outliers with imputed values
<code>outlier.tol</code>	The threshold to use to define outlier image. Default is 0.2, i.e. images with more than 20% outlier pixels are treated as outlier image.
<code>intermediate.save</code>	TRUE or FALSE; whether to save the intermediate results including mean, temporal effect and spacial effect imputation results. The intermediate results can be useful to avoid duplicating the computation for some imputation steps.
<code>intermediate.dir</code>	directory where to save the intermediate results
<code>use.intermediate.result</code>	whether to use the intermediate results in the 'intermediate.dir' folder. Default is TRUE.
<code>teff</code>	TRUE or FALSE, wheter to calculate the temporal effect. Default is TRUE.
<code>seff</code>	TRUE or FALSE, wheter to calculate the spatial effect. Default is TRUE.
<code>doy.break</code>	a vector of break points for doy where the spatial effect are estimated seperately on each interval. Default is NULL, i.e. the spatial effect is assumed to be the same over doy.
<code>cycle</code>	TRUE or FALSE. When <code>doy.break</code> is specified, whether to combine the first <code>doy.break</code> interval and the last <code>doy.break</code> together for spatial effect estimation.
<code>t.grid</code>	a vector of grid points on which to calculate the temporal covariance function
<code>t.grid.num</code>	number of grid points to use for temporal covariance estimation. Ignored if <code>t.grid</code> is given.
<code>clipRange</code>	passed to <code>meanEst</code> function
<code>clipMethod</code>	passed to <code>meanEst</code> function
<code>var.est</code>	Whether to estimate the variance of the temporal and spatial effects. Default is FALSE.

## Value

List of length 4 with entries:

- `imat`: imputed matrix of `mat`
- `smat`: standard error matrix of the same size as `mat`
- `idx`: a list of image indexes

- idx.allmissing: completely missing image indexes,
- idx.partialmissing: partially observed image indexes,
- idx.fullyobserved: fully observed image indexes,
- idx.outlier: outlier image indexes.
- outlier: a list of image outliers information
  - outidx: image index with outlier pixels,
  - outpct: percentage of outlier pixels corresponding to outidx,
  - outlst: a list of the same length as outidx, with each list the missing pixel index.

## Examples

```

library(doParallel)
library(raster)
library(rasterVis)
library(RColorBrewer)
dfB = landsat106[landsat106$year >= 2000,]
matB = as.matrix(dfB[,-c(1:2)])
year = dfB$year
doy = dfB$doy
if(require(doParallel))
  registerDoParallel(1)
res <- stfit_landsat(year, doy, matB, 31, 31, nnr=30,
use.intermediate.result = FALSE, intermediate.save = FALSE, var.est = TRUE)
## visualize the imputed results
idx = c(res$idx$idx.allmissing[150], res$idx$idx.partialmissing[c(30, 60, 90)])
rst_list = list()
for(i in 1:length(idx)){
  rst_list[(i-1)*3+1] = raster(matrix(matB[idx[i],], 31))
  rst_list[(i-1)*3+2] = raster(matrix(res$imat[idx[i],], 31))
  rst_list[(i-1)*3+3] = raster(matrix(res$sdmat[idx[i],], 31))
}
s = stack(rst_list)
levelplot(s, index.cond=list(c(seq(1, 12, 3), seq(2, 12, 3), seq(3, 12, 3))),
          par.setting = rasterTheme(panel.background=list(col="black"),
                                    region = brewer.pal(9, 'YlOrRd')),
          names.attr = c(rbind(paste0("Original ", idx),
                               paste0("Imputed ", idx),
                               paste0("Std. Error ", idx))),
          layout = c(4,3))

```

## Description

STFIT Temporal Effect Estimation

**Usage**

```
teffEst(
  ids,
  doy,
  rmat,
  doyeval = seq(min(doy), max(doy)),
  h.cov = 100,
  h.sigma2 = 300,
  weight.cov = NULL,
  weight.sigma2 = NULL,
  pve = 0.99,
  t.grid = NULL,
  t.grid.num = 50,
  var.est = FALSE
)
```

**Arguments**

ids	ids for 'group', for data with repeated measurement over years, year is ids; for pixels belong to certain clusters, cluster is ids.
doy	vector of DOY (day of the year)
rmat	residual matrix with rows corresponding to doy and columns corresponding to pixel index
doyeval	a vector of DOY on which to get the temporal imputation
h.cov	bandwidth for temporal covariance estimation; ignored if weight.cov is supplied
h.sigma2	bandwidth for temporal variance estimation
weight.cov	weight vector for temporal covariance estimation
weight.sigma2	weight vector for temporal variance estimation
pve	percentage of variance explained; used for number of eigen values selection. Default is 0.99.
t.grid	a vector of grid points on which to calculate the temporal covariance function
t.grid.num	number of grid points to use for temporal covariance estimation. Ignored if t.grid is given.
var.est	Whether to estimate the variance of the temporal effect. Default is FALSE.

**Value**

List of length 2 with entries:

- teff\_array: 3-d array with first dimension 'ids', second dimension 'doy' and third dimension pixel index.
- teff\_var\_array: same structure as teff\_array if var.est is TRUE, otherwise NULL.

---

`weightMatrix`                  *Weight matrix calculation*

---

**Description**

Weight matrix calculation

**Usage**

`weightMatrix(h)`

**Arguments**

`h`                  'bandwidth'

**Value**

a weighting matrix

---

`weightVector`                  *Weight vector calculation*

---

**Description**

Weight vector calculation

**Usage**

`weightVector(h)`

**Arguments**

`h`                  bandwidth, should be positive numbers

**Value**

a vector

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