Package 'stdReg2'

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Description Contains more modern tools for causal inference using regression standardization. Four general classes of models are implemented; generalized linear models, conditional generalized estimating equation models, Cox proportional hazards models, and shared frailty gamma-Weibull models. Methodological details are described in Sjölander, A. (2016) <doi:10.1007/s10654-016-0157-3>. Also includes functionality for doubly robust estimation for generalized linear models in some special cases, and the ability to implement custom models.

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stdReg2-package

stdReg2: Regression Standardization for Causal Inference

Description

Contains more modern tools for causal inference using regression standardization. Four general classes of models are implemented; generalized linear models, conditional generalized estimating equation models, Cox proportional hazards models, and shared frailty gamma-Weibull models. Methodological details are described in Sjölander, A. (2016) doi:10.1007/s1065401601573. Also includes functionality for doubly robust estimation for generalized linear models in some special cases, and the ability to implement custom models.

Author(s)

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- Arvid Sjölander
- Erin E Gabriel
- Johan Sebastian Ohlendorff
- Adam Brand

parfrailty

See Also

Useful links:

- https://sachsmc.github.io/stdReg2/
- Report bugs at https://github.com/sachsmc/stdReg2/issues/

parfrailty

Fits shared frailty gamma-Weibull models

Description

parfrailty fits shared frailty gamma-Weibull models. It is specifically designed to work with the function standardize_parfrailty, which performs regression standardization in shared frailty gamma-Weibull models.

Usage

parfrailty(formula, data, clusterid, init)

Arguments

formula	an object of class "formula", in the same format as accepted by the coxph func- tion.
data	a data frame containing the variables in the model.
clusterid	a string containing the name of a cluster identification variable.
init	an optional vector of initial values for the model parameters.

Details

parfrailty fits the shared frailty gamma-Weibull model

$$\lambda(t_{ij}|C_{ij}) = \lambda(t_{ij};\alpha,\eta)U_i \exp\{h(C_{ij};\beta)\},\$$

where t_{ij} and C_{ij} are the survival time and covariate vector for subject j in cluster i, respectively. $\lambda(t; \alpha, \eta)$ is the Weibull baseline hazard function

$$\eta t^{\eta-1} \alpha^{-\eta},$$

where η is the shape parameter and α is the scale parameter. U_i is the unobserved frailty term for cluster *i*, which is assumed to have a gamma distribution with scale = 1/shape = ϕ . $h(X;\beta)$ is the regression function as specified by the formula argument, parameterized by a vector β . The ML estimates { $\log(\hat{\alpha}), \log(\hat{\eta}), \log(\hat{\phi}), \hat{\beta}$ } are obtained by maximizing the marginal (over U) likelihood.

Value

An object of class "parfrailty" which is a list containing:

est	the Maximum Likelihood (ML) estimates $\{\log(\hat{\alpha}), \log(\hat{\eta}), \log(\phi), \beta\}$.
VCOV	the variance-covariance vector of the ML estimates.
score	a matrix containing the cluster-specific contributions to the ML score equations.

If left truncation is present, it is assumed that it is strong left truncation. This means that even if the truncation time may be subject-specific, the whole cluster is unobserved if at least one subject in the cluster dies before his/her truncation time. If all subjects in the cluster survive beyond their subject-specific truncation times, then the whole cluster is observed (Van den Berg and Drepper, 2016).

Author(s)

Arvid Sjölander and Elisabeth Dahlqwist.

References

Dahlqwist E., Pawitan Y., Sjölander A. (2019). Regression standardization and attributable fraction estimation with between-within frailty models for clustered survival data. *Statistical Methods in Medical Research* **28**(2), 462-485.

Van den Berg G.J., Drepper B. (2016). Inference for shared frailty survival models with left-truncated data. *Econometric Reviews*, 35(6), 1075-1098.

Examples

require(survival)

```
# simulate data
set.seed(5)
n <- 200
m <- 3
alpha <- 1.5
eta <- 1
phi <- 0.5
beta <- 1
id <- rep(1:n, each = m)
U <- rep(rgamma(n, shape = 1 / phi, scale = phi), each = m)</pre>
X <- rnorm(n * m)
# reparameterize scale as in rweibull function
weibull.scale <- alpha / (U * exp(beta * X))^(1 / eta)</pre>
T <- rweibull(n * m, shape = eta, scale = weibull.scale)</pre>
# right censoring
C <- runif(n * m, 0, 10)
D \le as.numeric(T \le C)
T <- pmin(T, C)
# strong left-truncation
L <- runif(n * m, 0, 2)
incl <- T > L
incl <- ave(x = incl, id, FUN = sum) == m</pre>
dd <- data.frame(L, T, D, X, id)
dd <- dd[incl, ]</pre>
```

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Note

plot.std_glm

```
fit <- parfrailty(formula = Surv(L, T, D) ~ X, data = dd, clusterid = "id")
print(fit)</pre>
```

plot.std_glm Plots regression standardization fit

Description

This is a plot method for class "std_glm".

Usage

```
## S3 method for class 'std_glm'
plot(
    x,
    plot_ci = TRUE,
    ci_type = "plain",
    ci_level = 0.95,
    transform = NULL,
    contrast = NULL,
    reference = NULL,
    summary_fun = "summary_std_glm",
    ...
)
```

Arguments

х	An object of class "std_glm".
plot_ci	if TRUE, add the confidence intervals to the plot.
ci_type	A string, indicating the type of confidence intervals. Either "plain", which gives untransformed intervals, or "log", which gives log-transformed intervals.
ci_level	Coverage probability of confidence intervals.
transform	If set to "log", "logit", or "odds", the standardized mean $\theta(x)$ is transformed into $\psi(x) = \log\{\theta(x)\}, \psi(x) = \log[\theta(x)/\{1 - \theta(x)\}]$, or $\psi(x) = \theta(x)/\{1 - \theta(x)\}$, respectively. If left unspecified, $\psi(x) = \theta(x)$.
contrast	If set to "difference" or "ratio", then $\psi(x) - \psi(x_0)$ or $\psi(x)/\psi(x_0)$ are constructed, where x_0 is a reference level specified by the reference argument. If not NULL, a doubly robust estimator of the standardized estimator is used.
reference	If contrast is specified, the desired reference level.
summary_fun	For internal use only. Do not change.
	Unused.

Value

None. Creates a plot as a side effect

Examples

see standardize_glm

plot.std_surv Plots regression standardization fit

Description

This is a plot method for class "std_surv".

Usage

```
## S3 method for class 'std_surv'
plot(
    x,
    plot_ci = TRUE,
    ci_type = "plain",
    ci_level = 0.95,
    transform = NULL,
    contrast = NULL,
    reference = NULL,
    legendpos = "bottomleft",
    summary_fun = "summary_std_coxph",
    ...
)
```

Arguments

х	An object of class "std_surv".
plot_ci	if TRUE, add the confidence intervals to the plot.
ci_type	A string, indicating the type of confidence intervals. Either "plain", which gives untransformed intervals, or "log", which gives log-transformed intervals.
ci_level	Coverage probability of confidence intervals.
transform	If set to "log", "logit", or "odds", the standardized mean $\theta(x)$ is transformed into $\psi(x) = \log\{\theta(x)\}, \psi(x) = \log[\theta(x)/\{1 - \theta(x)\}]$, or $\psi(x) = \theta(x)/\{1 - \theta(x)\}$, respectively. If left unspecified, $\psi(x) = \theta(x)$.
contrast	If set to "difference" or "ratio", then $\psi(x) - \psi(x_0)$ or $\psi(x)/\psi(x_0)$ are constructed, where x_0 is a reference level specified by the reference argument. If not NULL, a doubly robust estimator of the standardized estimator is used.
reference	If contrast is specified, the desired reference level.
legendpos	position of the legend; see legend.
summary_fun	For internal use only. Do not change.
	Unused.

print.std_surv

Value

None. Creates a plot as a side effect

print.std_surv Prints summary of regression standardization fit

Description

Prints summary of regression standardization fit

Usage

S3 method for class 'std_surv'
print(x, ...)
S3 method for class 'std_glm'
print(x, ...)

S3 method for class 'std_custom'
print(x, ...)

Arguments

х	an object of class "std_glm", "std_surv" or "std_custom".
	unused

Value

The object being printed, invisibly.

print.summary.parfrailty

Print method for parametric frailty fits

Description

Print method for parametric frailty fits

Usage

```
## S3 method for class 'summary.parfrailty'
print(x, digits = max(3L, getOption("digits") - 3L), ...)
```

sandwich

Arguments

x	An object of class "parfrailty"
digits	Number of digits to print
	Not used

Value

The object being printed, invisibly

sandwich	Compute the sandwich variance components from a model fit	

Description

Compute the sandwich variance components from a model fit

Usage

```
sandwich(fit, data, weights, t, fit.detail)
```

Arguments

fit	A fitted model object of class glm, coxph, ah, or survfit
data	The data used to fit the model
weights	Optional weights
t	Optional fixed time point for survival objects
fit.detail	For Cox models, the result of running coxph.detail on the model fit

Value

A list consisting of the Fisher information matrix (I) and the Score equations (U)

standardize

Description

Get standardized estimates using the g-formula with a custom model

Usage

```
standardize(
   fitter,
   arguments,
   predict_fun,
   data,
   values,
   B = NULL,
   ci_level = 0.95,
   contrasts = NULL,
   reference = NULL,
   seed = NULL,
   times = NULL,
   transforms = NULL,
   progressbar = TRUE
)
```

Arguments

fitter	The function to call to fit the data.
arguments	The arguments to be used in the fitter function as a list.
predict_fun	The function used to predict the means/probabilities for a new data set on the response level. For survival data, this should be a matrix where each column is the time, and each row the data.
data	The data.
values	A named list or data.frame specifying the variables and values at which marginal means of the outcome will be estimated.
В	Number of nonparametric bootstrap resamples. Default is NULL (no bootstrap).
ci_level	Coverage probability of confidence intervals.
contrasts	A vector of contrasts in the following format: If set to "difference" or "ratio", then $\psi(x) - \psi(x_0)$ or $\psi(x)/\psi(x_0)$ are constructed, where x_0 is a reference level specified by the reference argument. Has to be NULL if no references are specified.
reference	A vector of reference levels in the following format: If contrasts is not NULL, the desired reference level(s). This must be a vector or list the same length as contrasts, and if not named, it is assumed that the order is as specified in contrasts.

standardize

seed	The seed to use with the nonparametric bootstrap.
times	For use with survival data. Set to NULL otherwise.
transforms	A vector of transforms in the following format: If set to "log", "logit", or "odds", the standardized mean $\theta(x)$ is transformed into $\psi(x) = \log\{\theta(x)\}$, $\psi(x) = \log[\theta(x)/\{1-\theta(x)\}]$, or $\psi(x) = \theta(x)/\{1-\theta(x)\}$, respectively. If the vector is NULL, then $\psi(x) = \theta(x)$.
progressbar	Logical, if TRUE will print bootstrapping progress to the console

Details

Let Y, X, and Z be the outcome, the exposure, and a vector of covariates, respectively. standardize uses a model to estimate the standardized mean $\theta(x) = E\{E(Y|X = x, Z)\}$, where x is a specific value of X, and the outer expectation is over the marginal distribution of Z. With survival data, Y = I(T > t), and a vector of different time points times (t) can be given, where T is the uncensored survival time.

Value

An object of class std_custom. Obtain numeric results using tidy.std_custom. This is a list with the following components:

- **res_contrast** An unnamed list with one element for each of the requested contrasts. Each element is itself a list with the elements:
 - **B** The number of bootstrap replicates

estimates Estimated counterfactual means and standard errors for each exposure level

fit_outcome The estimated regression model for the outcome

estimates_boot A list of estimates, one for each bootstrap resample

exposure_names A character vector of the exposure variable names

times The vector of times at which the calculation is done, if relevant

est_table Data.frame of the estimates of the contrast with inference

transform The transform argument used for this contrast

contrast The requested contrast type

reference The reference level of the exposure

ci_level Confidence interval level

res A named list with the elements:

B The number of bootstrap replicates

estimates Estimated counterfactual means and standard errors for each exposure level
fit_outcome The estimated regression model for the outcome
estimates_boot A list of estimates, one for each bootstrap resample
exposure_names A character vector of the exposure variable names
times The vector of times at which the calculation is done, if relevant

standardize

References

Rothman K.J., Greenland S., Lash T.L. (2008). *Modern Epidemiology*, 3rd edition. Lippincott, Williams & Wilkins.

Sjölander A. (2016). Regression standardization with the R-package stdReg. *European Journal of Epidemiology* **31**(6), 563-574.

Sjölander A. (2016). Estimation of causal effect measures with the R-package stdReg. *European Journal of Epidemiology* **33**(9), 847-858.

```
set.seed(6)
n <- 100
Z <- rnorm(n)
X \leq rnorm(n, mean = Z)
Y \le rbinom(n, 1, prob = (1 + exp(X + Z))^{(-1)})
dd <- data.frame(Z, X, Y)
prob_predict.glm <- function(...) predict.glm(..., type = "response")</pre>
x <- standardize(</pre>
  fitter = "glm",
  arguments = list(
    formula = Y \sim X * Z,
    family = "binomial"
  ),
  predict_fun = prob_predict.glm,
  data = dd,
  values = list(X = seq(-1, 1, 0.1)),
  B = 100,
  reference = 0,
  contrasts = "difference"
)
х
require(survival)
prob_predict.coxph <- function(object, newdata, times) {</pre>
  fit.detail <- suppressWarnings(basehaz(object))</pre>
 cum.haz <- fit.detail$hazard[sapply(times, function(x) max(which(fit.detail$time <= x)))]</pre>
  predX <- predict(object = object, newdata = newdata, type = "risk")</pre>
  res <- matrix(NA, ncol = length(times), nrow = length(predX))</pre>
  for (ti in seq_len(length(times))) {
    res[, ti] <- exp(-predX * cum.haz[ti])</pre>
  }
  res
}
set.seed(68)
n <- 500
Z <- rnorm(n)
X \leq rnorm(n, mean = Z)
T \leq rexp(n, rate = exp(X + Z + X * Z)) # survival time
C \leq rexp(n, rate = exp(X + Z + X * Z)) # censoring time
U <- pmin(T, C) # time at risk
```

```
D <- as.numeric(T < C) # event indicator</pre>
dd <- data.frame(Z, X, U, D)
x <- standardize(</pre>
fitter = "coxph",
 arguments = list(
    formula = Surv(U, D) ~ X + Z + X * Z,
   method = "breslow",
   x = TRUE,
   y = TRUE
 ),
 predict_fun = prob_predict.coxph,
 data = dd,
 times = 1:5,
 values = list(X = c(-1, 0, 1)),
 B = 100,
 reference = 0,
 contrasts = "difference"
)
Х
```

standardize_coxph Regression standardization in Cox proportional hazards models

Description

standardize_coxph performs regression standardization in Cox proportional hazards models at specified values of the exposure over the sample covariate distribution. Let T, X, and Z be the survival outcome, the exposure, and a vector of covariates, respectively. standardize_coxph fits a Cox proportional hazards model and the Breslow estimator of the baseline hazard in order to estimate the standardized survival function $\theta(t, x) = E\{S(t|X = x, Z)\}$ when measure = "survival" or the standardized restricted mean survival up to time t $\theta(t, x) = E\{\int_0^t S(u|X = x, Z)du\}$ when measure = "rmean", where t is a specific value of T, x is a specific value of X, and the expectation is over the marginal distribution of Z.

Usage

```
standardize_coxph(
  formula,
  data,
  values,
  times,
  measure = c("survival", "rmean"),
  clusterid,
  ci_level = 0.95,
  ci_type = "plain",
  contrasts = NULL,
  family = "gaussian",
  reference = NULL,
  transforms = NULL
)
```

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Arguments

formula	The formula which is used to fit the model for the outcome.
data	The data.
values	A named list or data.frame specifying the variables and values at which marginal means of the outcome will be estimated.
times	A vector containing the specific values of T at which to estimate the standard- ized survival function.
measure	Either "survival" to estimate the survival function at times or "rmean" for the restricted mean survival up to the largest of times.
clusterid	An optional string containing the name of a cluster identification variable when data are clustered.
ci_level	Coverage probability of confidence intervals.
ci_type	A string, indicating the type of confidence intervals. Either "plain", which gives untransformed intervals, or "log", which gives log-transformed intervals.
contrasts	A vector of contrasts in the following format: If set to "difference" or "ratio", then $\psi(x) - \psi(x_0)$ or $\psi(x)/\psi(x_0)$ are constructed, where x_0 is a reference level specified by the reference argument. Has to be NULL if no references are specified.
family	The family argument which is used to fit the glm model for the outcome.
reference	A vector of reference levels in the following format: If contrasts is not NULL, the desired reference level(s). This must be a vector or list the same length as contrasts, and if not named, it is assumed that the order is as specified in contrasts.
transforms	A vector of transforms in the following format: If set to "log", "logit", or "odds", the standardized mean $\theta(x)$ is transformed into $\psi(x) = \log\{\theta(x)\}$, $\psi(x) = \log[\theta(x)/\{1 - \theta(x)\}]$, or $\psi(x) = \theta(x)/\{1 - \theta(x)\}$, respectively. If the vector is NULL, then $\psi(x) = \theta(x)$.

Details

standardize_coxph fits the Cox proportional hazards model

$$\lambda(t|X,Z) = \lambda_0(t) \exp\{h(X,Z;\beta)\}.$$

Breslow's estimator of the cumulative baseline hazard $\Lambda_0(t) = \int_0^t \lambda_0(u) du$ is used together with the partial likelihood estimate of β to obtain estimates of the survival function S(t|X = x, Z) if measure = "survival":

$$\hat{S}(t|X=x,Z) = \exp[-\hat{\Lambda}_0(t)\exp\{h(X=x,Z;\hat{\beta})\}].$$

For each t in the t argument and for each x in the x argument, these estimates are averaged across all subjects (i.e. all observed values of Z) to produce estimates

$$\hat{\theta}(t,x) = \sum_{i=1}^{n} \hat{S}(t|X=x, Z_i)/n,$$

where Z_i is the value of Z for subject i, i = 1, ..., n. The variance for $\hat{\theta}(t, x)$ is obtained by the sandwich formula.

If measure = "rmean", then $\Lambda_0(t) = \int_0^t \lambda_0(u) du$ is used together with the partial likelihood estimate of β to obtain estimates of the restricted mean survival up to time t: $\int_0^t S(u|X = x, Z) du$ for each element of times. The estimation and inference is done using the method described in Chen and Tsiatis 2001. Currently, we can only estimate the difference in RMST for a single binary exposure. Two separate Cox models are fit for each level of the exposure, which is expected to be coded as 0/1.

Value

An object of class std_surv. Obtain numeric results by using tidy.std_surv. This is a list with the following components:

res_contrast An unnamed list with one element for each of the requested contrasts. Each element is itself a list with the elements:

call The function call

input A list with components used in the estimation

measure Either "survival" or "rmean"

est Estimated counterfactual means and standard errors for each exposure level

vcov Estimated covariance matrix of counterfactual means for each time

est_table Data.frame of the estimates of the contrast with inference

times The vector of times used in the calculation

transform The transform argument used for this contrast

contrast The requested contrast type

reference The reference level of the exposure

ci_type Confidence interval type

ci_level Confidence interval level

res A named list with the elements:

call The function call

input A list with components used in the estimation

measure Either "survival" or "rmean"

est Estimated counterfactual means and standard errors for each exposure level

vcov Estimated covariance matrix of counterfactual means for each time

Note

Standardized survival functions are sometimes referred to as (direct) adjusted survival functions in the literature.

standardize_coxph/standardize_parfrailty does not currently handle time-varying exposures
or covariates.

standardize_coxph/standardize_parfrailty internally loops over all values in the t argument. Therefore, the function will usually be considerably faster if length(t) is small. The variance calculation performed by standardize_coxph does not condition on the observed covariates $\overline{Z} = (Z_1, ..., Z_n)$. To see how this matters, note that

$$var\{\hat{\theta}(t,x)\} = E[var\{\hat{\theta}(t,x)|\bar{Z}\}] + var[E\{\hat{\theta}(t,x)|\bar{Z}\}].$$

The usual parameter β in a Cox proportional hazards model does not depend on \overline{Z} . Thus, $E(\hat{\beta}|\overline{Z})$ is independent of \overline{Z} as well (since $E(\hat{\beta}|\overline{Z}) = \beta$), so that the term $var[E\{\hat{\beta}|\overline{Z}\}]$ in the corresponding variance decomposition for $var(\hat{\beta})$ becomes equal to 0. However, $\theta(t, x)$ depends on \overline{Z} through the average over the sample distribution for Z, and thus the term $var[E\{\hat{\theta}(t, x)|\overline{Z}\}]$ is not 0, unless one conditions on \overline{Z} . The variance calculation by Gail and Byar (1986) ignores this term, and thus effectively conditions on \overline{Z} .

Author(s)

Arvid Sjölander, Adam Brand, Michael Sachs

References

Chang I.M., Gelman G., Pagano M. (1982). Corrected group prognostic curves and summary statistics. *Journal of Chronic Diseases* **35**, 669-674.

Gail M.H. and Byar D.P. (1986). Variance calculations for direct adjusted survival curves, with applications to testing for no treatment effect. *Biometrical Journal* **28**(5), 587-599.

Makuch R.W. (1982). Adjusted survival curve estimation using covariates. *Journal of Chronic Diseases* **35**, 437-443.

Sjölander A. (2016). Regression standardization with the R-package stdReg. *European Journal of Epidemiology* **31**(6), 563-574.

Sjölander A. (2018). Estimation of causal effect measures with the R-package stdReg. *European Journal of Epidemiology* **33**(9), 847-858.

Chen, P. Y., Tsiatis, A. A. (2001). Causal inference on the difference of the restricted mean lifetime between two groups. *Biometrics*, **57**(4), 1030-1038.

```
require(survival)
set.seed(7)
n <- 300
Z <- rnorm(n)
Zbin <- rbinom(n, 1, .3)
X <- rnorm(n, mean = Z)
T <- rexp(n, rate = exp(X + Z + X * Z)) # survival time
C <- rexp(n, rate = exp(X + Z + X * Z)) # censoring time
fact <- factor(sample(letters[1:3], n, replace = TRUE))
U <- pmin(T, C) # time at risk
D <- as.numeric(T < C) # event indicator
dd <- data.frame(Z, Zbin, X, U, D, fact)
fit.std.surv <- standardize_coxph(
  formula = Surv(U, D) ~ X + Z + X * Z,
  data = dd,
```

```
values = list(X = seq(-1, 1, 0.5)),
 times = 1:5
)
print(fit.std.surv)
plot(fit.std.surv)
tidy(fit.std.surv)
fit.std <- standardize_coxph(</pre>
 formula = Surv(U, D) ~ X + Zbin + X * Zbin + fact,
 data = dd,
 values = list(Zbin = 0:1),
 times = 1.5,
 measure = "rmean",
 contrast = "difference",
 reference = 0
)
print(fit.std)
tidy(fit.std)
```

standardize_gee Regression standardization in conditional generalized estimating equations

Description

standardize_gee performs regression standardization in linear and log-linear fixed effects models, at specified values of the exposure, over the sample covariate distribution. Let Y, X, and Z be the outcome, the exposure, and a vector of covariates, respectively. It is assumed that data are clustered with a cluster indicator i. standardize_gee uses fitted fixed effects model, with cluster-specific intercept a_i (see details), to estimate the standardized mean $\theta(x) = E\{E(Y|i, X = x, Z)\}$, where x is a specific value of X, and the outer expectation is over the marginal distribution of (a_i, Z) .

Usage

```
standardize_gee(
  formula,
  link = "identity",
  data,
  values,
  clusterid,
  case_control = FALSE,
  ci_level = 0.95,
  ci_type = "plain",
  contrasts = NULL,
  family = "gaussian",
  reference = NULL,
  transforms = NULL
)
```

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Arguments

formula	A formula to be used with "gee" in the drgee package.
link	The link function to be used with "gee".
data	The data.
values	A named list or data.frame specifying the variables and values at which marginal means of the outcome will be estimated.
clusterid	An optional string containing the name of a cluster identification variable when data are clustered.
case_control	Whether the data comes from a case-control study.
ci_level	Coverage probability of confidence intervals.
ci_type	A string, indicating the type of confidence intervals. Either "plain", which gives untransformed intervals, or "log", which gives log-transformed intervals.
contrasts	A vector of contrasts in the following format: If set to "difference" or "ratio", then $\psi(x) - \psi(x_0)$ or $\psi(x)/\psi(x_0)$ are constructed, where x_0 is a reference level specified by the reference argument. Has to be NULL if no references are specified.
family	The family argument which is used to fit the glm model for the outcome.
reference	A vector of reference levels in the following format: If contrasts is not NULL, the desired reference level(s). This must be a vector or list the same length as contrasts, and if not named, it is assumed that the order is as specified in contrasts.
transforms	A vector of transforms in the following format: If set to "log", "logit", or "odds", the standardized mean $\theta(x)$ is transformed into $\psi(x) = \log\{\theta(x)\}$, $\psi(x) = \log[\theta(x)/\{1 - \theta(x)\}]$, or $\psi(x) = \theta(x)/\{1 - \theta(x)\}$, respectively. If the vector is NULL, then $\psi(x) = \theta(x)$.

Details

standardize_gee assumes that a fixed effects model

$$\eta\{E(Y|i, X, Z)\} = a_i + h(X, Z; \beta)$$

has been fitted. The link function η is assumed to be the identity link or the log link. The conditional generalized estimating equation (CGEE) estimate of β is used to obtain estimates of the cluster-specific means:

$$\hat{a}_i = \sum_{j=1}^{n_i} r_{ij} / n_i,$$

where

$$r_{ij} = Y_{ij} - h(X_{ij}, Z_{ij}; \hat{\beta})$$

if η is the identity link, and

$$r_{ij} = Y_{ij} \exp\{-h(X_{ij}, Z_{ij}; \hat{\beta})\}$$

if η is the log link, and (X_{ij}, Z_{ij}) is the value of (X, Z) for subject j in cluster $i, j = 1, ..., n_i, i = 1, ..., n$. The CGEE estimate of β and the estimate of a_i are used to estimate the mean E(Y|i, X = x, Z):

$$\hat{E}(Y|i, X = x, Z) = \eta^{-1} \{ \hat{a}_i + h(X = x, Z; \hat{\beta}) \}.$$

For each x in the x argument, these estimates are averaged across all subjects (i.e. all observed values of Z and all estimated values of a_i) to produce estimates

$$\hat{\theta}(x) = \sum_{i=1}^{n} \sum_{j=1}^{n_i} \hat{E}(Y|i, X = x, Z_i) / N,$$

where $N = \sum_{i=1}^{n} n_i$. The variance for $\hat{\theta}(x)$ is obtained by the sandwich formula.

Value

An object of class std_glm. Obtain numeric results in a data frame with the tidy.std_glm function. This is a list with the following components:

res_contrast An unnamed list with one element for each of the requested contrasts. Each element is itself a list with the elements:

estimates Estimated counterfactual means and standard errors for each exposure level

covariance Estimated covariance matrix of counterfactual means

fit_outcome The estimated regression model for the outcome

fit_exposure The estimated exposure model

exposure_names A character vector of the exposure variable names

est_table Data.frame of the estimates of the contrast with inference

transform The transform argument used for this contrast

contrast The requested contrast type

reference The reference level of the exposure

ci_type Confidence interval type

ci_level Confidence interval level

res A named list with the elements:

estimates Estimated counterfactual means and standard errors for each exposure level

covariance Estimated covariance matrix of counterfactual means

fit_outcome The estimated regression model for the outcome

fit_exposure The estimated exposure model

exposure_names A character vector of the exposure variable names

Note

The variance calculation performed by standardize_gee does not condition on the observed covariates $\overline{Z} = (Z_{11}, ..., Z_{nn_i})$. To see how this matters, note that

 $var\{\hat{\theta}(x)\} = E[var\{\hat{\theta}(x)|\bar{Z}\}] + var[E\{\hat{\theta}(x)|\bar{Z}\}].$

The usual parameter β in a generalized linear model does not depend on \overline{Z} . Thus, $E(\hat{\beta}|\overline{Z})$ is independent of \overline{Z} as well (since $E(\hat{\beta}|\overline{Z}) = \beta$), so that the term $var[E\{\hat{\beta}|\overline{Z}\}]$ in the corresponding variance decomposition for $var(\hat{\beta})$ becomes equal to 0. However, $\theta(x)$ depends on \overline{Z} through the average over the sample distribution for Z, and thus the term $var[E\{\hat{\theta}(x)|\overline{Z}\}]$ is not 0, unless one conditions on \overline{Z} .

Author(s)

Arvid Sjölander.

References

Goetgeluk S. and Vansteelandt S. (2008). Conditional generalized estimating equations for the analysis of clustered and longitudinal data. *Biometrics* **64**(3), 772-780.

Martin R.S. (2017). Estimation of average marginal effects in multiplicative unobserved effects panel models. *Economics Letters* **160**, 16-19.

Sjölander A. (2019). Estimation of marginal causal effects in the presence of confounding by cluster. *Biostatistics* doi: 10.1093/biostatistics/kxz054

Examples

```
require(drgee)
```

```
set.seed(4)
n <- 300
ni <- 2
id <- rep(1:n, each = ni)</pre>
ai <- rep(rnorm(n), each = ni)</pre>
Z <- rnorm(n * ni)</pre>
X <- rnorm(n * ni, mean = ai + Z)
Y <- rnorm(n * ni, mean = ai + X + Z + 0.1 * X^2)
dd <- data.frame(id, Z, X, Y)
fit.std <- standardize_gee(</pre>
  formula = Y \sim X + Z + I(X^2),
  link = "identity",
  data = dd,
  values = list(X = seq(-3, 3, 0.5)),
  clusterid = "id"
)
print(fit.std)
plot(fit.std)
```

standardize_glm Get regression standardized estimates from a glm

Description

Get regression standardized estimates from a glm

Usage

```
standardize_glm(
  formula,
  data,
```

```
values,
clusterid,
matched_density_cases,
matched_density_controls,
matching_variable,
p_population,
case_control = FALSE,
ci_level = 0.95,
ci_type = "plain",
contrasts = NULL,
family = "gaussian",
reference = NULL,
transforms = NULL
```

Arguments

)

formula	The formula which is used to fit the model for the outcome.	
data	The data.	
values	A named list or data.frame specifying the variables and values at which marginal means of the outcome will be estimated.	
clusterid	An optional string containing the name of a cluster identification variable when data are clustered.	
<pre>matched_density</pre>	/_cases	
	A function of the matching variable. The probability (or density) of the matched variable among the cases.	
<pre>matched_density</pre>	/_controls	
	A function of the matching variable. The probability (or density) of the matched variable among the controls.	
matching_variable		
	The matching variable extracted from the data set.	
p_population	Specifies the incidence in the population when case_control=TRUE.	
case_control	Whether the data comes from a case-control study.	
ci_level	Coverage probability of confidence intervals.	
ci_type	A string, indicating the type of confidence intervals. Either "plain", which gives untransformed intervals, or "log", which gives log-transformed intervals.	
contrasts	A vector of contrasts in the following format: If set to "difference" or "ratio", then $\psi(x) - \psi(x_0)$ or $\psi(x)/\psi(x_0)$ are constructed, where x_0 is a reference level specified by the reference argument. Has to be NULL if no references are specified.	
family	The family argument which is used to fit the glm model for the outcome.	
reference	A vector of reference levels in the following format: If contrasts is not NULL, the desired reference level(s). This must be a vector or list the same length as contrasts, and if not named, it is assumed that the order is as specified in contrasts.	

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transforms	A vector of transforms in the following format: If set to "log", "logit", or
	"odds", the standardized mean $\theta(x)$ is transformed into $\psi(x) = \log\{\theta(x)\}$,
	$\psi(x) = \log[\theta(x)/\{1 - \theta(x)\}]$, or $\psi(x) = \theta(x)/\{1 - \theta(x)\}$, respectively. If the
	vector is NULL, then $\psi(x) = \theta(x)$.

Details

standardize_glm performs regression standardization in generalized linear models, at specified values of the exposure, over the sample covariate distribution. Let Y, X, and Z be the outcome, the exposure, and a vector of covariates, respectively. standardize_glm uses a fitted generalized linear model to estimate the standardized mean $\theta(x) = E\{E(Y|X = x, Z)\}$, where x is a specific value of X, and the outer expectation is over the marginal distribution of Z.

Value

An object of class std_glm. Obtain numeric results in a data frame with the tidy.std_glm function. This is a list with the following components:

res_contrast An unnamed list with one element for each of the requested contrasts. Each element is itself a list with the elements:

estimates Estimated counterfactual means and standard errors for each exposure level **covariance** Estimated covariance matrix of counterfactual means

fit_outcome The estimated regression model for the outcome

fit_exposure The estimated exposure model

exposure_names A character vector of the exposure variable names

est_table Data.frame of the estimates of the contrast with inference

transform The transform argument used for this contrast

contrast The requested contrast type

reference The reference level of the exposure

ci_type Confidence interval type

ci_level Confidence interval level

res A named list with the elements:

estimates Estimated counterfactual means and standard errors for each exposure level **covariance** Estimated covariance matrix of counterfactual means

fit_outcome The estimated regression model for the outcome

fit_exposure The estimated exposure model

exposure_names A character vector of the exposure variable names

References

Rothman K.J., Greenland S., Lash T.L. (2008). *Modern Epidemiology*, 3rd edition. Lippincott, Williams & Wilkins.

Sjölander A. (2016). Regression standardization with the R-package stdReg. *European Journal of Epidemiology* **31**(6), 563-574.

Sjölander A. (2016). Estimation of causal effect measures with the R-package stdReg. *European Journal of Epidemiology* **33**(9), 847-858.

Examples

```
# basic example
# needs to correctly specify the outcome model and no unmeasered confounders
# (+ standard causal assumptions)
set.seed(6)
n <- 100
Z <- rnorm(n)
X <- cut(rnorm(n, mean = Z), breaks = c(-Inf, 0, Inf), labels = c("low", "high"))
Y <- rbinom(n, 1, prob = (1 + exp(as.numeric(X) + Z))^(-1))</pre>
dd <- data.frame(Z, X, Y)
x <- standardize_glm(</pre>
  formula = Y \sim X * Z,
  family = "binomial",
  data = dd,
  values = list(X = c("low", "high")),
  contrasts = c("difference", "ratio"),
  reference = "low"
)
х
# different transformations of causal effects
# example from Sjölander (2016) with case-control data
# here the matching variable needs to be passed as an argument
singapore <- AF::singapore</pre>
Mi <- singapore$Age
m <- mean(Mi)</pre>
s <- sd(Mi)
d <- 5
standardize_glm(
  formula = Oesophagealcancer ~ (Everhotbev + Age + Dial + Samsu + Cigs)^2,
  family = binomial, data = singapore,
  values = list(Everhotbev = 0:1), clusterid = "Set",
  case_control = TRUE,
  matched_density_cases = function(x) dnorm(x, m, s),
  matched_density_controls = function(x) dnorm(x, m - d, s),
  matching_variable = Mi,
  p_population = 19.3 / 100000
)
# multiple exposures
set.seed(7)
n <- 100
Z <- rnorm(n)
X1 <- rnorm(n, mean = Z)
X2 <- rnorm(n)
Y \le rbinom(n, 1, prob = (1 + exp(X1 + X2 + Z))^{(-1)})
dd <- data.frame(Z, X1, X2, Y)
x <- standardize_glm(</pre>
  formula = Y \sim X1 + X2 + Z,
  family = "binomial",
  data = dd, values = list(X1 = 0:1, X2 = 0:1),
  contrasts = c("difference", "ratio"),
```

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standardize_glm_dr

```
reference = c(X1 = 0, X2 = 0)
)
х
tidy(x)
# continuous exposure
set.seed(2)
n <- 100
Z <- rnorm(n)
X <- rnorm(n, mean = Z)
Y <- rnorm(n, mean = X + Z + 0.1 * X^2)
dd <- data.frame(Z, X, Y)
x <- standardize_glm(</pre>
  formula = Y \sim X * Z,
  family = "gaussian",
  data = dd,
  values = list(X = seq(-1, 1, 0.1))
)
# plot standardized mean as a function of x
plot(x)
# plot standardized mean - standardized mean at x = 0 as a function of x
plot(x, contrast = "difference", reference = 0)
```

standardize_glm_dr Get regression standardized doubly-robust estimates from a glm

Description

Get regression standardized doubly-robust estimates from a glm

Usage

```
standardize_glm_dr(
  formula_outcome,
  formula_exposure,
  data,
  values,
  ci_level = 0.95,
  ci_type = "plain",
  contrasts = NULL,
  family_outcome = "gaussian",
  family_exposure = "binomial",
  reference = NULL,
  transforms = NULL
)
```

Arguments

formula_outcome	e	
	The formula which is used to fit the glm model for the outcome.	
formula_exposu	re	
	The formula which is used to fit the glm model for the exposure. If not NULL, a doubly robust estimator of the standardized estimator is used.	
data	The data.	
values	A named list or data.frame specifying the variables and values at which marginal means of the outcome will be estimated.	
ci_level	Coverage probability of confidence intervals.	
ci_type	A string, indicating the type of confidence intervals. Either "plain", which gives untransformed intervals, or "log", which gives log-transformed intervals.	
contrasts	A vector of contrasts in the following format: If set to "difference" or "ratio", then $\psi(x) - \psi(x_0)$ or $\psi(x)/\psi(x_0)$ are constructed, where x_0 is a reference level specified by the reference argument. Has to be NULL if no references are specified.	
family_outcome	The family argument which is used to fit the glm model for the outcome.	
family_exposure		
	The family argument which is used to fit the glm model for the exposure.	
reference	A vector of reference levels in the following format: If contrasts is not NULL, the desired reference level(s). This must be a vector or list the same length as contrasts, and if not named, it is assumed that the order is as specified in contrasts.	
transforms	A vector of transforms in the following format: If set to "log", "logit", or "odds", the standardized mean $\theta(x)$ is transformed into $\psi(x) = \log\{\theta(x)\}$, $\psi(x) = \log[\theta(x)/\{1 - \theta(x)\}]$, or $\psi(x) = \theta(x)/\{1 - \theta(x)\}$, respectively. If the vector is NULL, then $\psi(x) = \theta(x)$.	

Details

standardize_glm_dr performs regression standardization in generalized linear models, see e.g., documentation for standardize_glm_dr. Specifically, this version uses a doubly robust estimator for standardization, meaning inference is valid when either the outcome regression or the exposure model is correctly specified and there is no unmeasured confounding.

Value

An object of class std_glm. Obtain numeric results in a data frame with the tidy.std_glm function. This is a list with the following components:

res_contrast An unnamed list with one element for each of the requested contrasts. Each element is itself a list with the elements:

estimates Estimated counterfactual means and standard errors for each exposure level

covariance Estimated covariance matrix of counterfactual means

fit_outcome The estimated regression model for the outcome

fit_exposure The estimated exposure model
exposure_names A character vector of the exposure variable names
est_table Data.frame of the estimates of the contrast with inference
transform The transform argument used for this contrast
contrast The requested contrast type
reference The reference level of the exposure
ci_type Confidence interval type
ci_level Confidence interval level

res A named list with the elements:

estimates Estimated counterfactual means and standard errors for each exposure level
covariance Estimated covariance matrix of counterfactual means
fit_outcome The estimated regression model for the outcome
fit_exposure The estimated exposure model
exposure_names A character vector of the exposure variable names

References

Gabriel E.E., Sachs, M.C., Martinussen T., Waernbaum I., Goetghebeur E., Vansteelandt S., Sjölander A. (2024), Inverse probability of treatment weighting with generalized linear outcome models for doubly robust estimation. *Statistics in Medicine*, **43**(3):534–547.

```
# doubly robust estimator
# needs to correctly specify either the outcome model or the exposure model
# for confounding
# NOTE: only works with binary exposures
data <- AF::clslowbwt</pre>
x <- standardize_glm_dr(</pre>
  formula_outcome = bwt ~ smoker * (race + age + lwt) + I(age^2) + I(lwt^2),
  formula_exposure = smoker ~ race * age * lwt + I(age^2) + I(lwt^2),
  family_outcome = "gaussian",
  family_exposure = "binomial",
  data = data,
  values = list(smoker = c(0, 1)), contrasts = "difference", reference = 0
)
set.seed(6)
n <- 100
Z <- rnorm(n)
X <- rbinom(n, 1, prob = (1 + exp(Z))^(-1))
Y <- rbinom(n, 1, prob = (1 + exp(as.numeric(X) + Z))^(-1))</pre>
dd <- data.frame(Z, X, Y)</pre>
x <- standardize_glm_dr(</pre>
  formula_outcome = Y ~ X * Z, formula_exposure = X ~ Z,
  family_outcome = "binomial",
  data = dd,
  values = list(X = 0:1), reference = 0,
  contrasts = c("difference"), transforms = c("odds")
```

)

standardize_level Get standardized estimates using the g-formula with and separate models for each exposure level in the data

Description

Get standardized estimates using the g-formula with and separate models for each exposure level in the data

Usage

```
standardize_level(
   fitter_list,
   arguments,
   predict_fun_list,
   data,
   values,
   B = NULL,
   ci_level = 0.95,
   contrasts = NULL,
   reference = NULL,
   times = NULL,
   transforms = NULL,
   progressbar = TRUE
)
```

Arguments

fitter_list	The function to call to fit the data (as a list).
arguments	The arguments to be used in the fitter function as a list.
predict_fun_li	st
	The function used to predict the means/probabilities for a new data set on the response level. For survival data, this should be a matrix where each column is the time, and each row the data (as a list).
data	The data.
values	A named list or data.frame specifying the variables and values at which marginal means of the outcome will be estimated.
В	Number of nonparametric bootstrap resamples. Default is NULL (no bootstrap).
ci_level	Coverage probability of confidence intervals.

contrasts	A vector of contrasts in the following format: If set to "difference" or "ratio", then $\psi(x) - \psi(x_0)$ or $\psi(x)/\psi(x_0)$ are constructed, where x_0 is a reference level specified by the reference argument. Has to be NULL if no references are specified.
reference	A vector of reference levels in the following format: If contrasts is not NULL, the desired reference level(s). This must be a vector or list the same length as contrasts, and if not named, it is assumed that the order is as specified in contrasts.
seed	The seed to use with the nonparametric bootstrap.
times	For use with survival data. Set to NULL otherwise.
transforms	A vector of transforms in the following format: If set to "log", "logit", or "odds", the standardized mean $\theta(x)$ is transformed into $\psi(x) = \log\{\theta(x)\}$, $\psi(x) = \log[\theta(x)/\{1 - \theta(x)\}]$, or $\psi(x) = \theta(x)/\{1 - \theta(x)\}$, respectively. If the vector is NULL, then $\psi(x) = \theta(x)$.
progressbar	Logical, if TRUE will print bootstrapping progress to the console

Details

See standardize. The difference is here that different models can be fitted for each value of x in values.

Value

An object of class std_custom. Obtain numeric results using tidy.std_custom. This is a list with the following components:

res_contrast An unnamed list with one element for each of the requested contrasts. Each element is itself a list with the elements:

B The number of bootstrap replicates

estimates Estimated counterfactual means and standard errors for each exposure level

fit_outcome The estimated regression model for the outcome

estimates_boot A list of estimates, one for each bootstrap resample

exposure_names A character vector of the exposure variable names

times The vector of times at which the calculation is done, if relevant

est_table Data.frame of the estimates of the contrast with inference

transform The transform argument used for this contrast

contrast The requested contrast type

reference The reference level of the exposure

ci_level Confidence interval level

res A named list with the elements:

B The number of bootstrap replicates

estimates Estimated counterfactual means and standard errors for each exposure level

fit_outcome The estimated regression model for the outcome

estimates_boot A list of estimates, one for each bootstrap resample

exposure_names A character vector of the exposure variable names

times The vector of times at which the calculation is done, if relevant

References

Rothman K.J., Greenland S., Lash T.L. (2008). *Modern Epidemiology*, 3rd edition. Lippincott, Williams & Wilkins.

Sjölander A. (2016). Regression standardization with the R-package stdReg. *European Journal of Epidemiology* **31**(6), 563-574.

Sjölander A. (2016). Estimation of causal effect measures with the R-package stdReg. *European Journal of Epidemiology* **33**(9), 847-858.

```
require(survival)
prob_predict.coxph <- function(object, newdata, times) {</pre>
  fit.detail <- suppressWarnings(basehaz(object))</pre>
 cum.haz <- fit.detail$hazard[sapply(times, function(x) max(which(fit.detail$time <= x)))]</pre>
  predX <- predict(object = object, newdata = newdata, type = "risk")</pre>
  res <- matrix(NA, ncol = length(times), nrow = length(predX))</pre>
  for (ti in seq_len(length(times))) {
    res[, ti] <- exp(-predX * cum.haz[ti])</pre>
  }
  res
}
set.seed(68)
n <- 500
Z <- rnorm(n)
X <- rbinom(n, 1, prob = 0.5)
T \leq rexp(n, rate = exp(X + Z + X * Z)) # survival time
C \le rexp(n, rate = exp(X + Z + X * Z)) \# censoring time
U <- pmin(T, C) # time at risk
D <- as.numeric(T < C) # event indicator</pre>
dd <- data.frame(Z, X, U, D)
x <- standardize_level(</pre>
  fitter_list = list("coxph", "coxph"),
  arguments = list(
    list(
      formula = Surv(U, D) ~ X + Z + X \star Z,
      method = "breslow",
      x = TRUE,
      y = TRUE
    ),
    list(
      formula = Surv(U, D) \sim X,
      method = "breslow",
      x = TRUE,
      y = TRUE
    )
  ),
  predict_fun_list = list(prob_predict.coxph, prob_predict.coxph),
  data = dd,
  times = seq(1, 5, 0.1),
  values = list(X = c(0, 1)),
```

standardize_parfrailty

```
B = 100,
reference = 0,
contrasts = "difference"
)
print(x)
```

standardize_parfrailty

Regression standardization in shared frailty gamma-Weibull models

Description

standardize_parfrailty performs regression standardization in shared frailty gamma-Weibull models, at specified values of the exposure, over the sample covariate distribution. Let T, X, and Z be the survival outcome, the exposure, and a vector of covariates, respectively. standardize_parfrailty fits a parametric frailty model to estimate the standardized survival function $\theta(t, x) = E\{S(t|X = x, Z)\}$, where t is a specific value of T, x is a specific value of X, and the expectation is over the marginal distribution of Z.

Usage

```
standardize_parfrailty(
  formula,
  data,
  values,
  times,
  clusterid,
  ci_level = 0.95,
  ci_type = "plain",
  contrasts = NULL,
  family = "gaussian",
  reference = NULL,
  transforms = NULL
)
```

Arguments

formula	The formula which is used to fit the model for the outcome.
data	The data.
values	A named list or data.frame specifying the variables and values at which marginal means of the outcome will be estimated.
times	A vector containing the specific values of T at which to estimate the standard- ized survival function.
clusterid	An optional string containing the name of a cluster identification variable when data are clustered.
ci_level	Coverage probability of confidence intervals.

ci_type	A string, indicating the type of confidence intervals. Either "plain", which gives untransformed intervals, or "log", which gives log-transformed intervals.
contrasts	A vector of contrasts in the following format: If set to "difference" or "ratio", then $\psi(x) - \psi(x_0)$ or $\psi(x)/\psi(x_0)$ are constructed, where x_0 is a reference level specified by the reference argument. Has to be NULL if no references are specified.
family	The family argument which is used to fit the glm model for the outcome.
reference	A vector of reference levels in the following format: If contrasts is not NULL, the desired reference level(s). This must be a vector or list the same length as contrasts, and if not named, it is assumed that the order is as specified in contrasts.
transforms	A vector of transforms in the following format: If set to "log", "logit", or "odds", the standardized mean $\theta(x)$ is transformed into $\psi(x) = \log\{\theta(x)\}$, $\psi(x) = \log[\theta(x)/\{1 - \theta(x)\}]$, or $\psi(x) = \theta(x)/\{1 - \theta(x)\}$, respectively. If the vector is NULL, then $\psi(x) = \theta(x)$.

Details

standardize_parfrailty fits a shared frailty gamma-Weibull model

$$\lambda(t_{ij}|X_{ij}, Z_{ij}) = \lambda(t_{ij}; \alpha, \eta) U_i exp\{h(X_{ij}, Z_{ij}; \beta)\}$$

, with parameterization as described in the help section for parfrailty. Integrating out the gamma frailty gives the survival function

$$S(t|X,Z) = [1 + \phi \Lambda_0(t;\alpha,\eta) \exp\{h(X,Z;\beta)\}]^{-1/\phi},$$

where $\Lambda_0(t; \alpha, \eta)$ is the cumulative baseline hazard

 $(t/\alpha)^{\eta}$.

The ML estimates of $(\alpha, \eta, \phi, \beta)$ are used to obtain estimates of the survival function S(t|X = x, Z):

$$\hat{S}(t|X=x,Z) = [1 + \hat{\phi}\Lambda_0(t;\hat{\alpha},\hat{\eta})\exp\{h(X,Z;\hat{\beta})\}]^{-1/\phi}$$

For each t in the t argument and for each x in the x argument, these estimates are averaged across all subjects (i.e. all observed values of Z) to produce estimates

$$\hat{\theta}(t,x) = \sum_{i=1}^{n} \hat{S}(t|X=x, Z_i)/n.$$

The variance for $\hat{\theta}(t, x)$ is obtained by the sandwich formula.

Value

An object of class std_surv. Obtain numeric results by using tidy.std_surv. This is a list with the following components:

res_contrast An unnamed list with one element for each of the requested contrasts. Each element is itself a list with the elements:

call The function call input A list with components used in the estimation measure Either "survival" or "rmean" est Estimated counterfactual means and standard errors for each exposure level vcov Estimated covariance matrix of counterfactual means for each time est_table Data.frame of the estimates of the contrast with inference times The vector of times used in the calculation transform The transform argument used for this contrast contrast The requested contrast type reference The reference level of the exposure ci_type Confidence interval type ci_level Confidence interval level

res A named list with the elements:

call The function call
input A list with components used in the estimation
measure Either "survival" or "rmean"
est Estimated counterfactual means and standard errors for each exposure level
vcov Estimated covariance matrix of counterfactual means for each time

Note

Standardized survival functions are sometimes referred to as (direct) adjusted survival functions in the literature.

standardize_coxph/standardize_parfrailty does not currently handle time-varying exposures or covariates.

standardize_coxph/standardize_parfrailty internally loops over all values in the t argument. Therefore, the function will usually be considerably faster if length(t) is small.

The variance calculation performed by standardize_coxph does not condition on the observed covariates $\overline{Z} = (Z_1, ..., Z_n)$. To see how this matters, note that

$$var\{\hat{\theta}(t,x)\} = E[var\{\hat{\theta}(t,x)|\bar{Z}\}] + var[E\{\hat{\theta}(t,x)|\bar{Z}\}].$$

The usual parameter β in a Cox proportional hazards model does not depend on \overline{Z} . Thus, $E(\hat{\beta}|\overline{Z})$ is independent of \overline{Z} as well (since $E(\hat{\beta}|\overline{Z}) = \beta$), so that the term $var[E\{\hat{\beta}|\overline{Z}\}]$ in the corresponding variance decomposition for $var(\hat{\beta})$ becomes equal to 0. However, $\theta(t, x)$ depends on \overline{Z} through the average over the sample distribution for Z, and thus the term $var[E\{\hat{\theta}(t, x)|\overline{Z}\}]$ is not 0, unless one conditions on \overline{Z} . The variance calculation by Gail and Byar (1986) ignores this term, and thus effectively conditions on \overline{Z} .

Author(s)

Arvid Sjölander

References

Chang I.M., Gelman G., Pagano M. (1982). Corrected group prognostic curves and summary statistics. *Journal of Chronic Diseases* **35**, 669-674.

Dahlqwist E., Pawitan Y., Sjölander A. (2019). Regression standardization and attributable fraction estimation with between-within frailty models for clustered survival data. *Statistical Methods in Medical Research* **28**(2), 462-485.

Gail M.H. and Byar D.P. (1986). Variance calculations for direct adjusted survival curves, with applications to testing for no treatment effect. *Biometrical Journal* **28**(5), 587-599.

Makuch R.W. (1982). Adjusted survival curve estimation using covariates. *Journal of Chronic Diseases* **35**, 437-443.

Examples

```
require(survival)
# simulate data
set.seed(6)
n <- 300
m <- 3
alpha <- 1.5
eta <- 1
phi <- 0.5
beta <- 1
id <- rep(1:n, each = m)
U \le rep(rgamma(n, shape = 1 / phi, scale = phi), each = m)
X <- rnorm(n * m)
# reparameterize scale as in rweibull function
weibull.scale <- alpha / (U * exp(beta * X))^(1 / eta)</pre>
T <- rweibull(n * m, shape = eta, scale = weibull.scale)</pre>
# right censoring
C <- runif(n * m, 0, 10)
D <- as.numeric(T < C)</pre>
T <- pmin(T, C)
# strong left-truncation
L <- runif(n * m, 0, 2)
incl <- T > L
incl <- ave(x = incl, id, FUN = sum) == m</pre>
dd <- data.frame(L, T, D, X, id)
dd <- dd[incl, ]</pre>
fit.std <- standardize_parfrailty(</pre>
  formula = Surv(L, T, D) \sim X,
  data = dd,
  values = list(X = seq(-1, 1, 0.5)),
  times = 1:5,
  clusterid = "id"
```

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```
)
print(fit.std)
plot(fit.std)
```

summary.parfrailty Summarizes parfrailty fit

Description

This is a summary method for class "parfrailty".

Usage

```
## S3 method for class 'parfrailty'
summary(
   object,
   ci_type = "plain",
   ci_level = 0.95,
   digits = max(3L, getOption("digits") - 3L),
   ...
)
```

Arguments

object	an object of class "parfrailty".
ci_type	string, indicating the type of confidence intervals. Either "plain", which gives untransformed intervals, or "log", which gives log-transformed intervals.
ci_level	desired coverage probability of confidence intervals, in decimal form.
digits	the number of significant digits to use when printing
	not used.

Value

An object of class "summary.parfrailty", which is a list that contains relevant summary statistics about the fitted model

Author(s)

Arvid Sjölander and Elisabeth Dahlqwist.

See Also

parfrailty

Examples

See documentation for parfrailty

tidy.std_custom

Description

Tidy summarizes information about the components of the standardized regression fit.

Usage

S3 method for class 'std_custom'
tidy(x, ...)

Arguments

Х	An object of class std_custom
	Not currently used

Value

A data.frame

```
set.seed(6)
n <- 100
Z <- rnorm(n)
X <- rnorm(n, mean = Z)
Y \le rbinom(n, 1, prob = (1 + exp(X + Z))^{(-1)})
dd <- data.frame(Z, X, Y)
prob_predict.glm <- function(...) predict.glm(..., type = "response")</pre>
x <- standardize(</pre>
  fitter = "glm",
  arguments = list(
    formula = Y \sim X * Z,
    family = "binomial"
  ),
  predict_fun = prob_predict.glm,
  data = dd,
  values = list(X = seq(-1, 1, 0.1)),
  B = 100,
  reference = 0,
  contrasts = "difference"
)
tidy(x)
```

tidy.std_glm

Description

Tidy summarizes information about the components of the standardized regression fit.

Usage

S3 method for class 'std_glm'
tidy(x, ...)

Arguments

х	An object of class std_glm
	Not currently used

Value

A data.frame

```
set.seed(6)
n <- 100
Z <- rnorm(n)
X <- rnorm(n, mean = Z)
Y <- rbinom(n, 1, prob = (1 + exp(X + Z))^(-1))
dd <- data.frame(Z, X, Y)
x <- standardize_glm(
   formula = Y ~ X * Z,
   family = "binomial",
   data = dd,
   values = list(X = 0:1),
   contrasts = c("difference", "ratio"),
   reference = 0
)
tidy(x)</pre>
```

tidy.std_surv

Description

Tidy summarizes information about the components of the standardized model fit.

Usage

S3 method for class 'std_surv'
tidy(x, ...)

Arguments

х	An object of class std_surv
	Not currently used

Value

A data.frame

```
require(survival)
set.seed(8)
n <- 300
Z <- rnorm(n)
X <- rnorm(n, mean = Z)
time <- rexp(n, rate = exp(X + Z + X * Z)) # survival time
C <- rexp(n, rate = exp(X + Z + X * Z)) # censoring time
U <- pmin(time, C) # time at risk
D <- as.numeric(time < C) # event indicator
dd <- data.frame(Z, X, U, D)
x <- standardize_coxph(
   formula = Surv(U, D) ~ X + Z + X * Z,
   data = dd, values = list(X = seq(-1, 1, 0.5)), times = c(2,3,4)
)</pre>
```

```
tidy(x)
```

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