# Package 'remaCor'

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Type Package

Title Random Effects Meta-Analysis for Correlated Test Statistics

**Version** 0.0.18

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**Description** Meta-analysis is widely used to summarize estimated effects sizes across multiple statistical tests. Standard fixed and random effect meta-analysis methods assume that the estimated of the effect sizes are statistically independent. Here we relax this assumption and enable meta-analysis when the correlation matrix between effect size estimates is known. Fixed effect meta-analysis uses the method of Lin and Sullivan (2009) <doi:10.1016/j.ajhg.2009.11.001>, and random effects meta-analysis uses the method of Han, et al. <doi:10.1093/hmg/ddw049>.

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URL https://diseaseneurogenomics.github.io/remaCor/

BugReports https://github.com/DiseaseNeurogenomics/remaCor/issues

Suggests knitr, RUnit, clusterGeneration, metafor

**Depends** R (>= 3.6.0), ggplot2, methods

Imports mvtnorm, grid, reshape2, compiler, Rcpp, EnvStats, Rdpack,

stats

VignetteBuilder knitr

RdMacros Rdpack

**Encoding** UTF-8

RoxygenNote 7.2.3

LinkingTo Rcpp, RcppArmadillo

NeedsCompilation yes

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**Repository** CRAN

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```
hotelling
```

Hottelling T^2 test for multivariate regression

# Description

Hottelling T^2 test compares estimated regression coefficients to specified values under the null. This tests a global hypothesis for all specified coefficients. It uses the F-distribution as the null for the test statistic which is exact under finite sample size.

#### Usage

hotelling(beta, Sigma, n, mu\_null = rep(0, length(beta)))

# Arguments

beta	regressioin coefficients
Sigma	covariance matrix of regression coefficients
n	sample size used for estimation
mu_null	the values of the regression coefficients under the null hypothesis. Defaults to all zeros

# Details

The Hotelling T2 test is not defined when n - p < 1. Returns data.frame with stat = pvalue = NA.

```
library(clusterGeneration)
library(mvtnorm)
# sample size
n = 30
# number of response variables
m = 2
# Error covariance
```

```
Sigma = genPositiveDefMat(m)$Sigma
# regression parameters
beta = matrix(.6, 1, m)
# covariates
X = matrix(rnorm(n), ncol=1)
# Simulate response variables
Y = X %*% beta + rmvnorm(n, sigma = Sigma)
# Multivariate regression
fit = lm(Y ~ X)
# extract coefficients and covariance
# corresponding to the x variable
beta = coef(fit)['X',]
S = vcov(fit)[c(2,4), c(2,4)]
# perform Hotelling test
hotelling(beta, S, n)
```

# LS

# Fixed effect meta-analysis for correlated test statistics

#### Description

Fixed effect meta-analysis for correlated test statistics using the Lin-Sullivan method.

#### Usage

```
LS(beta, stders, cor = diag(1, length(beta)))
```

# Arguments

beta	regression coefficients from each analysis
stders	standard errors corresponding to betas
cor	correlation matrix between of test statistics. Default considers uncorrelated test statistics

#### Details

Perform fixed effect meta-analysis for correlated test statistics using method of Lin and Sullivan (2009). By default, correlation is set to identity matrix to for independent test statistics.

This method requires the correlation matrix to be symmatric positive definite (SPD). If this condition is not satisfied, results will be NA. If the matrix is not SPD, there is likely an issue with how it was generated.

#### LS

However, evaluating the correlation between observations that are not pairwise complete can give correlation matrices that are not SPD. In this case, consider running Matrix::nearPD(x, corr=TRUE) to produce the nearest SPD matrix to the input.

#### Value

- beta: effect size
- se: effect size standard error

**p:** p-value

#### References

Lin D, Sullivan PF (2009). "Meta-analysis of genome-wide association studies with overlapping subjects." *The American Journal of Human Genetics*, **85**(6), 862–872. https://doi.org/10. 1016/j.ajhg.2009.11.001.

```
library(clusterGeneration)
library(mvtnorm)
# sample size
n = 30
# number of response variables
m = 6
# Error covariance
Sigma = genPositiveDefMat(m)$Sigma
# regression parameters
beta = matrix(.6, 1, m)
# covariates
X = matrix(rnorm(n), ncol=1)
# Simulate response variables
Y = X %*% beta + rmvnorm(n, sigma = Sigma)
# Multivariate regression
fit = lm(Y \sim X)
# Correlation between residuals
C = cor(residuals(fit))
# Extract effect sizes and standard errors from model fit
df = lapply(coef(summary(fit)), function(a)
data.frame(beta = a["X", 1], se = a["X", 2]))
df = do.call(rbind, df)
# Run fixed effects meta-analysis,
```

# LS.empirical

```
# assume identity correlation
LS( df$beta, df$se)
# Run fixed effects meta-analysis,
# account for correlation
LS( df$beta, df$se, C)
```

LS.empirical

Fixed effect meta-analysis for correlated test statistics

#### Description

Fixed effect meta-analysis for correlated test statistics using the Lin-Sullivan method using Monte Carlo draws from the null distribution to compute the p-value.

#### Usage

```
LS.empirical(
   beta,
   stders,
   cor = diag(1, length(beta)),
   nu,
   n.mc.samples = 10000,
   seed = 1
)
```

#### Arguments

beta	regression coefficients from each analysis
stders	standard errors corresponding to betas
cor	correlation matrix between of test statistics. Default considers uncorrelated test statistics
nu	degrees of freedom
n.mc.samples	number of Monte Carlo samples
seed	random seed so results are reproducable

#### Details

The theoretical null for the Lin-Sullivan statistic for fixed effects meta-analysis is chisq when the regression coefficients are estimated from a large sample size. But for finite sample size, this null distribution is not well characterized. In this case, we are not aware of a closed from cumulative distribution function. Instead we draw covariance matrices from a Wishart distribution, sample coefficients from a multivariate normal with this covariance, and then compute the Lin-Sullivan statistic. A gamma distribution is then fit to these draws from the null distribution and a p-value is computed from the cumulative distribution of this gamma.

pkg.env

#### See Also

LS()

# Examples

```
library(clusterGeneration)
library(mvtnorm)
# sample size
n = 30
# number of response variables
m = 6
# Error covariance
Sigma = genPositiveDefMat(m)$Sigma
# regression parameters
beta = matrix(.6, 1, m)
# covariates
X = matrix(rnorm(n), ncol=1)
# Simulate response variables
Y = X %*% beta + rmvnorm(n, sigma = Sigma)
# Multivariate regression
fit = lm(Y \sim X)
# Correlation between residuals
C = cor(residuals(fit))
# Extract effect sizes and standard errors from model fit
df = lapply(coef(summary(fit)), function(a)
data.frame(beta = a["X", 1], se = a["X", 2]))
df = do.call(rbind, df)
# Meta-analysis assuming infinite sample size
# but the p-value is anti-conservative
LS(df$beta, df$se, C)
# Meta-analysis explicitly modeling the finite sample size
# Gives properly calibrated p-values
# nu is the residual degrees of freedom from the model fit
LS.empirical(df$beta, df$se, C, nu=n-2)
```

pkg.env

# plotCor

# Description

Local environment

#### Usage

pkg.env

# Format

An object of class environment of length 0.

plotCor

Correlation plot

# Description

Correlation plot

# Usage

plotCor(cor)

#### Arguments

cor

correlation matrix between of test statistics. Default considers uncorrelated test statistics

#### Value

Plot of correlation matrix

```
# Generate effects
library(mvtnorm)
library(clusterGeneration )
n = 4
Sigma = cov2cor(genPositiveDefMat(n)$Sigma)
beta = t(rmvnorm(1, rep(0, n), Sigma))
stders = rep(.1, n)
# set names
rownames(Sigma) = colnames(Sigma) = LETTERS[1:n]
rownames(beta) = names(stders) = LETTERS[1:n]
# Run random effects meta-analysis,
```

```
# account for correlation
RE2C( beta, stders, Sigma)
```

```
# Make plot
plotCor( Sigma )
```

plotForest

# Forest plot of coefficients

# Description

Forest plot of coefficients

# Usage

plotForest(beta, stders)

# Arguments

beta	regression coefficients from each analysis
stders	standard errors corresponding to betas

#### Value

Forest plot of effect sizes and standard errors

```
# Generate effects
library(mvtnorm)
library(clusterGeneration )
n = 4
Sigma = cov2cor(genPositiveDefMat(n)$Sigma)
beta = t(rmvnorm(1, rep(0, n), Sigma))
stders = rep(.1, n)
# set names
rownames(Sigma) = colnames(Sigma) = LETTERS[1:n]
rownames(beta) = names(stders) = LETTERS[1:n]
# Run random effects meta-analysis,
# account for correlation
RE2C( beta, stders, Sigma)
# Make plot
plotForest( beta, stders )
```

#### Description

Random effect meta-analysis for correlated test statistics using RE2C

# Usage

```
RE2C(beta, stders, cor = diag(1, length(beta)), twoStep = FALSE)
```

#### Arguments

beta	regression coefficients from each analysis
stders	standard errors corresponding to betas
cor	correlation matrix between of test statistics. Default considers uncorrelated test statistics
twoStep	Apply two step version of RE2C that is designed to be applied only after the fixed effect model.

#### Details

Perform random effect meta-analysis for correlated test statistics using RE2 method of Han and Eskin (2011), or RE2 for correlated test statistics from Han, et al., (2016). Also uses RE2C method of Lee, Eskin and Han (2017) to further test for heterogenity in effect size. By default, correlation is set to identity matrix to for independent test statistics.

This method requires the correlation matrix to be symmatric positive definite (SPD). If this condition is not satisfied, results will be NA. If the matrix is not SPD, there is likely an issue with how it was generated.

However, evaluating the correlation between observations that are not pairwise complete can give correlation matricies that are not SPD. In this case, consider running Matrix::nearPD(x, corr=TRUE) to produce the nearest SPD matrix to the input.

#### Value

**stat1:** statistic testing effect mean

stat2: statistic testing effect heterogeneity

RE2Cp: RE2 p-value accounting for correlelation between tests

**RE2Cp.twoStep:** two step RE2C test after fixed effect test. Only evaluated if twoStep==TRUE

QE: test statistic for the test of (residual) heterogeneity

QEp: p-value for the test of (residual) heterogeneity

Isq: I^2 statistic

QE, QEp and ISq are only evaluted if correlation is diagonal

#### References

Lee CH, Eskin E, Han B (2017). "Increasing the power of meta-analysis of genome-wide association studies to detect heterogeneous effects." *Bioinformatics*, **33**(14), i379–i388. https://doi.org/10.1093/bioinformatics/btx242.

Han B, Duong D, Sul JH, de Bakker PI, Eskin E, Raychaudhuri S (2016). "A general framework for meta-analyzing dependent studies with overlapping subjects in association mapping." *Human Molecular Genetics*, **25**(9), 1857–1866. https://doi.org/10.1093/hmg/ddw049.

Han B, Eskin E (2011). "Random-effects model aimed at discovering associations in meta-analysis of genome-wide association studies." *The American Journal of Human Genetics*, **88**(5), 586–598. https://doi.org/10.1016/j.ajhg.2011.04.014.

```
library(clusterGeneration)
library(mvtnorm)
# sample size
n = 30
# number of response variables
m = 6
# Error covariance
Sigma = genPositiveDefMat(m)$Sigma
# regression parameters
beta = matrix(.6, 1, m)
# covariates
X = matrix(rnorm(n), ncol=1)
# Simulate response variables
Y = X %*% beta + rmvnorm(n, sigma = Sigma)
# Multivariate regression
fit = lm(Y \sim X)
# Correlation between residuals
C = cor(residuals(fit))
# Extract effect sizes and standard errors from model fit
df = lapply(coef(summary(fit)), function(a)
data.frame(beta = a["X", 1], se = a["X", 2]))
df = do.call(rbind, df)
# Run fixed effects meta-analysis,
# assume identity correlation
LS( df$beta, df$se)
# Run random effects meta-analysis,
```

# RE2C

RE2C( df\$beta, df\$se)
# Run fixed effects meta-analysis,
# account for correlation
LS( df\$beta, df\$se, C)

# Run random effects meta-analysis, # account for correlation RE2C( df\$beta, df\$se, C)

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