# Package 'piecewiseSEM'

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Type Package

Title Piecewise Structural Equation Modeling

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**Description** Implements piecewise structural equation modeling from a single list of structural equations, with new methods for non-linear, latent, and composite variables, standardized coefficients, query-based prediction and indirect effects. See <a href="http://jslefche.github.io/piecewiseSEM/">http://jslefche.github.io/piecewiseSEM/</a>> for more.

**Depends** R (>= 4.4.0)

URL https://github.com/jslefche/

BugReports https://github.com/jslefche/piecewiseSEM/issues

**Imports** car, DiagrammeR, emmeans, igraph, lme4, multcomp, MuMIn, MASS, methods, nlme, performance

License GPL-3

Encoding UTF-8

LazyData true

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Suggests knitr, rmarkdown

VignetteBuilder knitr

NeedsCompilation no

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piecewiseSEM-package The 'piecewiseSEM' package

## Description

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Piecewise structural equation modeling

Fitting and evaluation of piecewise structural equation models, complete with goodness-of-fit tests, estimates of (standardized) path coefficients, and evaluation of individual model fits (e.g., through R-squared values). Compared with traditional variance-covariance based SEM, piecewise SEM

#### piecewiseSEM-package

allows for fitting of models to different distributions through GLM and/or hierarchical/nested random structures through (G)LMER. Supported model classes include: lm, glm, gls, Sarlm, lme, glmmPQL, lmerMod, merModLmerTest,glmerMod, glmmTMB, gam.

Package:	piecewiseSEM
Type:	Package
Version:	2.3.0.1
Date:	2024-06-11
Depends:	R (>= 4.4.0), car, DiagrammeR, emmeans, igraph, lme4, multcomp, MuMIn, MASS, methods, nlme
License:	MIT

The primary functions in the package are psem which unites structural equations in a single model, and summary.psem can be used on an object of class psem to provide various summary statistics for evaluation and interpretation.

#### Author(s)

Jon Lefcheck <jslefche@gmail.com>

#### References

Shipley, Bill. "A new inferential test for path models based on directed acyclic graphs." Structural Equation Modeling 7.2 (2000): 206-218.

Shipley, Bill. Cause and correlation in biology: a user's guide to path analysis, structural equations and causal inference. Cambridge University Press, 2002.

Shipley, Bill. "Confirmatory path analysis in a generalized multilevel context." Ecology 90.2 (2009): 363-368.

Shipley, Bill. "The AIC model selection method applied to path analytic models compared using a d-separation test." Ecology 94.3 (2013): 560-564.

Shipley, Bill, and Jacob C. Douma. "Generalized AIC and chi-squared statistics for path models consistent with directed acyclic graphs." Ecology 101.3 (2020): e02960.

Grace, J.B., Johnson, D.A., Lefcheck, J.S., and Byrnes, J.E. "Standardized Coefficients in Regression and Structural Models with Binary Outcomes." Ecosphere 9(6): e02283.

Nakagawa, Shinichi, Paul CD Johnson, and Holger Schielzeth. "The coefficient of determination R2 and intra-class correlation coefficient from generalized linear mixed-effects models revisited and expanded." Journal of the Royal Society Interface 14.134 (2017): 20170213.

## See Also

Useful links:

- https://github.com/jslefche/
- Report bugs at https://github.com/jslefche/piecewiseSEM/issues

AIC.psem

## Description

Generic function for SEM AIC(c) score

## Usage

```
## S3 method for class 'psem'
AIC(object, ..., AIC.type = "loglik", aicc = FALSE)
```

## Arguments

object	a psem object
	additional arguments to AIC
AIC.type	whether the log-likelihood "loglik" or d-sep "dsep" AIC score should be reported. Default is "loglik"
aicc	whether correction for small sample size should be applied. Default is FALSE

## Examples

```
mod <- psem(
lm(rich ~ cover, data = keeley),
lm(cover ~ firesev, data = keeley),
lm(firesev ~ age, data = keeley),
data = keeley
)
# Get log-likelihood based AIC
AIC(mod)
# Get d-sep based AIC
AIC(mod, AIC.type = "dsep")
```

AIC\_psem

Information criterion values for SEM

## Description

Information criterion values for SEM

## AIC\_psem

## Usage

```
AIC_psem(
  modelList,
  AIC.type = "loglik",
  Cstat = NULL,
  add.claims = NULL,
  basis.set = NULL,
  direction = NULL,
  interactions = FALSE,
  conserve = FALSE,
  conditional = FALSE,
  .progressBar = FALSE
)
```

## Arguments

modelList	a list of structural equations
AIC.type	whether the log-likelihood "loglik" or d-sep "dsep" AIC score should be reported. Default is "loglik"
Cstat	Fisher's C statistic obtained from fisherC
add.claims	an optional vector of additional independence claims (P-values) to be added to the basis set
basis.set	An optional list of independence claims.
direction	a vector of claims defining the specific directionality of any independence claim(s)
interactions	whether interactions should be included in independence claims. Default is FALSE
conserve	whether the most conservative P-value should be returned (See Details) Default is FALSE
conditional	whether the conditioning variables should be shown in the table. Default is FALSE
.progressBar	an optional progress bar. Default is FALSE

#### Value

a data.frame of AIC, AICc, d.f., and sample size

#### Author(s)

Jon Lefcheck <LefcheckJ@si.edu>, Jim Grace

#### References

Shipley, Bill, and Jacob C. Douma. "Generalized AIC and chi-squared statistics for path models consistent with directed acyclic graphs." Ecology 101.3 (2020): e02960.

Shipley, Bill. "The AIC model selection method applied to path analytic models compared using a d-separation test." Ecology 94.3 (2013): 560-564.

anova.psem

#### Description

Compute analysis of variance table for one or more structural equation models.

#### Usage

```
## S3 method for class 'psem'
anova(object, ..., digits = 3, anovafun = "Anova")
```

## Arguments

object	a psem object
	additional objects of the same type
digits	number of digits to round results. Default is 3
anovafun	The function used for ANOVA. Defaults to Anova

## Details

Additional models will be tested against the first model using a Chi-squared difference test.

#### Value

an F, LRT, or other table for a single model, or a list of comparisons between multiple models

#### Author(s)

Jon Lefcheck <lefcheckj@si.edu>, Jarrett Byrnes <jarrett.byrnes@umb.edu>

#### See Also

Anova

## Examples

```
data(keeley)
```

```
mod1 <- psem(
lm(rich ~ cover, data = keeley),
lm(cover ~ firesev, data = keeley),
lm(firesev ~ age, data = keeley),
data = keeley
)
# get type II Anova
anova(mod1)
```

## as.psem

```
# conduct LRT
mod2 <- psem(
    lm(rich ~ cover, data = keeley),
    lm(cover ~ firesev, data = keeley),
    age ~ 1,
    data = keeley
)
anova(mod1, mod2)</pre>
```

as.psem

#### Convert list to psem object

## Description

Convert list to psem object

## Usage

as.psem(object, Class = "psem")

## Arguments

object	any R object
Class	the name of the class to which object should be coerced

basisSet

Derivation of the basis set

## Description

Acquires the set of independence claims-or the 'basis set'-for use in evaluating the goodness-of-fit for piecewise structural equation models.

#### Usage

```
basisSet(modelList, direction = NULL, interactions = FALSE)
```

modelList	A list of structural equations
direction	a vector of claims defining the specific directionality of any independence claim(s) $% \left( \frac{1}{2} \right) = \left( \frac{1}{2} \right) \left( \frac{1}{2$
interactions	whether interactions should be included in independence claims. Default is FALSE

#### Details

This function returns a list of independence claims. Each claim is a vector of the predictor of interest, followed by the response, and, if present, any conditioning variables.

Relationships among exogenous variables are omitted from the basis set because the directionality is unclear–e.g., does temperature cause latitude or does latitude cause temperature?–and the assumptions of the variables are not specified in the list of structural equations, so evaluating the relationship becomes challenging without further input from the user. This creates a circular scenario whereby the user specifies relationships among exogenous variables, raising the issue of whether they should be included as directed paths if they can be assigned directional relationships.

Paths can be omitted from the basis set by specifying them as correlated errors using  $%\sim~\%$  or by assigning a directionality using the argument direction, e.g. direction = c("X <- Y"). This can be done if post hoc examination of the d-sep tests reveals nonsensical independence claims (e.g., arthropod abundance predicting photosynthetically-active radiation) that the user may wish to exclude from evaluation.

#### Value

A list of independence claims.

#### Author(s)

Jon Lefcheck <LefcheckJ@si.edu>

#### References

Shipley, Bill. "A new inferential test for path models based on directed acyclic graphs." Structural Equation Modeling 7.2 (2000): 206-218.

#### See Also

dSep

cbind\_fill Bind data.frames of differing dimensions

#### Description

From: https://stackoverflow.com/a/31678079

#### Usage

cbind\_fill(...)

#### Arguments

. . .

data.frames to be bound, separated by commas @keywords internal cerror

#### Description

Calculates partial correlations and partial significance tests.

#### Usage

```
cerror(formula., modelList, data = NULL)
```

## Arguments

formula.	A formula specifying the two correlated variables using %~~%.
modelList	A list of structural equations.
data	A data.frame containing the data used in the list of equations.

#### Details

If the variables are exogenous, then the correlated error is the raw bivariate correlation.

If the variables are endogenous, then the correlated error is the partial correlation, accounting for the influence of any predictors.

The significance of the correlated error is conducted using cor.test if the variables are exogenous. Otherwise, a t-statistic is constructed and compared to a t-distribution with N - k - 2 degrees of freedom (where N is the total number of replicates, and k is the total number of variables informing the relationship) to derive a P-value.

## Value

Returns a data. frame containing the (partial) correlation and associated significance test.

## Author(s)

Jon Lefcheck <lefcheckj@si.edu>

## See Also

%~~%

#### Examples

```
# Generate example data
dat <- data.frame(x1 = runif(50),
x2 = runif(50), y1 = runif(50),
y2 = runif(50))</pre>
```

# Create list of structural equations

```
sem <- psem(</pre>
  lm(y1 \sim x1 + x2, dat),
  lm(y2 \sim y1 + x1, dat)
)
# Look at correlated error between x1 and x2
# (exogenous)
cerror(x1 %~~% x2, sem, dat)
# Same as cor.test
with(dat, cor.test(x1, x2))
# Look at correlatde error between x1 and y1
# (endogenous)
cerror(y1 %~~% x1, sem, dat)
# Not the same as cor.test
# (accounts for influence of x1 and x2 on y1)
with(dat, cor.test(y1, x1))
# Specify in psem
sem <- update(sem, x1 %~~% y1)</pre>
coefs(sem)
```

coefs

#### Extract path coefficients

#### Description

Extracts (standardized) path coefficients from a psem object.

## Usage

```
coefs(
  modelList,
  standardize = "scale",
  standardize.type = "latent.linear",
  test.statistic = "F",
  test.type = "II",
  intercepts = FALSE
)
```

#### Arguments

modelList	A list of structural equations, or a model.
standardize	The type of standardization: none, scale, range. Default is scale.

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coefs

standardize.typ	be	
	The type of standardized for non-Gaussian responses: latent.linear, Menarce Default is latent.linear for binomial; otherwise it is Menard.OE.	
test.statistic	the type of test statistic generated by Anova	
test.type	the type of test for significance of categorical variables from Anova. Default is type "II".	
intercepts	Whether intercepts should be included in the coefficients table. Default is FALSE.	

#### Details

P-values for models constructed using 1me4 are obtained using the Kenward-Roger approximation of the denominator degrees of freedom as implemented in the Anova function.

Different forms of standardization can be implemented using the standardize argument:

- · none No standardized coefficients are reported.
- scale Raw coefficients are scaled by the ratio of the standard deviation of x divided by the standard deviation of y. See below for cases pertaining to GLM.
- range Raw coefficients are scaled by a pre-selected range of x divided by a preselected range of y. The default argument is range which takes the two extremes of the data, otherwise the user must supply must a named list where the names are the variables to be standardized, and each entry contains a vector of length == 2 to the ranges to be used in standardization.

For non-Gaussian responses, standardized coefficients are obtained in one of two ways:

- latent.linear Referred to in Grace et al. 2019 as the standard form of the latent-theoretic (LT) approach. In this method, there is assumed to be a continuous latent propensity, y\*, that underlies the observed binary responses. The standard deviation of y\* is computed as the square-root of the variance of the predictions (on the linear or 'link' scale) plus the distribution-specific theoretical variance in the case of binomial responses (for logit links: pi^2/3, for probit links: 1).
- Menard.OE Referred to in Grace et al. 2019 as the standard form of the observed-empirical (OE) approach. In this method, error variance is based on the differences between predicted scores and the observed binary data. The standard deviation used for standardization is computed as the square-root of the variance of the predictions (on the linear scale) plus the correlation between the observed and predicted (on the original or 'response' scale) values of y.

For categorical predictors: significance is determined using ANOVA (or analysis of deviance). Because n-1 coefficients are reported for n levels, the output instead reports model-estimated means in the Estimate column. This is done so all n paths in the corresponding path diagram have assignable values.

The means are generated using function emmeans in the emmeans package. Pairwise contrasts are further conducted among all levels using the default correction for multiple testing. The results of those comparisons are given in the significance codes (e.g., "a", "b", "ab") as reported in the multcomp::cld function.

For non-linear variables (i.e., smoothing functions from mgcv::gam), there are no linear estimates reported.

## Value

Returns a data.frame of coefficients, their standard errors, degrees of freedom, and significance tests.

#### Author(s)

Jon Lefcheck <LefcheckJ@si.edu>, Jim Grace

## References

Grace, J.B., Johnson, D.A., Lefcheck, J.S., and Byrnes, J.E. "Standardized Coefficients in Regression and Structural Models with Binary Outcomes." Ecosphere 9(6): e02283.

#### See Also

Anova, emmeans, cld

#### Examples

```
mod <- psem(
lm(rich ~ cover, data = keeley),
lm(cover ~ firesev, data = keeley),
lm(firesev ~ age, data = keeley),
data = keeley
)</pre>
```

coefs(mod)

dSep

Tests of directed separation

## Description

Evaluation of conditional independence claims to be used in determining the goodness-of-fit for piecewise structural equation models.

#### Usage

```
dSep(
   modelList,
   basis.set = NULL,
   direction = NULL,
   interactions = FALSE,
   conserve = FALSE,
   conditioning = FALSE,
   .progressBar = TRUE
)
```

## dSep

#### Arguments

modelList	A list of structural equations created using psem.
basis.set	An optional list of independence claims.
direction	A vector of claims defining the specific directionality of independence claims; for use in special cases (see Details).
interactions	whether interactions should be included in independence claims. Default is FALSE
conserve	Whether the most conservative P-value should be returned; for use in special cases (see Details). Default is FALSE.
conditioning	Whether the conditioning variables should be shown in the summary table. Default is FALSE.
.progressBar	An optional progress bar. Default is TRUE.

#### Details

In cases involving non-normally distributed responses in the independence claims that are modeled using generalized linear models, the significance of the independence claim is not reversible (e.g., the P-value of Y ~ X is not the same as X ~ Y). This is due to the transformation of the response via the link function. In extreme cases, this can bias the goodness-of-fit tests. summary.psem will issue a warning when this case is present and provide guidance for solutions.

One solution is to specify the directionality of the relationship using the direction argument, e.g. direction = c("X <- Y"). Another is to run both tests (Y ~ X, X ~ Y) and return the most conservative (i.e., lowest) P-value, which can be toggled using the conserve = TRUE argument.

## Value

Returns a data. frame of independence claims and their significance values.

#### Author(s)

Jon Lefcheck <lefcheckj@si.edu>, Jarrett Byrnes

#### References

Shipley, Bill. "A new inferential test for path models based on directed acyclic graphs." Structural Equation Modeling 7.2 (2000): 206-218.

#### See Also

basisSet

evaluateClasses

## Description

Evaluate model classes and stop if unsupported model class

#### Usage

```
evaluateClasses(x)
```

## Arguments

х

a list of structural equations or a model object

fisherC

Summarize tests of directed separation using Fisher's C statistic

## Description

Summarize tests of directed separation using Fisher's C statistic

## Usage

```
fisherC(
   dTable,
   add.claims = NULL,
   basis.set = NULL,
   direction = NULL,
   interactions = FALSE,
   conserve = FALSE,
   conditional = FALSE,
   .progressBar = FALSE
)
```

dTable	a data.frame containing tests of directed separation from dSep
add.claims	an optional vector of additional independence claims (i.e., P-values) to be added to the basis set
basis.set	An optional list of independence claims.
direction	a vector of claims defining the specific directionality of any independence claim(s)
interactions	whether interactions should be included in independence claims. Default is FALSE

## getDAG

conserve	whether the most conservative P-value should be returned. Default is FALSE
conditional	whether the conditioning variables should be shown in the table. Default is FALSE
.progressBar	an optional progress bar. Default is FALSE

#### Value

a data.frame corresponding to the C statistic, d.f., and P-value

getDAG	Generate adjacency matrix from	list of structural equations
0		······································

#### Description

Generate adjacency matrix from list of structural equations

#### Usage

getDAG(modelList)

## Arguments

modelList A list of structural equations

getSortedPsem Get a sorted psem object in DAG order

## Description

Takes a [psem] object, pulls out the DAG, and then sorts the psem object into the order of the DAG (from exogenous to terminal endogenous variable) for use by other functions. Note: removes correlated errors.

## Usage

```
getSortedPsem(object, keepdata = TRUE)
```

## Arguments

object	A fit [psem] object
keepdata	Defaults to TRUE. Should the data with the psem be included in the returned object?

## Value

A new [psem] object, without the data.

import

## Description

Functions to import from dependencies

keeley

## Data set from Grace & Keeley (2006)

## Description

Data set from Grace & Keeley (2006)

## Usage

keeley

## Format

A data.frame with 90 observations of 8 variables.

distance Distance to coast

elev Elevation from sea level

abiotic Abiotic favorability

age Age of stand before fire

hetero Plot heterogeneity

firesev Severity of fire

cover Cover of plants

rich Plant species richness

#### Description

Derivation of log-likelihoods to be used in determining the goodness-of-fit for piecewise structural equation models.

## Usage

```
LLchisq(
  modelList,
  basis.set = NULL,
  direction = NULL,
  interactions = FALSE,
  conserve = FALSE
)
```

## Arguments

modelList	A list of structural equations created using psem.
basis.set	An optional list of independence claims.
direction	A vector of claims defining the specific directionality of independence claims; for use in special cases (see dSep.
interactions	whether interactions should be included in basis set. Default is FALSE
conserve	Whether the most conservative log-likelihood should be returned; for use in special cases (see Details). Default is FALSE.

## Details

Here, a list of saturated models is first derived from the list of structured equations using the basis set. Then, the differences in summed log-likelihoods are computed and used to calculate the Chi-squared statistic.

#### Value

a data.frame corresponding to the Chi-squared statistic, d.f., and P-value

## Author(s)

Jon Lefcheck <LefcheckJ@si.edu>

#### References

Shipley, Bill, and Jacob C. Douma. "Generalized AIC and chi-squared statistics for path models consistent with directed acyclic graphs." Ecology 101.3 (2020): e02960.

meadows

## See Also

basisSet, dSep

## Examples

```
mod <- psem(
lm(rich ~ cover, data = keeley),
lm(cover ~ firesev, data = keeley),
lm(firesev ~ age, data = keeley),
data = keeley
)</pre>
```

LLchisq(mod)

meadows

Data set from Grace & Jutila (1999)

## Description

Data set from Grace & Jutila (1999)

#### Usage

meadows

## Format

A data.frame with 354 observations of 4 variables.

**grazed** Whether meadows were exposed to grazing: 0 = no, 1 = yes

mass Plant biomass in g m[-2]

elev Elevation of the plot above mean sea level

rich Plant species richness per m[2]

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multigroup

## Description

Multigroup Analysis for Piecewise SEM

## Usage

```
multigroup(
  modelList,
  group,
  standardize = "scale",
  standardize.type = "latent.linear",
  test.type = "III"
)
```

## Arguments

modelList	a list of structural equations
group	the name of the grouping variable in quotes
standardize	The type of standardization: none, scale, range. Default is scale.
standardize.typ	be
	The type of standardized for non-Gaussian responses: latent.linear, Menard.OE. Default is latent.linear.
test.type	what kind of ANOVA should be reported. Default is type III

## Author(s)

Jon Lefcheck <lefcheckj@si.edu>

## Examples

```
data(meadows)
jutila <- psem(
lm(rich ~ elev + mass, data = meadows),
lm(mass ~ elev, data = meadows)
)
jutila.multigroup <- multigroup(jutila, group = "grazed")
jutila.multigroup</pre>
```

partialResid

#### Description

Extracts partial residuals from a model or psem object for a given x and y.

#### Usage

partialResid(formula., modelList, data = NULL)

#### Arguments

formula.	A formula where the 1hs is the response and the rhs is the predictor whose partial effect is desired.
modelList	A list of structural equations.
data	A data.frame used to fit the equations.

#### Details

This function computes the partial residuals of  $y \sim x + Z$  in a two-step procedure to remove the variation explained by Z: (1) remove x from the equation and model  $y \sim Z$ , and (2) replace y with x and model  $x \sim Z$ .

## Value

Returns a data.frame of residuals of y ~ Z called yresids, of x ~ Z called xresids.

#### Author(s)

Jon Lefcheck <lefcheckj@si.edu>

#### See Also

cerror

#### Examples

```
# Generate data
dat <- data.frame(y = rnorm(100), x1 = rnorm(100), x2 = rnorm(100))
# Build model
model <- lm(y ~ x1 + x2, dat)
# Compute partial residuals of y ~ x1
yresid <- resid(lm(y ~ x2, dat))
xresid <- resid(lm(x1 ~ x2, dat))</pre>
```

## plot.psem

```
plot(xresid, yresid)
# Use partialResid
presid <- partialResid(y ~ x1, model)
with(presid, plot(xresid, yresid)) # identical plot!</pre>
```

plot.psem

Plotting of Piecewise Structural Equation Models

#### Description

plot.psem uses [DiagrammeR] to generate path diagrams of 'piecewiseSEM" fits within R.

## Usage

```
## S3 method for class 'psem'
plot(
    x,
    return = FALSE,
    node_attrs = data.frame(shape = "rectangle", color = "black", fillcolor = "white"),
    edge_attrs = data.frame(style = "solid", color = "black"),
    ns_dashed = T,
    alpha = 0.05,
    show = "std",
    digits = 3,
    add_edge_label_spaces = TRUE,
    ...
)
```

x	a [psem()] object
return	whether to return the output from [DiagrammeR::create_graph()] for modifica- tion and later plotting
node_attrs	List of node attributes to override defaults of rectangular nodes with black out- line and white fill. See [here](http://visualizers.co/diagrammer/articles/node- edge-data-frames.html) and [here](http://visualizers.co/diagrammer/articles/graphviz- mermaid.html) for a more complete rundown of options.
edge_attrs	List of edge attributes to override defaults of solid black arrows. See [here](http://visualizers.co/diagramm edge-data-frames.html) and [here](http://visualizers.co/diagrammer/articles/graphviz-mermaid.html) for a more complete rundown of options.
ns_dashed	If TRUE, paths that are not different from 0 will be dashed rather than solid, unless the whole is overridden in 'edge_attrs'

alpha	The alpha level for assessing whether a path is different from 0	
show	What types of path coefficients are shown? Default '"std"' is standardized coefficients. For undstandardized, use '"unstd"'	
digits	How many significant digits should be shown?	
add_edge_label_spaces		
	Should spaces by added on either side of edge labels? Default is 'TRUE' as otherwise paths too often overlap edges.	
	Other arguments to [DiagrammeR::render_graph()]	

#### Value

Returns an object of class [DiagrammeR::dgr\_graph]

## Author(s)

Jarrett Byrnes <jarrett.byrnes@umb.edu>

## Examples

```
data(keeley)
mod <- psem(
    lm(rich ~ cover, data=keeley),
    lm(cover ~ firesev, data=keeley),
    lm(firesev ~ age, data=keeley),
    data = keeley
)
plot(mod)
### More customized plot
plot(mod, node_attrs = list(
    shape = "rectangle", color = "black",
    fillcolor = "orange", x = 3, y=1:4))</pre>
```

print.anova.psem Print anova

## Description

Print anova

#### Usage

```
## S3 method for class 'anova.psem'
print(x, ...)
```

## print.basisSet

## Arguments

x	an object of class anova.psem
	further arguments passed to or from other methods

print.basisSet Print basis set

## Description

Print basis set

## Usage

## S3 method for class 'basisSet'
print(x, ...)

## Arguments

х	a basis set
	further arguments passed to or from other methods

print.multigroup.psem Print multigroup

## Description

Print multigroup

## Usage

```
## S3 method for class 'multigroup.psem'
print(x, ...)
```

х	an object to print
	additional arguments to print

print.psem

Print psem

## Description

Print psem

## Usage

## S3 method for class 'psem'
print(x, ...)

## Arguments

х	an object of class psem
	further arguments passed to or from other methods

print.summary.psem Print summary

## Description

Print summary

## Usage

```
## S3 method for class 'summary.psem'
print(x, ...)
```

х	an object of class summary.psem
	further arguments passed to or from other methods

psem

#### Description

psem is used to unite a list of structural equations into a single structural equation model.

#### Usage

psem(...)

#### Arguments

... A list of structural equations

## Details

psem takes a list of structural equations, which can be model objects of classes: lm, glm, gls, pgls, Sarlm, lme, glmmPQL, lmerMod, lmerModLmerTest, glmerMod, glmmTMB, gam.

It also takes objects of class formula, formula.cerror, corresponding to additional variables to be included in the tests of directed separation  $(X \sim 1)$  or correlated errors  $(X1 \% \sim \% X2)$ .

The function optionally accepts data objects of classes: matrix, data.frame, SpatialPointsDataFrame, comparative.data, or these are derived internally from the structural equations.

#### Value

Returns an object of class psem

## Author(s)

Jon Lefcheck <LefcheckJ@si.edu>

## See Also

summary.psem, %~~%

#### Examples

```
mod <- psem(
lm(rich ~ cover, data = keeley),
lm(cover ~ firesev, data = keeley),
lm(firesev ~ age, data = keeley),
data = keeley
)</pre>
```

summary(mod)

residuals.psem

## Description

Residual values from fit models

#### Usage

## S3 method for class 'psem'
residuals(object, ...)

## Arguments

object	a psem object
	additional arguments to residuals

#### Value

a data.frame of residuals for endogenous variables as columns

rsquared

R-squared for linear regression

## Description

Returns (pseudo)-R^2 values for all linear, generalized linear, and generalized linear mixed effects models.

#### Usage

rsquared(modelList, method = NULL)

modelList	a regression, or a list of structural equations.
method	The method used to compute the R2 value (See Details)

#### rsquared

#### Details

For mixed models, marginal R2 considers only the variance by the fixed effects, and the conditional R2 by both the fixed and random effects.

For generalized additive models fit to gaussian distribution, the function returns the adjusted-R2. For all other distributions, it returns the proportion of deviance explained.

For GLMs (glm), supported methods include:

- mcfadden 1 ratio of likelihoods of full vs. null models
- coxsnell McFadden's R2 but raised to 2/N. Upper limit is < 1
- nagelkerke Adjusts Cox-Snell R2 so that upper limit = 1. The DEFAULT method

For GLMERs fit to Poisson, Gamma, and negative binomial distributions (glmer, glmmPQL, glmer.nb), supported methods include

- delta Approximates the observation variance based on second-order Taylor series expansion. Can be used with many families and link functions
- lognormal Observation variance is the variance of the log-normal distribution
- trigamma Provides most accurate estimate of the observation variance but is limited to only the log link. The DEFAULT method

For GLMERs fit to the binomial distribution (glmer, glmmPQL), supported methods include:

- theoretical Assumes observation variance is pi<sup>2/3</sup>
- · delta Approximates the observation variance as above. The DEFAULT method

#### Value

Returns a data.frame with the response, its family and link, the method used to estimate R2, and the R2 value itself. Mixed models also return marginal and conditional R2 values.

#### Author(s)

Jon Lefcheck <lefcheckj@si.edu>

#### References

Nakagawa, Shinichi, Paul CD Johnson, and Holger Schielzeth. "The coefficient of determination R 2 and intra-class correlation coefficient from generalized linear mixed-effects models revisited and expanded." Journal of the Royal Society Interface 14.134 (2017): 20170213.

#### Examples

```
## Not run:
    # Create data
    dat <- data.frame(
        ynorm = rnorm(100),
        ypois = rpois(100, 100),
        x1 = rnorm(100),
        random = letters[1:5]</pre>
```

```
)
 # Get R2 for linear model
 rsquared(lm(ynorm ~ x1, dat))
 # Get R2 for generalized linear model
 rsquared(glm(ypois ~ x1, "poisson", dat))
 rsquared(glm(ypois ~ x1, "poisson", dat), method = "mcfadden") # McFadden R2
 # Get R2 for generalized least-squares model
 rsquared(gls(ynorm ~ x1, dat))
 # Get R2 for linear mixed effects model (nlme)
 rsquared(nlme::lme(ynorm ~ x1, random = ~ 1 | random, dat))
 # Get R2 for linear mixed effects model (lme4)
 rsquared(lme4::lmer(ynorm ~ x1 + (1 | random), dat))
 # Get R2 for generalized linear mixed effects model (lme4)
 rsquared(lme4::glmer(ypois ~ x1 + (1 | random), family = poisson, dat))
rsquared(lme4::glmer(ypois ~ x1 + (1 | random), family = poisson, dat), method = "delta")
 # Get R2 for generalized linear mixed effects model (glmmPQL)
 rsquared(MASS::glmmPQL(ypois ~ x1, random = ~ 1 | random, family = poisson, dat))
 # Get R2 for generalized additive models (gam)
 rsquared(mgcv::gam(ynorm ~ x1, dat))
```

## End(Not run)

shipley

Data set from Shipley (2006)

#### Description

Data set from Shipley (2006)

#### Usage

shipley

#### Format

A data.frame with 1900 observations of 9 variables.

site Site of observation

tree Individual tree of observation

#### summary.psem

lat Latitude
year Year of observation
Date Julian date of first bud burst
DD Cumulative degree days until first bud burst
Growth Increase in stem diameter
Survival Proportional survival
Live Alive (1) or dead (0)

summary.psem

Summarizing piecewise structural equation models

## Description

Returns information necessary to interpret piecewise structural equation models, including tests of directed separation, path coefficients, information criterion values, and R-squared values of individual models.

#### Usage

```
## S3 method for class 'psem'
summary(
 object,
  ...,
 basis.set = NULL,
 direction = NULL,
  interactions = FALSE,
  conserve = FALSE,
  conditioning = FALSE,
  add.claims = NULL,
  standardize = "scale",
  standardize.type = "latent.linear",
  test.statistic = "F",
  test.type = "II",
  intercepts = FALSE,
 AIC.type = "loglik",
  .progressBar = TRUE
)
```

object	a list of structural equations
	additional arguments to summary
basis.set	an optional basis set
direction	a vector of claims defining the specific directionality of any independence claim(s)

interactions	whether interactions should be included in independence claims. Default is FALSE
conserve	whether the most conservative P-value should be returned (See Details) Default is FALSE
conditioning	whether all conditioning variables should be shown in the table Default is FALSE
add.claims	an optional vector of additional independence claims (P-values) to be added to the basis set
standardize	whether standardized path coefficients should be reported Default is "scale"
standardize.type	
	the type of standardized for non-Gaussian responses: latent.linear (default), Mendard.OE
test.statistic	the type of test statistic generated by Anova
test.statistic test.type	the type of test statistic generated by Anova the type of test ("II" or "III") for significance of categorical variables (from car::Anova)
	the type of test ("II" or "III") for significance of categorical variables (from
test.type	the type of test ("II" or "III") for significance of categorical variables (from car::Anova)

#### Details

The forthcoming argument groups splits the analysis based on an optional grouping factor, conducts separate d-sep tests, and reports goodness-of-fit and path coefficients for each submodel. The procedure is approximately similar to a multigroup analysis in traditional variance-covariance SEM. Coming in version 2.1.

In cases involving non-normally distributed responses in the independence claims that are modeled using generalized linear models, the significance of the independence claim is not reversible (e.g., the P-value of Y ~ X is not the same as X ~ Y). This is due to the transformation of the response via the link function. In extreme cases, this can bias the goodness-of-fit tests. summary.psem will issue a warning when this case is present and provide guidance for solutions. One solution is to specify the directionality of the relationship using the direction argument, e.g. direction = c("X <- Y"). Another is to run both tests (Y ~ X, X ~ Y) and return the most conservative (i.e., lowest) P-value, which can be toggled using the conserve = TRUE argument.

In some cases, additional claims that were excluded from the basis set can be added back in using the argument add.claims. These could be, for instance, independence claims among exogenous variables. See Details in basisSet.

Standardized path coefficients are scaled by standard deviations.

## Value

The function summary.psem returns a list of summary statistics:

dTable	A summary table of the tests of directed separation, from dSep.
CStat	Fisher's C statistic, degrees of freedom, and significance value based on a Chi-
	square test.

## update.psem

AIC	Information criterion (Akaike, corrected Akaike) as well as degrees of freedom and sample size.
coefficients	A summary table of the path coefficients, from link{coefs}.
R2	(Pseudo)-R2 values, from rsquared.

#### Author(s)

Jon Lefcheck <lefcheckj@si.edu>

## References

Shipley, Bill. "A new inferential test for path models based on directed acyclic graphs." Structural Equation Modeling 7.2 (2000): 206-218.

Shipley, Bill. Cause and correlation in biology: a user's guide to path analysis, structural equations and causal inference. Cambridge University Press, 2002.

Shipley, Bill. "Confirmatory path analysis in a generalized multilevel context." Ecology 90.2 (2009): 363-368.

Shipley, Bill. "The AIC model selection method applied to path analytic models compared using a d-separation test." Ecology 94.3 (2013): 560-564.

#### See Also

The model fitting function psem.

update.psem

Update psem model object with additional values.

#### Description

Update psem model object with additional values.

#### Usage

## S3 method for class 'psem'
update(object, ...)

object	a psem object
	additional arguments to update

## Examples

```
mod <- psem(
lm(rich ~ cover, data = keeley),
lm(cover ~ firesev, data = keeley),
lm(firesev ~ age, data = keeley),
data = keeley
)
update(mod, firesev ~ age + cover)
```

%~~%

#### Correlated error operator

## Description

Specifies correlated errors among predictors

## Usage

e1 %~~% e2

#### Arguments

e1	first variable involved in correlated error
e2	second variable involved in correlated error

#### Details

For use in psem to identify correlated sets of variables.

## Author(s)

Jon Lefcheck <LefcheckJ@si.edu>, Jarrett Byrnes

#### See Also

cerror

## Examples

```
# Generate example data
dat <- data.frame(x1 = runif(50),
    x2 = runif(50), y1 = runif(50),
    y2 = runif(50))
# Create list of structural equations
sem <- psem(
    lm(y1 ~ x1 + x2, dat),</pre>
```

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```
%~~%
```

```
lm(y2 ~ y1 + x1, dat)
)
# Look at correlated error between x1 and x2
# (exogenous)
cerror(x1 %~~% x2, sem, dat)
# Same as cor.test
with(dat, cor.test(x1, x2))
# Look at correlatde error between x1 and y1
# (endogenous)
cerror(y1 %~~% x1, sem, dat)
# Not the same as cor.test
# (accounts for influence of x1 and x2 on y1)
with(dat, cor.test(y1, x1))
# Specify in psem
sem <- update(sem, x1 %~~% y1)</pre>
```

coefs(sem)

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