# Package 'mixvlmc'

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Type Package

Title Variable Length Markov Chains with Covariates

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Description Estimates Variable Length Markov Chains (VLMC) models and VLMC with covariates models from discrete sequences. Supports model selection via information criteria and simulation of new sequences from an estimated model. See Bühlmann, P. and Wyner, A. J. (1999) <doi:10.1214/aos/1018031204> for VLMC and Zanin Zambom, A., Kim, S. and Lopes Garcia, N. (2022) <doi:10.1111/jtsa.12615> for VLMC with covariates.

License GPL (>= 3)

URL https://github.com/fabrice-rossi/mixvlmc,

https://fabrice-rossi.github.io/mixvlmc/

BugReports https://github.com/fabrice-rossi/mixvlmc/issues

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mixvlmc-package mixvlmc: Variable Length Markov Chains with Covariates

## Description

Estimates Variable Length Markov Chains (VLMC) models and VLMC with covariates models from discrete sequences. Supports model selection via information criteria and simulation of new sequences from an estimated model. See Bühlmann, P. and Wyner, A. J. (1999) doi:10.1214/aos/1018031204 for VLMC and Zanin Zambom, A., Kim, S. and Lopes Garcia, N. (2022) doi:10.1111/jtsa.12615 for VLMC with covariates.

#### **Package options**

Mixvlmc uses the following options():

- mixvlmc.maxit: maximum number of iterations in model fitting for covlmc()
- mixvlmc.predictive: specifies the computing engine used for model fitting for covlmc(). Two values are supported:
  - "glm" (default value): covlmc() uses stats::glm() with a binomial link (stats::binomial()) for a two values state space, and VGAM::vglm() with a multinomial link (VGAM::multinomial()) for a state space with three or more values;
  - "multinom": covlmc() uses nnet::multinom() in all cases.

The first option "glm" is recommended as both stats::glm() and VGAM::vglm() are able to detect and deal with degeneracy in the data set.

- mixvlmc.backend: specifies the implementation used for the context tree construction in ctx\_tree(), vlmc() and tune\_vlmc(). Two values are supported:
  - "R" (default value): this corresponds to the original almost pure R implementation.
  - "C++": this corresponds to the experimental C++ implementation. This version is significantly faster than the R version, but is still considered experimental.

## Author(s)

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#### See Also

Useful links:

- https://github.com/fabrice-rossi/mixvlmc
- https://fabrice-rossi.github.io/mixvlmc/
- Report bugs at https://github.com/fabrice-rossi/mixvlmc/issues

as_covlmc	Convert an object to a Variable Length Markov Chain with covariates
	(coVLMC)

#### Description

This generic function converts an object into a covlmc.

#### as\_sequence

## Usage

```
as_covlmc(x, ...)
```

```
## S3 method for class 'tune_covlmc'
as_covlmc(x, ...)
```

## Arguments

Х	an object to convert into a covlmc.
	additional arguments for conversion functions.

## Value

a covlmc

## See Also

tune\_covlmc()

## Examples

```
## conversion from the results of tune_covlmc
pc <- powerconsumption[powerconsumption$week == 5, ]
dts <- cut(pc$active_power, breaks = c(0, quantile(pc$active_power, probs = c(0.5, 1))))
dts_cov <- data.frame(day_night = (pc$hour >= 7 & pc$hour <= 17))
dts_best_model_tune <- tune_covlmc(dts, dts_cov)
dts_best_model <- as_covlmc(dts_best_model_tune)
draw(dts_best_model)</pre>
```

as\_sequence

```
Extract the sequence encoded by a node
```

#### Description

This function returns the sequence represented by the node object.

## Usage

```
as_sequence(node, reverse)
```

## Arguments

node	a ctx_node object as returned by find_sequence()
reverse	specifies whether the sequence should be reported in reverse temporal order (TRUE) or in the temporal order (FALSE). Defaults to the order associated to the ctx_node which is determined by the parameters of the call to contexts() or find_sequence().

#### Value

the sequence represented by the node object, a vector

#### Examples

```
dts <- c("A", "B", "C", "A", "A", "B", "B", "C", "C", "A")
dts_tree <- ctx_tree(dts, max_depth = 3)
res <- find_sequence(dts_tree, "A")
as_sequence(res)</pre>
```

as\_vlmc

Convert an object to a Variable Length Markov Chain (VLMC)

## Description

This generic function converts an object into a vlmc.

## Usage

```
as_vlmc(x, ...)
## S3 method for class 'ctx_tree'
as_vlmc(x, alpha, cutoff, ...)
## S3 method for class 'tune_vlmc'
as_vlmc(x, ...)
```

## Arguments

x	an object to convert into a vlmc.
	additional arguments for conversion functions.
alpha	cut off parameter applied during the conversion, quantile scale (if specified)
cutoff	cut off parameter applied during the conversion, native scale (if specified)

## Details

This function converts a context tree into a VLMC. If alpha or cutoff is specified, it is used to reduce the complexity of the tree as in a direct call to vlmc() (prune()).

## Value

a vlmc

## See Also

ctx\_tree()
tune\_vlmc()

#### as\_vlmc.ctx\_tree\_cpp

## Examples

```
## conversion from a context tree
dts <- c(0, 1, 1, 1, 0, 0, 1, 0, 1, 0)
dts_ctree <- ctx_tree(dts, min_size = 1, max_depth = 3)
draw(dts_ctree)
dts_vlmc <- as_vlmc(dts_ctree)
class(dts_vlmc)
draw(dts_vlmc)
## conversion from the result of tune_vlmc
dts <- sample(as.factor(c("A", "B", "C")), 100, replace = TRUE)
tune_result <- tune_vlmc(dts)
tune_result
dts_best_vlmc <- as_vlmc(tune_result)
draw(dts_best_vlmc)
```

as\_vlmc.ctx\_tree\_cpp Convert an object to a Variable Length Markov Chain (VLMC)

#### Description

This generic function converts an object into a vlmc.

#### Usage

```
## S3 method for class 'ctx_tree_cpp'
as_vlmc(x, alpha, cutoff, ...)
```

#### Arguments

х	an object to convert into a vlmc.
alpha	cut off parameter applied during the conversion, quantile scale (if specified)
cutoff	cut off parameter applied during the conversion, native scale (if specified)
	additional arguments for conversion functions.

## Details

This function converts a context tree into a VLMC. If alpha or cutoff is specified, it is used to reduce the complexity of the tree as in a direct call to vlmc() (prune()).

## Value

a vlmc

## See Also

ctx\_tree()
tune\_vlmc()

## Examples

```
## conversion from a context tree
dts <- c(0, 1, 1, 1, 0, 0, 1, 0, 1, 0)
dts_ctree <- ctx_tree(dts, min_size = 1, max_depth = 3, backend = "C++")
draw(dts_ctree)
dts_vlmc <- as_vlmc(dts_ctree)
class(dts_vlmc)
draw(dts_vlmc)
```

autoplot.tune\_covlmc Create a complete ggplot for the results of automatic COVLMC complexity selection

## Description

This function prepares a plot of the results of tune\_covlmc() using ggplot2. The result can be passed to print() to display the result.

## Usage

## S3 method for class 'tune\_covlmc'
autoplot(object, ...)

#### Arguments

object	a tune_covlmc object
	additional parameters (not used currently)

## Details

The graphical representation proposed by this function is complete, while the one produced by plot.tune\_covlmc() is minimalistic. We use here the faceting capabilities of ggplot2 to combine on a single graphical representation the evolution of multiple characteristics of the VLMC during the pruning process, while plot.tune\_covlmc() shows only the selection criterion or the log like-lihood. Each facet of the resulting plot shows a quantity as a function of the cut off expressed in quantile or native scale.

#### Value

a ggplot object

#### autoplot.tune\_vlmc

#### Examples

```
pc <- powerconsumption[powerconsumption$week %in% 10:12, ]
dts <- cut(pc$active_power, breaks = c(0, quantile(pc$active_power, probs = c(0.5, 1))))
dts_cov <- data.frame(day_night = (pc$hour >= 7 & pc$hour <= 17))
dts_best_model_tune <- tune_covlmc(dts, dts_cov, criterion = "AIC")
covlmc_plot <- ggplot2::autoplot(dts_best_model_tune)
print(covlmc_plot)</pre>
```

autoplot.tune\_vlmc Create a complete ggplot for the results of automatic VLMC complexity selection

## Description

This function prepares a plot of the results of tune\_vlmc() using ggplot2. The result can be passed to print() to display the result.

#### Usage

```
## S3 method for class 'tune_vlmc'
autoplot(object, cutoff = c("quantile", "native"), ...)
```

#### Arguments

object	a tune_vlmc object
cutoff	the scale used for the cut off criterion (default "quantile")
	additional parameters (not used currently)

#### Details

The graphical representation proposed by this function is complete, while the one produced by plot.tune\_vlmc() is minimalistic. We use here the faceting capabilities of ggplot2 to combine on a single graphical representation the evolution of multiple characteristics of the VLMC during the pruning process, while plot.tune\_vlmc() shows only the selection criterion or the log likelihood. Each facet of the resulting plot shows a quantity as a function of the cut off expressed in quantile or native scale.

#### Value

a ggplot object

#### Examples

```
pc <- powerconsumption[powerconsumption$week %in% 10:11, ]
dts <- cut(pc$active_power, breaks = c(0, quantile(pc$active_power, probs = c(0.5, 1))))
dts_best_model_tune <- tune_vlmc(dts, criterion = "BIC")
vlmc_plot <- ggplot2::autoplot(dts_best_model_tune)
print(vlmc_plot)
## simple post customisation
print(vlmc_plot + ggplot2::geom_point())</pre>
```

children

Find the children nodes of a node in a context tree

## Description

This function returns a list (possibly empty) of ctx\_node objects. Each object represents one of the children of the node represented by the node parameter.

#### Usage

children(node)
## S3 method for class 'ctx\_node'
children(node)
## S3 method for class 'ctx\_node\_cpp'
children(node)

#### Arguments

node

a ctx\_node object as returned by find\_sequence()

## Details

Each node of a context tree represents a sequence. When find\_sequence() is called with success, the returned object represents the corresponding node in the context tree. If this node has no child, the present function returns an empty list. When the node has at least one child, the function returns a list with one value for each element in the state space (see states()). The value is NULL if the corresponding child is empty, while it is a ctx\_node object when the child is present. Each ctx\_node object is associated to the sequence obtained by adding to the past of the sequence represented by node an observation of the associated state (this corresponds to an extension to the left of the sequence in temporal order).

#### Value

a list of ctx\_node objects, see details.

#### contexts

#### Examples

```
dts <- c(0, 1, 1, 1, 0, 0, 1, 0, 1, 0)
dts_ctree <- ctx_tree(dts, min_size = 1, max_depth = 3)</pre>
ctx_00 <- find_sequence(dts_ctree, c(0, 0))</pre>
## this context can only be extended in the past by 1:
children(ctx_00)
ctx_10 <- find_sequence(dts_ctree, c(1, 0))</pre>
## this context can be extended by both states
children(ctx_10)
## C++ backend
dts <- c(0, 1, 1, 1, 0, 0, 1, 0, 1, 0)
dts_ctree <- ctx_tree(dts, min_size = 1, max_depth = 3, backend = "C++")</pre>
ctx_00 <- find_sequence(dts_ctree, c(0, 0))</pre>
## this context can only be extended in the past by 1:
children(ctx_00)
ctx_10 <- find_sequence(dts_ctree, c(1, 0))</pre>
## this context can be extended by both states
children(ctx_10)
```

```
contexts
```

Contexts of a context tree

#### Description

This function extracts from a context tree a description of all of its contexts.

#### Usage

```
contexts(ct, sequence = FALSE, reverse = FALSE, ...)
```

#### Arguments

ct	a context tree.
sequence	if TRUE the function returns its results as a data.frame, if FALSE (default) as a list of ctx_node objects. (see details)
reverse	logical (defaults to FALSE). See details.
	additional arguments for the contexts function.

#### Details

The default behaviour consists in returning a list of all the contexts contained in the tree using ctx\_node objects (as returned by e.g. find\_sequence()) (with type="list"). The properties of the contexts can then be explored using adapted functions such as counts() and positions(). The result list is of class contexts. When sequence=TRUE, the method returns a data.frame whose first column, named context, contains the contexts as vectors (i.e. the value returned by as\_sequence() applied to a ctx\_node object). Other columns contain context specific values which depend on the actual class of the tree and on additional parameters. In all implementations of contexts(), setting the additional parameters to any no default value leads to a data.frame result.

## Value

A list of class contexts containing the contexts represented in this tree (as ctx\_node) or a data.frame.

#### State order in a context

Notice that contexts are given by default in the temporal order and not in the "reverse" order used by many VLMC research papers: older values are on the left. For instance, the context c(1, 0) is reported if the sequence 0, then 1 appeared in the time series used to build the context tree. Set reverse to TRUE for the reverse convention which is somewhat easier to relate to the way the context trees are represented by draw() (i.e. recent values at the top the tree).

## See Also

find\_sequence() and find\_sequence.covlmc() for direct access to a specific context, and contexts.ctx\_tree(), contexts.vlmc() and contexts.covlmc() for concrete implementations of contexts().

## Examples

```
dts <- sample(as.factor(c("A", "B", "C")), 100, replace = TRUE)
dts_tree <- ctx_tree(dts, max_depth = 3, min_size = 5)
contexts(dts_tree)
contexts(dts_tree, TRUE, TRUE)</pre>
```

contexts.covlmc Contexts of a VLMC with covariates

## Description

This function returns the different contexts present in a VLMC with covariates, possibly with some associated data.

#### Usage

```
## S3 method for class 'covlmc'
contexts(
   ct,
   sequence = FALSE,
   reverse = FALSE,
   frequency = NULL,
   positions = FALSE,
   local = FALSE,
   metrics = FALSE,
   model = NULL,
   hsize = FALSE,
   merging = FALSE,
   ...
)
```

#### contexts.covlmc

#### Arguments

ct	a fitted covlmc model.
sequence	if TRUE the function returns its results as a data.frame, if FALSE (default) as a list of ctx_node objects. (see details)
reverse	logical (defaults to FALSE). See details.
frequency	specifies the counts to be included in the result data.frame. The default value of NULL does not include anything. "total" gives the number of occurrences of each context in the original sequence. "detailed" includes in addition the break down of these occurrences into all the possible states.
positions	logical (defaults to FALSE). Specify whether the positions of each context in the time series used to build the context tree should be reported in a positions column of the result data frame. The availability of the positions depends on the way the context tree was built. See details for the definition of a position.
local	specifies how the counts reported by frequency are computed. When local is FALSE (default value) the counts include both counts that are specific to the context (if any) and counts from the descendants of the context in the tree. When local is TRUE the counts include only the number of times the context appears without being the last part of a longer context.
metrics	if TRUE, adds predictive metrics for each context (see metrics() for the defi- nition of predictive metrics).
model	specifies whether to include the model associated to a each context. The default result with model=NULL does not include any model. Setting model to "coef" adds the coefficients of the models in a coef column, while "full" include the models themselves (as R objects) in a model column.
hsize	if TRUE, adds a hsize column to the result data frame that gives for each context the size of the history of covariates used by the model.
merging	if TRUE, adds a merged column to the result data frame. For a normal context, the value of merged is FALSE. Contexts that share the same model have a TRUE merged value.
	additional arguments for the contexts function.

#### Details

The default behaviour of the function is to return a list of all the contexts using ctx\_node\_covlmc objects (as returned by find\_sequence.covlmc()). The properties of the contexts can then be explored using adapted functions such as counts(), covariate\_memory(), cutoff.ctx\_node(), metrics.ctx\_node(), model(), merged\_with() and positions().

When sequence=TRUE the method returns a data.frame whose first column, named context, contains the contexts as vectors (i.e. the value returned by as\_sequence() applied to a ctx\_node object). Other columns contain context specific values specified by the additional parameters. Setting any of those parameters to a value that ask for reporting information will toggle the result type of the function to data.frame.

See contexts.ctx\_tree() for details about the frequency parameter. When model is non NULL, the resulting data.frame contains the models associated to each context (either the full R model or its coefficients). Other columns are added is the corresponding parameters are set to TRUE.

#### Value

A list of class contexts containing the contexts represented in this tree (as ctx\_node\_covlmc) or a data.frame.

## Positions

A position of a context ctx in the time series x is an index value t such that the context ends with x[t]. Thus x[t+1] is after the context. For instance if x=c(0, 0, 1, 1) and ctx=c(0, 1) (in standard state order), then the position of ctx in x is 3.

## State order in a context

Notice that contexts are given by default in the temporal order and not in the "reverse" order used by many VLMC research papers: older values are on the left. For instance, the context c(1, 0) is reported if the sequence 0, then 1 appeared in the time series used to build the context tree. Set reverse to TRUE for the reverse convention which is somewhat easier to relate to the way the context trees are represented by draw() (i.e. recent values at the top the tree).

## See Also

find\_sequence() and find\_sequence.covlmc() for direct access to a specific context, and contexts.ctx\_tree(),
contexts.vlmc() and contexts.covlmc() for concrete implementations of contexts().

#### Examples

```
pc <- powerconsumption[powerconsumption$week == 5, ]
breaks <- c(0, median(pc$active_power), max(pc$active_power))
dts <- cut(pc$active_power, breaks = breaks)
dts_cov <- data.frame(day_night = (pc$hour >= 7 & pc$hour <= 17))
m_cov <- covlmc(dts, dts_cov, min_size = 5)
## direct representation with ctx_node_covlmc objects
m_cov_ctxs <- contexts(m_cov)
m_cov_ctxs
sapply(m_cov_ctxs, covariate_memory)
sapply(m_cov_ctxs, is_merged)
sapply(m_cov_ctxs, model)
## data.frame interface
contexts(m_cov, model = "coef")
contexts(m_cov, model = "full", hsize = TRUE)</pre>
```

contexts.ctx\_tree Contexts of a context tree

#### Description

This function extracts from a context tree a description of all of its contexts.

#### contexts.ctx\_tree

## Usage

```
## S3 method for class 'ctx_tree'
contexts(
  ct,
  sequence = FALSE,
  reverse = FALSE,
  frequency = NULL,
  positions = FALSE,
  . . .
)
## S3 method for class 'ctx_tree_cpp'
contexts(
  ct,
  sequence = FALSE,
  reverse = FALSE,
  frequency = NULL,
  positions = FALSE,
  . . .
)
```

## Arguments

ct	a context tree.
sequence	if TRUE the function returns its results as a data.frame, if FALSE (default) as a list of ctx_node objects. (see details)
reverse	logical (defaults to FALSE). See details.
frequency	specifies the counts to be included in the result data.frame. The default value of NULL does not include anything. "total" gives the number of occurrences of each context in the original sequence. "detailed" includes in addition the break down of these occurrences into all the possible states.
positions	logical (defaults to FALSE). Specify whether the positions of each context in the time series used to build the context tree should be reported in a positions column of the result data frame. The availability of the positions depends on the way the context tree was built. See details for the definition of a position.
	additional arguments for the contexts function.

## Details

The default behaviour of the function is to return a list of all the contexts using ctx\_node objects (as returned by find\_sequence()). The properties of the contexts can then be explored using adapted functions such as counts() and positions().

When sequence=TRUE the method returns a data.frame whose first column, named context, contains the contexts as vectors (i.e. the value returned by as\_sequence() applied to a ctx\_node object). Other columns contain context specific values specified by the additional parameters. Setting any of those parameters to a value that ask for reporting information will toggle the result type of the function to data.frame. If frequency="total", an additional column named freq gives the number of occurrences of each context in the series used to build the tree. If frequency="detailed", one additional column is added per state in the context space. Each column records the number of times a given context is followed by the corresponding value in the original series.

#### Value

A list of class contexts containing the contexts represented in this tree (as ctx\_node) or a data.frame.

## Positions

A position of a context ctx in the time series x is an index value t such that the context ends with x[t]. Thus x[t+1] is after the context. For instance if x=c(0, 0, 1, 1) and ctx=c(0, 1) (in standard state order), then the position of ctx in x is 3.

#### State order in a context

Notice that contexts are given by default in the temporal order and not in the "reverse" order used by many VLMC research papers: older values are on the left. For instance, the context c(1, 0)is reported if the sequence 0, then 1 appeared in the time series used to build the context tree. Set reverse to TRUE for the reverse convention which is somewhat easier to relate to the way the context trees are represented by draw() (i.e. recent values at the top the tree).

#### See Also

find\_sequence() and find\_sequence.covlmc() for direct access to a specific context, and contexts.ctx\_tree(),
contexts.vlmc() and contexts.covlmc() for concrete implementations of contexts().

## Examples

```
dts <- sample(as.factor(c("A", "B", "C")), 100, replace = TRUE)
dts_tree <- ctx_tree(dts, max_depth = 3, min_size = 5)
## direct representation with ctx_node objects
contexts(dts_tree)
## data.frame format
contexts(dts_tree, sequence = TRUE)
contexts(dts_tree, frequency = "total")
contexts(dts_tree, frequency = "detailed")</pre>
```

contexts.vlmc Contexts of a VLMC

#### Description

This function extracts all the contexts from a fitted VLMC, possibly with some associated data.

## contexts.vlmc

## Usage

```
## S3 method for class 'vlmc'
contexts(
 ct,
  sequence = FALSE,
  reverse = FALSE,
  frequency = NULL,
 positions = FALSE,
 local = FALSE,
 cutoff = NULL,
 metrics = FALSE,
  . . .
)
## S3 method for class 'vlmc_cpp'
contexts(
 ct,
  sequence = FALSE,
  reverse = FALSE,
 frequency = NULL,
 positions = FALSE,
 local = FALSE,
 cutoff = NULL,
 metrics = FALSE,
  . . .
)
```

## Arguments

ct	a context tree.
sequence	if TRUE the function returns its results as a data.frame, if FALSE (default) as a list of ctx_node objects. (see details)
reverse	logical (defaults to FALSE). See details.
frequency	specifies the counts to be included in the result data.frame. The default value of NULL does not include anything. "total" gives the number of occurrences of each context in the original sequence. "detailed" includes in addition the break down of these occurrences into all the possible states.
positions	logical (defaults to FALSE). Specify whether the positions of each context in the time series used to build the context tree should be reported in a positions column of the result data frame. The availability of the positions depends on the way the context tree was built. See details for the definition of a position.
local	specifies how the counts reported by frequency are computed. When local is FALSE (default value) the counts include both counts that are specific to the context (if any) and counts from the descendants of the context in the tree. When local is TRUE the counts include only the number of times the context appears without being the last part of a longer context.

cutoff	specifies whether to include the cut off value associated to each context (see cutoff() and prune()). The default result with cutoff=NULL does not include those values. Setting cutoff to quantile adds the cut off values in quantile scale, while cutoff="native" adds them in the native scale. The returned values are directly based on the log likelihood ratio computed in the context tree and are not modified to ensure pruning (as when cutoff() is called by raw=TRUE).
metrics	if TRUE, adds predictive metrics for each context (see metrics() for the defi- nition of predictive metrics).
	additional arguments for the contexts function.

## Details

The default behaviour of the function is to return a list of all the contexts using ctx\_node objects (as returned by find\_sequence()). The properties of the contexts can then be explored using adapted functions such as counts(), cutoff.ctx\_node(), metrics.ctx\_node() and positions().

When sequence=TRUE the method returns a data.frame whose first column, named context, contains the contexts as vectors (i.e. the value returned by as\_sequence() applied to a ctx\_node object). Other columns contain context specific values specified by the additional parameters. Setting any of those parameters to a value that ask for reporting information will toggle the result type of the function to data.frame.

The frequency parameter is described in details in the documentation of contexts.ctx\_tree(). When cutoff is non NULL, the resulting data.frame contains a cutoff column with the cut off values, either in quantile or in native scale. See cutoff.vlmc() and prune.vlmc() for the definitions of cut off values and of the two scales.

## Value

A list of class contexts containing the contexts represented in this tree (as ctx\_node) or a data.frame.

## Cut off values

The cut off values reported by contexts.vlmc can be different from the ones reported by cutoff.vlmc() for three reasons:

- cutoff.vlmc() reports only useful cut off values, i.e., cut off values that should induce a simplification of the VLMC when used in prune(). This exclude cut off values associated to simple contexts that are smaller than the ones of their descendants in the context tree. Those values are reported by context.vlmc.
- context.vlmc reports only cut off values of actual contexts, while cutoff.vlmc() reports cut off values for all nodes of the context tree.
- 3. values are not modified to induce pruning, contrarily to the default behaviour of cutoff.vlmc()

#### Positions

A position of a context ctx in the time series x is an index value t such that the context ends with x[t]. Thus x[t+1] is after the context. For instance if x=c(0, 0, 1, 1) and ctx=c(0, 1) (in standard state order), then the position of ctx in x is 3.

#### context\_number

#### State order in a context

Notice that contexts are given by default in the temporal order and not in the "reverse" order used by many VLMC research papers: older values are on the left. For instance, the context c(1, 0)is reported if the sequence 0, then 1 appeared in the time series used to build the context tree. Set reverse to TRUE for the reverse convention which is somewhat easier to relate to the way the context trees are represented by draw() (i.e. recent values at the top the tree).

## See Also

find\_sequence() and find\_sequence.covlmc() for direct access to a specific context, and contexts.ctx\_tree(), contexts.vlmc() and contexts.covlmc() for concrete implementations of contexts().

#### Examples

```
dts <- sample(as.factor(c("A", "B", "C")), 100, replace = TRUE)
model <- vlmc(dts, alpha = 0.5)
## direct representation with ctx_node objects
model_ctxs <- contexts(model)
model_ctxs
sapply(model_ctxs, cutoff, scale = "quantile")
sapply(model_ctxs, cutoff, scale = "native")
sapply(model_ctxs, function(x) metrics(x)$accuracy)
## data.frame format
contexts(model, frequency = "total")
contexts(model, cutoff = "quantile")
contexts(model, cutoff = "native", metrics = TRUE)</pre>
```

context\_number Number of contexts of a context tree

#### Description

This function returns the number of distinct contexts in a context tree.

#### Usage

```
context_number(ct)
```

#### Arguments

ct a context tree.

#### Value

the number of contexts of the tree.

counts

## Examples

```
dts <- c(0, 1, 1, 1, 0, 0, 1, 0, 1, 0)
dts_ctree <- ctx_tree(dts, min_size = 1, max_depth = 3)
# should be 8
context_number(dts_ctree)</pre>
```

context\_number.covlmc Contexts number of a VLMC with covariates

#### Description

This function returns the total number of contexts of a VLMC with covariates.

#### Usage

```
## S3 method for class 'covlmc'
context_number(ct)
```

## Arguments

ct a fitted covlmc model.

#### Value

the number of contexts present in the VLMC with covariates.

## Examples

```
pc <- powerconsumption[powerconsumption$week == 5, ]
dts <- cut(pc$active_power, breaks = c(0, quantile(pc$active_power, probs = c(0.5, 1))))
dts_cov <- data.frame(day_night = (pc$hour >= 7 & pc$hour <= 17))
m_cov <- covlmc(dts, dts_cov, min_size = 10)
# should be 3
context_number(m_cov)</pre>
```

counts

Report the distribution of values that follow occurrences of a sequence

## Description

This function reports the number of occurrences of the sequence represented by node in the original time series used to build the associated context tree (not including a possible final occurrence not followed by any value at the end of the original time series). In addition if frequency=="detailed", the function reports the frequencies of each of the possible value of the time series when they appear just after the sequence.

#### counts

## Usage

```
counts(node, frequency = c("detailed", "total"), local = FALSE)
## S3 method for class 'ctx_node'
counts(node, frequency = c("detailed", "total"), local = FALSE)
## S3 method for class 'ctx_node_cpp'
counts(node, frequency = c("detailed", "total"), local = FALSE)
```

## Arguments

node	a ctx_node object as returned by find_sequence()
frequency	specifies the counts to be included in the result. "total" gives the number of occurrences of the sequence in the original sequence. "detailed" includes in addition the break down of these occurrences into all the possible states.
local	specifies how the counts are computed. When local is FALSE (default value) the counts include both counts that are specific to the context (if any) and counts from the descendants of the context in the tree. When local is TRUE the counts include only the number of times the context appears without being the last part of a longer context.

## Value

either an integer when frequency="total" which gives the total number of occurrences of the sequence represented by node or a data.frame with a total column with the same value and a column for each of the possible value of the original time series, reporting counts in each column (see the description above).

#### See Also

contexts() and contexts.ctx\_tree()

## Examples

```
dts <- sample(as.factor(c("A", "B", "C")), 100, replace = TRUE)
dts_tree <- ctx_tree(dts, max_depth = 3, min_size = 5)
subseq <- find_sequence(dts_tree, factor(c("A", "A"), levels = c("A", "B", "C")))
if (!is.null(subseq)) {
    counts(subseq)
}</pre>
```

covariate\_depth

#### Description

This function return the longest covariate memory used by a VLMC with covariates.

#### Usage

```
covariate_depth(model)
```

#### Arguments

model a covlmc object

#### Value

the longest covariate memory of this model

## Examples

```
pc <- powerconsumption[powerconsumption$week == 5, ]
dts <- cut(pc$active_power, breaks = c(0, quantile(pc$active_power, probs = c(0.5, 1))))
m_nocovariate <- vlmc(dts)
dts_cov <- data.frame(day_night = (pc$hour >= 7 & pc$hour <= 17))
m_cov <- covlmc(dts, dts_cov, min_size = 10)
covariate_depth(m_cov)</pre>
```

covariate\_memory Covariate memory length for a COVLMC context

## Description

This function returns the length of the memory of a COVLMC context represented by a ctx\_node\_covlmc object.

#### Usage

```
covariate_memory(node)
```

## Arguments node

A ctx\_node\_covlmc object as returned by find\_sequence() or contexts.covlmc()

## Value

the memory length, an integer

## covlmc

## Examples

```
pc <- powerconsumption[powerconsumption$week == 5, ]
dts <- cut(pc$active_power, breaks = c(0, quantile(pc$active_power, probs = c(0.5, 1))))
dts_cov <- data.frame(day_night = (pc$hour >= 7 & pc$hour <= 17))
m_cov <- covlmc(dts, dts_cov, min_size = 10)
ctxs <- contexts(m_cov)
## get all the memory lengths
sapply(ctxs, covariate_memory)</pre>
```

```
covlmc
```

*Fit a Variable Length Markov Chain with Covariates (coVLMC)* 

## Description

This function fits a Variable Length Markov Chain with covariates (coVLMC) to a discrete time series coupled with a time series of covariates.

## Usage

```
covlmc(
    x,
    covariate,
    alpha = 0.05,
    min_size = 5L,
    max_depth = 100L,
    keep_data = TRUE,
    control = covlmc_control(...),
    ...
)
```

#### Arguments

х	a discrete time series; can be numeric, character, factor or logical.
covariate	a data frame of covariates.
alpha	number in $(0,1)$ (default: 0.05) cut off value in the pruning phase (in quantile scale).
min_size	number >= 1 (default: 5). Tune the minimum number of observations for a context in the growing phase of the context tree (see below for details).
<pre>max_depth</pre>	integer >= 1 (default: 100). Longest context considered in growing phase of the context tree.
keep_data	logical (defaults to TRUE). If TRUE, the original data are stored in the resulting object to enable post pruning (see prune.covlmc()).
control	a list with control parameters, see covlmc_control().
	arguments passed to covlmc_control().

## Details

The model is built using the algorithm described in Zanin Zambom et al. As for the vlmc() approach, the algorithm builds first a context tree (see  $ctx\_tree()$ ). The min\_size parameter is used to compute the actual number of observations per context in the growing phase of the tree. It is computed as min\_size\*(1+ncol(covariate)\*d)\*(s-1) where d is the length of the context (a.k.a. the depth in the tree) and s is the number of states. This corresponds to ensuring min\_size observations per parameter of the logistic regression during the estimation phase.

Then logistic models are adjusted in the leaves at the tree: the goal of each logistic model is to estimate the conditional distribution of the next state of the times series given the context (the recent past of the time series) and delayed versions of the covariates. A pruning strategy is used to simplified the models (mainly to reduce the time window associated to the covariates) and the tree itself.

Parameters specified by control are used to fine tune the behaviour of the algorithm.

#### Value

a fitted covlmc model.

#### Logistic models

By default, covlmc uses two different computing engines for logistic models:

- when the time series has only two states, covlmc uses stats::glm() with a binomial link (stats::binomial());
- when the time series has at least three states, covlmc use VGAM::vglm() with a multinomial link (VGAM::multinomial()).

Both engines are able to detect degenerate cases and lead to more robust results that using nnet::multinom(). It is nevertheless possible to replace stats::glm() and VGAM::vglm() with nnet::multinom() by setting the global option mixvlmc.predictive to "multinom" (the default value is "glm"). Notice that while results should be comparable, there is no guarantee that they will be identical.

#### References

- Bühlmann, P. and Wyner, A. J. (1999), "Variable length Markov chains." Ann. Statist. 27 (2) 480-513 doi:10.1214/aos/1018031204
- Zanin Zambom, A., Kim, S. and Lopes Garcia, N. (2022), "Variable length Markov chain with exogenous covariates." J. Time Ser. Anal., 43 (2) 312-328 doi:10.1111/jtsa.12615

#### See Also

cutoff.covlmc() and prune.covlmc() for post-pruning.

## Examples

```
pc <- powerconsumption[powerconsumption$week == 5, ]
dts <- cut(pc$active_power, breaks = c(0, quantile(pc$active_power, probs = c(1 / 3, 2 / 3, 1))))
dts_cov <- data.frame(day_night = (pc$hour >= 7 & pc$hour <= 17))
m_cov <- covlmc(dts, dts_cov, min_size = 15)</pre>
```

#### covlmc\_control

```
draw(m_cov)
withr::with_options(
    list(mixvlmc.predictive = "multinom"),
    m_cov_nnet <- covlmc(dts, dts_cov, min_size = 15)
)
draw(m_cov_nnet)</pre>
```

covlmc\_control Control for coVLMC fitting

## Description

This function creates a list with parameters used to fine tune the coVLMC fitting algorithm.

#### Usage

```
covlmc_control(pseudo_obs = 1)
```

#### Arguments

pseudo\_obs number of fake observations of each state to add to the observed ones.

## Details

pseudo\_obs is used to regularize the probability estimations when a context is only observed followed by always the same state. Transition probabilities are computed after adding pseudo\_obs pseudo observations of each of the states (including the observed one). This corresponds to a Bayesian posterior mean estimation with a Dirichlet prior.

## Value

a list.

## Examples

```
dts <- rep(c(0, 1), 100)
dts_cov <- data.frame(y = rep(0, length(dts)))
default_model <- covlmc(dts, dts_cov)
contexts(default_model, type = "data.frame", model = "coef")$coef
control <- covlmc_control(pseudo_obs = 10)
model <- covlmc(dts, dts_cov, control = control)
contexts(model, type = "data.frame", model = "coef")$coef</pre>
```

ctx\_tree

## Description

This function builds a context tree for a time series.

#### Usage

```
ctx_tree(
    x,
    min_size = 2L,
    max_depth = 100L,
    keep_position = TRUE,
    backend = getOption("mixvlmc.backend", "R")
)
```

#### Arguments

Х	a discrete time series; can be numeric, character, factor or logical.
min_size	integer $\geq 1$ (default: 2). Minimum number of observations for a context to be included in the tree.
max_depth	integer $>= 1$ (default: 100). Maximum length of a context to be included in the tree.
keep_position	logical (default: TRUE). Should the context tree keep the position of the contexts.
backend	"R" or "C++" (default: as specified by the "mixvlmc.backend" option). Specifies the implementation used to represent the context tree and to built it. See details.

## Details

The tree represents all the sequences of symbols/states of length smaller than max\_depth that appear at least min\_size times in the time series and stores the frequencies of the states that follow each context. Optionally, the positions of the contexts in the time series can be stored in the tree.

## Value

a context tree (of class that inherits from ctx\_tree).

## **Back ends**

Two back ends are available to compute context trees:

• the "R" back end represents the tree in pure R data structures (nested lists) that be easily processed further in pure R (C++ helper functions are used to speed up the construction).

## cutoff

• the "C++" back end represents the tree with C++ classes. This back end is considered experimental. The tree is built with an optimised suffix tree algorithm which speeds up the construction by at least a factor 10 in standard settings. As the tree is kept outside of R direct reach, context trees built with the C++ back end must be restored after a saveRDS()/readRDS() sequence. This is done automatically by recomputing completely the context tree.

#### Examples

```
dts <- c(0, 1, 1, 1, 0, 0, 1, 0, 1, 0)
## get all contexts of length 2
dts_ctree <- ctx_tree(dts, min_size = 1, max_depth = 2)
draw(dts_ctree)</pre>
```

cutoff

Cut off values for VLMC like model

## Description

This generic function returns one or more cut off values that are guaranteed to have an effect on the model passed to the function when a simplification procedure is applied (in general a tree pruning operation as provided by prune()).

#### Usage

cutoff(model, ...)

## Arguments

model	a model.
	additional arguments for the cutoff function implementations

## Details

The exact definition of what is a cut off value depends on the model type and is documented in concrete implementation of the function.

## Value

a cut off value or a vector of cut off values.

#### See Also

prune()

## Examples

```
pc <- powerconsumption[powerconsumption$week == 5, ]
dts <- cut(pc$active_power, breaks = c(0, quantile(pc$active_power, probs = c(0.25, 0.5, 0.75, 1))))
model <- vlmc(dts)
draw(model)
model_cuts <- cutoff(model)
model_2 <- prune(model, model_cuts[2])
draw(model_2)</pre>
```

cutoff.covlmc Cut off values for pruning the context tree of a VLMC with covariates

#### Description

This function returns all the cut off values that should induce a pruning of the context tree of a VLMC with covariates.

#### Usage

```
## S3 method for class 'covlmc'
cutoff(model, raw = FALSE, tolerance = .Machine$double.eps^0.5, ...)
```

#### Arguments

model	a fitted COVLMC model.
raw	specify whether the returned values should be limit values computed in the model or modified values that guarantee pruning (see details)
tolerance	specify the minimum separation between two consecutive values of the cut off in native mode (before any transformation). See details.
	additional arguments for the cutoff function.

## Details

Notice that the list of cut off values returned by the function is not as complete as the one computed for a VLMC without covariates. Indeed, pruning the COVLMC tree creates new pruning opportunities that are not evaluated during the construction of the initial model, while all pruning opportunities are computed during the construction of a VLMC context tree. Nevertheless, the largest value returned by the function is guaranteed to produce the least pruned tree consistent with the reference one.

For large COVLMC, some cut off values can be almost identical, with a difference of the order of the machine epsilon value. The tolerance parameter is used to keep only values that are different enough. This is done in the quantile scale, before transformations implemented when raw is FALSE.

Notice that the loglikelihood scale is not directly useful in COVLMC as the differences in model sizes are not constant through the pruning process. As a consequence, this function does not provide mode parameter, contrarily to cutoff.vlmc().

#### cutoff.ctx\_node

Setting raw to TRUE removes the small perturbation that are subtracted from the log-likelihood ratio values computed from the COVLMC (in quantile scale).

As automated model selection is provided by tune\_covlmc(), the direct use of cutoff should be reserved to advanced exploration of the set of trees that can be obtained from a complex one, e.g. to implement model selection techniques that are not provided by tune\_covlmc().

## Value

a vector of cut off values, NULL if none can be computed

#### Examples

```
pc <- powerconsumption[powerconsumption$week == 5, ]
dts <- cut(pc$active_power, breaks = c(0, quantile(pc$active_power, probs = c(0.5, 1))))
m_nocovariate <- vlmc(dts)
draw(m_nocovariate)
dts_cov <- data.frame(day_night = (pc$hour >= 7 & pc$hour <= 17))
m_cov <- covlmc(dts, dts_cov, min_size = 5)
draw(m_cov)
cutoff(m_cov)</pre>
```

cutoff.ctx\_node Cut off value for pruning a node in the context tree of a VLMC

#### Description

This function returns the cut off value associated to a specific node in the context tree interpreted as a VLMC. The node is represented by a ctx\_node object as returned by find\_sequence() or contexts(). For details, see cutoff.vlmc().

## Usage

```
## S3 method for class 'ctx_node'
cutoff(model, scale = c("quantile", "native"), raw = FALSE, ...)
```

## Arguments

model	a ctx_node object as returned by find_sequence()
scale	specify whether the results should be "native" log likelihood ratio values or expressed in a "quantile" scale of a chi-squared distribution (defaults to "quantile").
raw	specify whether the returned values should be limit values computed in the model or modified values that guarantee pruning (see details in cutoff.vlmc())
	additional arguments for the cutoff function.

#### Value

a cut off value

#### See Also

cutoff()

#### Examples

```
pc <- powerconsumption[powerconsumption$week == 5, ]
dts <- cut(pc$active_power, breaks = c(0, quantile(pc$active_power, probs = c(0.25, 0.5, 0.75, 1))))
model <- vlmc(dts)
model_ctxs <- contexts(model)
cutoff(model_ctxs[[1]])
cutoff(model_ctxs[[2]], scale = "native", raw = TRUE)</pre>
```

cutoff.vlmc *Cut off values for pruning the context tree of a VLMC* 

## Description

This function returns a collection of cut off values that are guaranteed to induce all valid pruned trees of the context tree of a VLMC. Pruning is implemented by the prune() function.

#### Usage

```
## S3 method for class 'vlmc'
cutoff(
 model,
  scale = c("quantile", "native"),
  raw = FALSE,
  tolerance = .Machine$double.eps^0.5,
  . . .
)
## S3 method for class 'vlmc_cpp'
cutoff(
 model,
  scale = c("quantile", "native"),
  raw = FALSE,
  tolerance = .Machine$double.eps^0.5,
  . . .
)
```

#### Arguments

model	a fitted VLMC model.
scale	specify whether the results should be "native" log likelihood ratio values or expressed in a "quantile" scale of a chi-squared distribution (defaults to "quantile").
raw	specify whether the returned values should be limit values computed in the model or modified values that guarantee pruning (see details)

#### depth

tolerance	specify the minimum separation between two consecutive values of the cut off in native mode (before any transformation). See details.
	additional arguments for the cutoff function.

#### Details

By default, the function returns values that can be used directly to induce pruning in the context tree. This is done by computing the log likelihood ratios used by the context algorithm on the reference VLMC and by keeping the relevant ones. From them the function selects intermediate values that are guaranteed to generate via pruning all the VLMC models that could be generated by using larger values of the cutoff parameter that was used to build the reference model (or smaller values of the alpha parameter in "quantile" scale).

Setting the raw parameter to TRUE removes this operation on the values and asks the function to return the relevant log likelihood ratios.

For large VLMC, some log likelihood ratios can be almost identical, with a difference of the order of the machine epsilon value. The tolerance parameter is used to keep only values that are different enough. This is done in the native scale, before transformations implemented when raw is FALSE.

As automated model selection is provided by  $tune_vlmc()$ , the direct use of cutoff should be reserved to advanced exploration of the set of trees that can be obtained from a complex one, e.g. to implement model selection techniques that are not provided by  $tune_vlmc()$ .

#### Value

a vector of cut off values.

## See Also

prune() and tune\_vlmc()

## Examples

```
pc <- powerconsumption[powerconsumption$week == 5, ]
dts <- cut(pc$active_power, breaks = c(0, quantile(pc$active_power, probs = c(0.25, 0.5, 0.75, 1))))
model <- vlmc(dts)
draw(model)
model_cuts <- cutoff(model)
model_2 <- prune(model, model_cuts[2])
draw(model_2)</pre>
```

depth

Depth of a context tree

#### Description

This function returns the depth of a context tree, i.e. the length of the longest context represented in the tree.

#### Usage

depth(ct)

## Arguments

ct a context tree.

## Value

the depth of the tree.

## Examples

```
dts <- c(0, 1, 1, 1, 0, 0, 1, 0, 1, 0)
dts_ctree <- ctx_tree(dts, min_size = 1, max_depth = 3)
## should be 3
depth(dts_ctree)</pre>
```

```
draw
```

Text based representation of a context tree

## Description

This function 'draws' a context tree as a text.

## Usage

```
draw(ct, control = draw_control(), ...)
```

## Arguments

ct	a context tree.
control	a list of low level control parameters of the text representation. See details and draw_control().
	additional arguments for draw.

## Details

The function uses basic "ascii art" to represent the context tree. Characters used to represent the structure of the tree, e.g. branches, can be modified using draw\_control().

In addition to the structure of the context tree, draw can represent information attached to the node (contexts and partial contexts). This is controlled by additional parameters depending on the type of the context tree.

## Value

the context tree (invisibly).

## draw.covlmc

## Examples

```
dts <- sample(c(0, 1), 100, replace = TRUE)
ctree <- ctx_tree(dts, min_size = 10, max_depth = 2)
draw(ctree)
dts_c <- sample(c("A", "B", "CD"), 100, replace = TRUE)
ctree_c <- ctx_tree(dts_c, min_size = 10, max_depth = 2)
draw(ctree_c, draw_control(root = "x"))</pre>
```

```
draw.covlmc
```

Text based representation of a covlmc model

## Description

This function 'draws' a context tree as a text.

#### Usage

```
## S3 method for class 'covlmc'
draw(
   ct,
   control = draw_control(),
   model = c("coef", "full"),
   p_value = TRUE,
   digits = 4,
   with_state = FALSE,
   ...
)
```

#### Arguments

ct	a fitted covlmc model.
control	a list of low level control parameters of the text representation. See details and draw_control().
model	this parameter controls the display of logistic models associated to nodes. The default model="coef" represents the coefficients of the logistic models associated to each context. model="full" includes the name of the variables in the representation (see details). Setting model=NULL removes the model representations. Additional parameters can be used to tweak model representations (see details).
p_value	specifies whether the p-values of the likelihood ratio tests conducted during the covlmc construction must be included in the representation.
digits	numerical parameters and p-values are represented using the base::signif func- tion, using the number of significant digits specified with this parameter.
with_state	specifies whether to display the state associated to each dimension of the logistic model (see details).
	additional arguments for draw.

#### Details

The function uses basic "ascii art" to represent the context tree. Characters used to represent the structure of the tree, e.g. branches, can be modified using draw\_control().

In addition to the structure of the context tree, draw can represent information attached to the node (contexts and partial contexts). This is controlled by additional parameters depending on the type of the context tree.

## Value

the context tree (invisibly).

## Tweaking model representation

Model representations are affected by the following additional parameter:

• time\_sep: character(s) used to split the coefficients list by blocks associated to time delays in the covariate inclusion into the logistic model. The first block contains the intercept(s), the second block the covariate values a time t-1, the third block at time t-2, etc.

## Variable representation

When model="full", the representation includes the names of the variables used by the logistic models. Names are the one generated by the underlying logistic model, e.g. stats::glm(). Numerical variable names are used as is, while factors have levels appended. The intercept is denoted (I) to save space. The time delays are represented by an underscore followed by the time delay. For instance if the model uses the numerical covariate y with two delays, it will appear as to variables  $y_1$  and  $y_2$ .

#### State representation

When model is not NULL, the coefficients of the logistic models are presented, organized in rows associated to states. One state is used as the reference state and the logistic model aims at predicting the ratio of probability between another state and the reference one (in log scale). When with\_state is TRUE, the display includes for each row of coefficients the target state. This is useful when using e.g. VGAM::vglm as unused levels of the target variable will be automatically dropped from the model, leading to a reduce number of rows. The reference state is either shown on the first row if model is "full" or after the state on each row if model is "coef".

#### Examples

```
pc <- powerconsumption[powerconsumption$week == 5, ]
dts <- cut(pc$active_power, breaks = c(0, quantile(pc$active_power, probs = c(0.5, 1))))
dts_cov <- data.frame(day_night = (pc$hour >= 7 & pc$hour <= 17))
m_cov <- covlmc(dts, dts_cov, min_size = 5)
draw(m_cov, digits = 3)
draw(m_cov, model = NULL)
draw(m_cov, p_value = FALSE)
draw(m_cov, p_value = FALSE, time_sep = " | ")
draw(m_cov, model = "full", time_sep = " | ")</pre>
```

draw.ctx\_tree\_cpp Text based representation of a context tree

#### Description

This function 'draws' a context tree as a text.

#### Usage

```
## S3 method for class 'ctx_tree_cpp'
draw(ct, control = draw_control(), frequency = NULL, ...)
## S3 method for class 'ctx_tree'
draw(ct, control = draw_control(), frequency = NULL, ...)
```

## Arguments

ct	a context tree.
control	a list of low level control parameters of the text representation. See details and draw_control().
frequency	this parameter controls the display of node level information in the tree. The default NULL value does not include anything. Setting frequency to "total" includes the frequency of the (partial) context of the node, while "detailed" includes the frequency of the states that follow the context (as in contexts.ctx_tree()).
	additional arguments for draw.

## Details

The function uses basic "ascii art" to represent the context tree. Characters used to represent the structure of the tree, e.g. branches, can be modified using draw\_control().

In addition to the structure of the context tree, draw can represent information attached to the node (contexts and partial contexts). This is controlled by additional parameters depending on the type of the context tree.

## Value

the context tree (invisibly).

#### Examples

```
dts_c <- sample(c("A", "B", "CD"), 100, replace = TRUE)
ctree_c <- ctx_tree(dts_c, min_size = 10, max_depth = 2)
draw(ctree_c, frequency = "total")
draw(ctree_c, frequency = "detailed")</pre>
```

draw.vlmc

#### Description

This function 'draws' a context tree as a text.

#### Usage

```
## S3 method for class 'vlmc'
draw(ct, control = draw_control(), prob = TRUE, ...)
## S3 method for class 'vlmc_cpp'
draw(ct, control = draw_control(), prob = TRUE, ...)
```

#### Arguments

ct	a fitted vlmc.
control	a list of low level control parameters of the text representation. See details and draw_control().
prob	this parameter controls the display of node level information in the tree. The default prob=TRUE represents the conditional distribution of the states given the (partial) context associated to the node. Setting prob=FALSE replaces the conditional distribution by the frequency of the states that follow the context as in draw.ctx_tree(). Setting prob=NULL removes all additional information.
	additional arguments for draw.

## Details

The function uses basic "ascii art" to represent the context tree. Characters used to represent the structure of the tree, e.g. branches, can be modified using draw\_control().

In addition to the structure of the context tree, draw can represent information attached to the node (contexts and partial contexts). This is controlled by additional parameters depending on the type of the context tree.

## Value

the context tree (invisibly).

## Examples

```
dts <- sample(c("A", "B", "C"), 500, replace = TRUE)
model <- vlmc(dts, alpha = 0.05)
draw(model)
draw(model, prob = FALSE)
draw(model, prob = NULL)</pre>
```
draw\_control

# Description

This function returns a list used to fine tune the draw() function behaviour.

# Usage

```
draw_control(
   root = "*",
   first_node = "+",
   next_node = "'",
   vbranch = "|",
   hbranch = "--",
   open_ct = "(",
   close_ct = ")"
)
```

# Arguments

root	character used for the root node.
first_node	characters used for the first child of a node.
next_node	characters used for other children of a node.
vbranch	characters used to represent a branch in a vertical way.
hbranch	characters used to represent a branch in a horizontal was.
open_ct	characters used to start each node specific text representation.
close_ct	characters used to end each node specific text representation.

# Value

a list

```
draw_control(open_ct = "[", close_ct = "]")
```

```
find_sequence
```

### Description

This function checks whether the sequence ctx is represented in the context tree ct. If this is the case, it returns a description of matching node, an object of class  $ctx_node$ . If the sequence is not represented in the tree, the function return NULL.

### Usage

find\_sequence(ct, ctx, reverse = FALSE, ...)
## S3 method for class 'ctx\_tree'
find\_sequence(ct, ctx, reverse = FALSE, ...)
## S3 method for class 'ctx\_tree\_cpp'
find\_sequence(ct, ctx, reverse = FALSE, ...)

# Arguments

ct	a context tree.
ctx	a sequence to search in the context tree
reverse	specifies whether the sequence ctx is given the temporal order (FALSE, default value) or in the reverse temporal order (TRUE). See the dedicated section.
	additional parameters for the find_sequence function

# Details

The function looks for sequences in general. The is\_context() function can be used on the resulting object to test if the sequence is in addition a proper context.

#### Value

an object of class  $ctx_node$  if the sequence ctx is represented in the context tree, NULL when this is not the case.

#### State order in a sequence

sequence are given by default in the temporal order and not in the "reverse" order used by many VLMC research papers: older values are on the left. For instance, the context c(1, 0) is reported if the sequence 0, then 1 appeared in the time series used to build the context tree. In the present function, reverse refers both to the order used for the ctx parameter and for the default order used by the resulting ctx\_node object.

### find\_sequence.covlmc

# Examples

```
dts <- c("A", "B", "C", "A", "A", "B", "B", "C", "C", "A")
dts_tree <- ctx_tree(dts, max_depth = 3)
find_sequence(dts_tree, "A")
## returns NULL as "A" "C" does not appear in dts
find_sequence(dts_tree, c("A", "C"))</pre>
```

find\_sequence.covlmc Find the node of a sequence in a COVLMC context tree

# Description

This function checks whether the sequence ctx is represented in the context tree of the COVLMC model ct. If this is the case, it returns a description of matching node, an object of class ctx\_node\_covlmc. If the sequence is not represented in the tree, the function return NULL.

# Usage

```
## S3 method for class 'covlmc'
find_sequence(ct, ctx, reverse = FALSE, ...)
```

#### Arguments

ct	a context tree.
ctx	a sequence to search in the context tree
reverse	specifies whether the sequence ctx is given the temporal order (FALSE, default value) or in the reverse temporal order (TRUE). See the dedicated section.
	additional parameters for the find_sequence function

# Details

The function looks for sequences in general. The is\_context() function can be used on the resulting object to test if the sequence is in addition a proper context.

### Value

an object of class  $ctx_node_covlmc$  if the sequence ctx is represented in the context tree, NULL when this is not the case

#### State order in a sequence

sequence are given by default in the temporal order and not in the "reverse" order used by many VLMC research papers: older values are on the left. For instance, the context c(1, 0) is reported if the sequence 0, then 1 appeared in the time series used to build the context tree. In the present function, reverse refers both to the order used for the ctx parameter and for the default order used by the resulting ctx\_node object.

# Examples

```
pc <- powerconsumption[powerconsumption$week == 5, ]
dts <- cut(pc$active_power, breaks = c(0, quantile(pc$active_power, probs = c(0.5, 1))))
dts_cov <- data.frame(day_night = (pc$hour >= 7 & pc$hour <= 17))
m_cov <- covlmc(dts, dts_cov, min_size = 10)
## not in the tree
vals <- states(m_cov)
find_sequence(m_cov, c(vals[2], vals[2]))
## in the tree but not a context
node <- find_sequence(m_cov, c(vals[1]))
node
is_context(node)
## in the tree and a context
</pre>
```

node <- find\_sequence(m\_cov, c(vals[1], vals[1]))
node
is\_context(node)</pre>

```
model(node)
```

globalearthquake Significant Earthquake Dataset

#### Description

A data set containing Earthquake that have occured during the period of 1900-2022 with GPS coordinates and magnitudes.

#### Usage

globalearthquake

#### Format

A data frame with 98785 rows and 12 variables:

date\_time Date and time in POSIXct format

**latitude** latitude of the earthquake, from  $-90^{\circ}$  to  $90^{\circ}$ 

**longitude** longitude of the earthquake, from  $-180^{\circ}$  to  $180^{\circ}$ 

mag the magnitude of the earthquake, indicating its strenth

Date date when the seisme occured

**nbweeks** number of weeks since 1900/01/01

year year

month month of the year

**month\_day** day of the month

week week number

week\_day day of the week from 1 = Sunday to 7 = Saturday

year\_day day of the year from 1 to 366

### is\_context

### Details

This is a compiled version of the full data set available on U.S. Geological Survey Earthquake Events (USGS) which is in the public domain.

The data set contains only the earthquake between 1900 and 2022 with a magnitude higher than 5.

### Source

Earthquake Catalog, U.S. Geological Survey, Department of the Interior. https://www.usgs.gov/programs/earthquake-hazards

is\_context

Report the nature of a node in a context tree

# Description

This function returns TRUE if the node is a proper context, FALSE in the other case.

#### Usage

is\_context(node)

# Arguments

node

a ctx\_node object as returned by find\_sequence()

### Value

TRUE if the node node is a proper context, FALSE when this is not the case

```
dts <- c(0, 1, 1, 1, 0, 0, 1, 0, 1, 0)
dts_ctree <- ctx_tree(dts, min_size = 1, max_depth = 3)
draw(dts_ctree)
## 0, 0 is a context but 1, 0 is not
is_context(find_sequence(dts_ctree, c(0, 0)))
is_context(find_sequence(dts_ctree, c(1, 0)))</pre>
```

is\_covlmc

# Description

This function returns TRUE for VLMC models with covariates and FALSE for other objects.

# Usage

is\_covlmc(x)

### Arguments

х

an R object.

#### Value

TRUE for VLMC models with covariates.

# Examples

```
pc <- powerconsumption[powerconsumption$week == 5, ]
dts <- cut(pc$active_power, breaks = c(0, quantile(pc$active_power, probs = c(0.5, 1))))
dts_cov <- data.frame(day_night = (pc$hour >= 7 & pc$hour <= 17))
m_cov <- covlmc(dts, dts_cov, min_size = 5)
# should be true
is_ctx_tree(m_cov)
# should be true
is_covlmc(m_cov)
# should be false
is_vlmc(m_cov)</pre>
```

is\_ctx\_tree

Test if the object is a context tree

# Description

This function returns TRUE for context trees and FALSE for other objects.

# Usage

is\_ctx\_tree(x)

# Arguments ×

an R object.

### is\_merged

### Value

TRUE for context trees.

### Examples

```
dts <- c(0, 1, 1, 1, 0, 0, 1, 0, 1, 0)
dts_ctree <- ctx_tree(dts, min_size = 1, max_depth = 2)
is_ctx_tree(dts_ctree)
is_ctx_tree(dts)</pre>
```

```
is_merged
```

Merging status of a COVLMC context

# Description

The function returns TRUE if the context represented by this node is merged with at least another one and FALSE if this is not the case.

### Usage

is\_merged(node)

# Arguments

node

A ctx\_node\_covlmc object as returned by find\_sequence() or contexts.covlmc()

# Details

When a COVLMC is built on a time series with at least three distinct states, some contexts can be merged: they use the same logistic model, leading to a more parsimonious model. Those contexts are reported individually by functions such as contexts.covlmc(). The present function can be used to detect such merging, while merged\_with() can be used to recover the other contexts.

# Value

TRUE or FALSE, depending on the nature of the context

# See Also

```
merged_with()
```

```
pc <- powerconsumption[powerconsumption$week == 15, ]
dts <- cut(pc$active_power, breaks = c(0, 1, 2, 3, 8))
dts_cov <- data.frame(day_night = (pc$hour >= 7 & pc$hour <= 17))
m_cov <- covlmc(dts, dts_cov, min_size = 5, alpha = 0.1)
ctxs <- contexts(m_cov)
## no merging
sapply(ctxs, is_merged)</pre>
```

is\_reversed

# Description

This function returns TRUE if the node is using a reverse temporal ordering and FALSE in the other case.

# Usage

is\_reversed(node)

# Arguments

node

a ctx\_node object as returned by find\_sequence()

# Value

TRUE if the node node use a reverse temporal ordering, FALSE when this is not the case

### See Also

rev.ctx\_node()

# Examples

```
dts <- c(0, 1, 1, 1, 0, 0, 1, 0, 1, 0)
dts_ctree <- ctx_tree(dts, min_size = 1, max_depth = 3)
is_reversed(find_sequence(dts_ctree, c(0, 0)))
is_reversed(find_sequence(dts_ctree, c(1, 0), reverse = TRUE))</pre>
```

is\_vlmc

Test if the object is a vlmc model

### Description

This function returns TRUE for VLMC models and FALSE for other objects.

# Usage

is\_vlmc(x)

### Arguments

x an R object.

# logLik.covlmc

# Value

TRUE for VLMC models.

#### Examples

```
pc <- powerconsumption[powerconsumption$week == 5, ]
dts <- cut(pc$active_power, breaks = c(0, quantile(pc$active_power, probs = c(0.25, 0.5, 0.75, 1))))
model <- vlmc(dts)
# should be true
is_ctx_tree(model)
# should be true
is_vlmc(model)
# should be false
is_covlmc(model)</pre>
```

logLik.covlmc Log-Likelihood of a VLMC with covariates

# Description

This function evaluates the log-likelihood of a VLMC with covariates fitted on a discrete time series.

### Usage

```
## S3 method for class 'covlmc'
logLik(object, initial = c("truncated", "specific", "extended"), ...)
```

# Arguments

object	the covlmc representation.
initial	specifies the likelihood function, more precisely the way the first few observa- tions for which contexts cannot be calculated are integrated in the likelihood. Defaults to "truncated". See loglikelihood() for details.
	additional parameters for logLik.

# Value

an object of class logLik. This is a number, the log-likelihood of the (CO)VLMC with the following attributes:

- df: the number of parameters used by the VLMC for this likelihood calculation
- nobs: the number of observations included in this likelihood calculation
- initial: the value of the initial parameter used to compute this likelihood

# See Also

loglikelihood()

# Examples

```
## Likelihood for a fitted VLMC with covariates.
pc <- powerconsumption[powerconsumption$week == 5, ]
breaks <- c(
    0,
    median(powerconsumption$active_power, na.rm = TRUE),
    max(powerconsumption$active_power, na.rm = TRUE)
)
labels <- c(0, 1)
dts <- cut(pc$active_power, breaks = breaks, labels = labels)
dts_cov <- data.frame(day_night = (pc$hour >= 7 & pc$hour <= 17))
m_cov <- covlmc(dts, dts_cov, min_size = 5)
ll <- logLik(m_cov)
attributes(ll)</pre>
```

logLik.vlmc

Log-Likelihood of a VLMC

### Description

This function evaluates the log-likelihood of a VLMC fitted on a discrete time series.

# Usage

```
## S3 method for class 'vlmc'
logLik(object, initial = c("truncated", "specific", "extended"), ...)
## S3 method for class 'vlmc_cpp'
logLik(object, initial = c("truncated", "specific", "extended"), ...)
```

### Arguments

object	the vlmc representation.
initial	specifies the likelihood function, more precisely the way the first few observa- tions for which contexts cannot be calculated are integrated in the likelihood. Defaults to "truncated". See loglikelihood() for details.
	additional parameters for logLik.

### Value

an object of class logLik. This is a number, the log-likelihood of the (CO)VLMC with the following attributes:

- df: the number of parameters used by the VLMC for this likelihood calculation
- nobs: the number of observations included in this likelihood calculation
- initial: the value of the initial parameter used to compute this likelihood

# loglikelihood

# See Also

loglikelihood()

# Examples

```
pc <- powerconsumption[powerconsumption$week == 5, ]
breaks <- c(
    0,
    median(powerconsumption$active_power, na.rm = TRUE),
    max(powerconsumption$active_power, na.rm = TRUE)
)
labels <- c(0, 1)
dts <- cut(pc$active_power, breaks = breaks, labels = labels)
m_nocovariate <- vlmc(dts)
ll <- logLik(m_nocovariate)
ll
attributes(ll)</pre>
```

loglikelihood Log-Likelihood of a VLMC

# Description

This function evaluates the log-likelihood of a VLMC fitted on a discrete time series. When the optional argument newdata is provided, the function evaluates instead the log-likelihood for this (new) discrete time series.

### Usage

```
loglikelihood(
  vlmc,
  newdata,
  initial = c("truncated", "specific", "extended"),
  ignore,
  . . .
)
## S3 method for class 'vlmc'
loglikelihood(
  vlmc,
  newdata,
  initial = c("truncated", "specific", "extended"),
  ignore,
  . . .
)
## S3 method for class 'vlmc_cpp'
loglikelihood(
```

```
vlmc,
newdata,
initial = c("truncated", "specific", "extended"),
ignore,
...
```

# Arguments

)

vlmc	the vlmc representation.
newdata	an optional discrete time series.
initial	specifies the likelihood function, more precisely the way the first few observa- tions for which contexts cannot be calculated are integrated in the likelihood. Defaults to "truncated". See below for details.
ignore	specifies the number of initial values for which the loglikelihood will not be computed. The minimal number depends on the likelihood function as detailed below.
	additional parameters for loglikelihood.

# Details

The definition of the likelihood function depends on the value of the initial parameters, see the section below as well as the dedicated vignette: vignette("likelihood", package = "mixvlmc").

For VLMC objects, the method loglikelihood.vlmc will be used. For VLMC with covariables, loglikelihood.covlmc will instead be called. For more informations on loglikelihood methods, use methods(loglikelihood) and their associated documentation.

#### Value

an object of class logLikMixVLMC and logLik. This is a number, the log-likelihood of the (CO)VLMC with the following attributes:

- df: the number of parameters used by the VLMC for this likelihood calculation
- · nobs: the number of observations included in this likelihood calculation
- initial: the value of the initial parameter used to compute this likelihood

#### likelihood calculation

In a (CO)VLMC of depth()=k, we need k past values in order to compute the context of a given observation. As a consequence, in a time series x, the contexts of x[1] to x[k] are unknown. Depending on the value of initial different likelihood functions are used to tackle this difficulty:

- initial=="truncated": the likelihood is computed using only x[(k+1):length(x)]
- initial=="specific": the likelihood is computed on the full time series using a specific context for the initial values, x[1] to x[k]. Each of the specific context is unique, leading to a perfect likelihood of 1 (0 in log scale). Thus the numerical value of the likelihood is identical as the one obtained with initial=="truncated" but it is computed on length(x) with a model with more parameters than in this previous case.

#### loglikelihood

initial=="extended" (default): the likelihood is computed on the full time series using an
extended context matching for the initial values, x[1] to x[k]. This can be seen as a compromised between the two other possibilities: the relaxed context matching needs in general to
turn internal nodes of the context tree into actual context, increasing the number of parameters, but not as much as with "specific". However, the likelihood of say x[1] with an empty
context is generally not 1 and thus the full likelihood is smaller than the one computed with
"specific".

In all cases, the ignore first values of the time series are not included in the computed likelihood, but still used to compute contexts. If ignore is not specified, it is set to the minimal possible value, that is k for the truncated likelihood and 0 for the other ones. If it is specified, it must be larger or equal to k for truncated.

See the dedicated vignette for a more mathematically oriented discussion: vignette("likelihood", package = "mixvlmc").

# See Also

stats::logLik()

```
## Likelihood for a fitted VLMC.
pc <- powerconsumption[powerconsumption$week == 5, ]</pre>
breaks <- c(</pre>
  0.
  median(powerconsumption$active_power, na.rm = TRUE),
  max(powerconsumption$active_power, na.rm = TRUE)
)
labels <- c(0, 1)
dts <- cut(pc$active_power, breaks = breaks, labels = labels)</pre>
m_nocovariate <- vlmc(dts)</pre>
11 <- loglikelihood(m_nocovariate)</pre>
11
attr(ll, "nobs")
attr(ll, "df")
## Likelihood for a new time series with previously fitted VLMC.
pc_new <- powerconsumption[powerconsumption$week == 11, ]</pre>
dts_new <- cut(pc_new$active_power, breaks = breaks, labels = labels)</pre>
ll_new <- loglikelihood(m_nocovariate, newdata = dts_new)</pre>
ll_new
attributes(ll_new)
ll_new_specific <- loglikelihood(m_nocovariate, initial = "specific", newdata = dts_new)</pre>
11_new_specific
attributes(ll_new_specific)
ll_new_extended <- loglikelihood(m_nocovariate, initial = "extended", newdata = dts_new)</pre>
11_new_extended
attributes(ll_new_extended)
```

loglikelihood.covlmc Log-Likelihood of a VLMC with covariates

## Description

This function evaluates the log-likelihood of a VLMC with covariates fitted on a discrete time series. When the optional arguments newdata is provided, the function evaluates instead the log-likelihood for this (new) discrete time series on the new covariates which must be provided through the newcov parameter.

# Usage

```
## S3 method for class 'covlmc'
loglikelihood(
  vlmc,
  newdata,
  initial = c("truncated", "specific", "extended"),
  ignore,
  newcov,
  ...
)
```

### Arguments

vlmc	the covlmc representation.
newdata	an optional discrete time series.
initial	specifies the likelihood function, more precisely the way the first few observa- tions for which contexts cannot be calculated are integrated in the likelihood. Defaults to "truncated". See below for details.
ignore	specifies the number of initial values for which the loglikelihood will not be computed. The minimal number depends on the likelihood function as detailed below.
newcov	an optional data frame with the new values for the covariates.
	additional parameters for loglikelihood.

# Details

The definition of the likelihood function depends on the value of the initial parameters, see the section below as well as the dedicated vignette: vignette("likelihood", package = "mixvlmc").

# Value

an object of class logLikMixVLMC and logLik. This is a number, the log-likelihood of the (CO)VLMC with the following attributes:

• df: the number of parameters used by the VLMC for this likelihood calculation

- · nobs: the number of observations included in this likelihood calculation
- initial: the value of the initial parameter used to compute this likelihood

#### likelihood calculation

In a (CO)VLMC of depth()=k, we need k past values in order to compute the context of a given observation. As a consequence, in a time series x, the contexts of x[1] to x[k] are unknown. Depending on the value of initial different likelihood functions are used to tackle this difficulty:

- initial=="truncated": the likelihood is computed using only x[(k+1):length(x)]
- initial=="specific": the likelihood is computed on the full time series using a specific context for the initial values, x[1] to x[k]. Each of the specific context is unique, leading to a perfect likelihood of 1 (0 in log scale). Thus the numerical value of the likelihood is identical as the one obtained with initial=="truncated" but it is computed on length(x) with a model with more parameters than in this previous case.
- initial=="extended" (default): the likelihood is computed on the full time series using an
  extended context matching for the initial values, x[1] to x[k]. This can be seen as a compromised between the two other possibilities: the relaxed context matching needs in general to
  turn internal nodes of the context tree into actual context, increasing the number of parameters, but not as much as with "specific". However, the likelihood of say x[1] with an empty
  context is generally not 1 and thus the full likelihood is smaller than the one computed with
  "specific".

In all cases, the ignore first values of the time series are not included in the computed likelihood, but still used to compute contexts. If ignore is not specified, it is set to the minimal possible value, that is k for the truncated likelihood and 0 for the other ones. If it is specified, it must be larger or equal to k for truncated.

See the dedicated vignette for a more mathematically oriented discussion: vignette("likelihood", package = "mixvlmc").

# See Also

#### stats::logLik()

```
## Likelihood for a fitted VLMC with covariates.
pc <- powerconsumption[powerconsumption$week == 5, ]
breaks <- c(
    0,
    median(powerconsumption$active_power, na.rm = TRUE),
    max(powerconsumption$active_power, na.rm = TRUE)
)
labels <- c(0, 1)
dts <- cut(pc$active_power, breaks = breaks, labels = labels)
dts_cov <- data.frame(day_night = (pc$hour >= 7 & pc$hour <= 17))
m_cov <- covlmc(dts, dts_cov, min_size = 5)
ll <- loglikelihood(m_cov)
ll
attr(ll, "nobs")</pre>
```

```
## Likelihood for new time series and covariates with previously
## fitted VLMC with covariates
pc_new <- powerconsumption[powerconsumption$week == 11, ]
dts_new <- cut(pc_new$active_power, breaks = breaks, labels = labels)
dts_cov_new <- data.frame(day_night = (pc_new$hour >= 7 & pc_new$hour <= 17))
ll_new <- loglikelihood(m_cov, newdata = dts_new, newcov = dts_cov_new)
ll_new
attributes(ll_new)</pre>
```

merged\_with

# Merged contexts in a COVLMC

# Description

The function returns NULL when the context represented by the node parameter is not merged with another context (see is\_merged()). In the other case, it returns a list of contexts with which this one is merged.

### Usage

merged\_with(node)

### Arguments

node

A ctx\_node\_covlmc object as returned by find\_sequence() or contexts.covlmc()

# Details

If the context is merged, the function returns a list with one value for each element in the state space (see states()). The value is NULL if the corresponding context is not merged with the node context, while it is a ctx\_node\_covlmc object in the other case. A context merged with node differs from the context represented by node only in its last value (in temporal order) which is used as its name in the list. For instance, if the context ABC is merged only with CBC (when represented in temporal ordering), then the resulting list is of the form list("A" = NULL, "B" = NULL, "C"= ctx\_node\_covlmc(CBX)).

# Value

NULL or a list of contexts merged with node represented by ctx\_node\_covlmc objects

#### See Also

is\_merged()

#### metrics

# Examples

```
pc_week_15_16 <- powerconsumption[powerconsumption$week %in% c(15, 16), ]
elec <- pc_week_15_16$active_power
elec_dts <- cut(elec, breaks = c(0, 0.4, 2, 8), labels = c("low", "typical", "high"))
elec_cov <- data.frame(day = (pc_week_15_16$hour >= 7 & pc_week_15_16$hour <= 18))
elec_tune <- tune_covlmc(elec_dts, elec_cov, min_size = 5)
elec_model <- prune(as_covlmc(elec_tune), alpha = 3.961e-10)
ctxs <- contexts(elec_model)
for (ctx in ctxs) {
    if (is_merged(ctx)) {
        print(ctx)
        cat("\nis merged with\n\n")
        print(merged_with(ctx))
    }
}</pre>
```

metrics

Predictive quality metrics for context based models

# Description

This function computes and returns predictive quality metrics for context based models such as VLMC and VLMC with covariates.

### Usage

metrics(model, ...)

#### Arguments

model	The context based model on which to compute predictive metrics.
	Additional parameters for predictive metrics computation.

### Details

A context based model computes transition probabilities for its contexts. Using a maximum transition probability decision rule, this can be used to predict the new state that is the more likely to follow the current one, given the context (see predict.vlmc()). The quality of these predictions is evaluated using standard metrics including:

- accuracy
- the full confusion matrix
- the area under the roc curve (AUC), considering the context based model as a (conditional) probability estimator. We use Hand and Till (2001) multiclass AUC in case of a state space with more than 2 states

# Value

The returned value is guaranteed to have at least three components

- accuracy: the accuracy of the predictions
- conf\_mat: the confusion matrix of the predictions, with predicted values in rows and true values in columns
- auc: the AUC of the predictive model

## References

David J. Hand and Robert J. Till (2001). "A Simple Generalisation of the Area Under the ROC Curve for Multiple Class Classification Problems." *Machine Learning* 45(2), p. 171–186. DOI: doi:10.1023/A:1010920819831.

# See Also

```
metrics.vlmc(), metrics.ctx_node(), contexts.vlmc(), predict.vlmc().
```

#### Examples

```
pc <- powerconsumption[powerconsumption$week == 5, ]
breaks <- c(
    0,
    median(powerconsumption$active_power, na.rm = TRUE),
    max(powerconsumption$active_power, na.rm = TRUE)
)
labels <- c(0, 1)
dts <- cut(pc$active_power, breaks = breaks, labels = labels)
model <- vlmc(dts)
metrics(model)</pre>
```

metrics.covlmc Predictive quality metrics for VLMC with covariates

### Description

This function computes and returns predictive quality metrics for context based models such as VLMC and VLMC with covariates.

# Usage

```
## S3 method for class 'covlmc'
metrics(model, ...)
## S3 method for class 'metrics.covlmc'
print(x, ...)
```

#### metrics.covlmc

#### Arguments

model	The context based model on which to compute predictive metrics.
	Additional parameters for predictive metrics computation.
x	A metrics.covlmc object, results of a call to metrics.covlmc()

# Details

A context based model computes transition probabilities for its contexts. Using a maximum transition probability decision rule, this can be used to predict the new state that is the more likely to follow the current one, given the context (see predict.vlmc()). The quality of these predictions is evaluated using standard metrics including:

- accuracy
- the full confusion matrix
- the area under the roc curve (AUC), considering the context based model as a (conditional) probability estimator. We use Hand and Till (2001) multiclass AUC in case of a state space with more than 2 states

#### Value

An object of class metrics.covlmc with the following components:

- accuracy: the accuracy of the predictions
- conf\_mat: the confusion matrix of the predictions, with predicted values in rows and true values in columns
- auc: the AUC of the predictive model

The object has a print method that recalls basic information about the model together with the values of the components above.

# Methods (by generic)

• print(metrics.covlmc): Prints the predictive metrics of the VLMC model with covariates.

# **Extended contexts**

As explained in details in loglikelihood.covlmc() documentation and in the dedicated vignette("likelihood", package = "mixvlmc"), the first initial values of a time series do not in general have a proper context for a COVLMC with a non zero order. In order to predict something meaningful for those values, we rely on the notion of extended context defined in the documents mentioned above. This follows the same logic as using loglikelihood.covlmc() with the parameter initial="extended". All covlmc functions that need to manipulate initial values with no proper context use the same approach.

# References

David J. Hand and Robert J. Till (2001). "A Simple Generalisation of the Area Under the ROC Curve for Multiple Class Classification Problems." *Machine Learning* 45(2), p. 171–186. DOI: doi:10.1023/A:1010920819831.

# See Also

metrics.vlmc(), metrics.ctx\_node(), contexts.vlmc(), predict.vlmc().

### Examples

```
pc <- powerconsumption[powerconsumption$week == 5, ]
breaks <- c(
    0,
    median(powerconsumption$active_power, na.rm = TRUE),
    max(powerconsumption$active_power, na.rm = TRUE)
)
labels <- c(0, 1)
dts <- cut(pc$active_power, breaks = breaks, labels = labels)
dts_cov <- data.frame(day_night = (pc$hour >= 7 & pc$hour <= 17))
m_cov <- covlmc(dts, dts_cov, min_size = 5)
metrics(m_cov)</pre>
```

metrics.ctx\_node *Predictive quality metrics for a node of a context tree* 

### Description

This function computes and returns predictive quality metrics for a node (ctx\_node) extracted from a context tree.

#### Usage

## S3 method for class 'ctx\_node'
metrics(model, ...)

# Arguments

model	T ctx_node object as returned by find_sequence().
	Additional parameters for predictive metrics computation.

# Details

Compared to metrics.vlmc(), this function focuses on a single context and assesses the quality of its predictions, disregarding observations that have other contexts. Apart from this limited scope, the function operates as metrics.vlmc().

# Value

The returned value is guaranteed to have at least three components

- accuracy: the accuracy of the predictions
- conf\_mat: the confusion matrix of the predictions, with predicted values in rows and true values in columns
- auc: the AUC of the predictive model

### References

David J. Hand and Robert J. Till (2001). "A Simple Generalisation of the Area Under the ROC Curve for Multiple Class Classification Problems." *Machine Learning* 45(2), p. 171–186. DOI: doi:10.1023/A:1010920819831.

# See Also

metrics.vlmc(), metrics.ctx\_node(), contexts.vlmc(), predict.vlmc().

# Examples

```
pc <- powerconsumption[powerconsumption$week == 5, ]
dts <- cut(pc$active_power, breaks = c(0, quantile(pc$active_power, probs = c(0.25, 0.5, 0.75, 1))))
model <- vlmc(dts)
model_ctxs <- contexts(model)
metrics(model_ctxs[[4]])</pre>
```

metrics.ctx\_node\_covlmc

Predictive quality metrics for a node of a COVLMC context tree

### Description

This function computes and returns predictive quality metrics for a node (ctx\_node\_covlmc) extracted from a covlmc

# Usage

## S3 method for class 'ctx\_node\_covlmc'
metrics(model, ...)

### Arguments

model	A ctx_node_covlmc object as returned by find_sequence() or contexts.covlmc()
	Additional parameters for predictive metrics computation.

# Details

Compared to metrics.covlmc(), this function focuses on a single context and assesses the quality of its predictions, disregarding observations that have other contexts. Apart from this limited scope, the function operates as metrics.covlmc().

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Value

an object of class metrics.covlmc with the following components:

- · accuracy: the accuracy of the predictions
- conf\_mat: the confusion matrix of the predictions, with predicted values in rows and true values in columns
- auc: the AUC of the predictive model

#### References

David J. Hand and Robert J. Till (2001). "A Simple Generalisation of the Area Under the ROC Curve for Multiple Class Classification Problems." *Machine Learning* 45(2), p. 171–186. DOI: doi:10.1023/A:1010920819831.

# See Also

metrics.vlmc(), metrics.ctx\_node(), contexts.vlmc(), predict.vlmc().

# Examples

```
pc <- powerconsumption[powerconsumption$week == 5, ]
breaks <- c(
    0,
    median(powerconsumption$active_power, na.rm = TRUE),
    max(powerconsumption$active_power, na.rm = TRUE)
)
labels <- c(0, 1)
dts <- cut(pc$active_power, breaks = breaks, labels = labels)
dts_cov <- data.frame(day_night = (pc$hour >= 7 & pc$hour <= 17))
m_cov <- covlmc(dts, dts_cov, min_size = 5)
m_ctxs <- contexts(m_cov)
## get the predictive metrics for each context
lapply(m_ctxs, metrics)</pre>
```

metrics.vlmc Predictive quality metrics for VLMC

#### Description

This function computes and returns predictive quality metrics for context based models such as VLMC and VLMC with covariates.

# Usage

```
## S3 method for class 'vlmc'
metrics(model, ...)
## S3 method for class 'metrics.vlmc'
print(x, ...)
```

#### metrics.vlmc

#### Arguments

model	The context based model on which to compute predictive metrics.
	Additional parameters for predictive metrics computation.
x	A metrics.vlmc object, results of a call to metrics.vlmc()

# Details

A context based model computes transition probabilities for its contexts. Using a maximum transition probability decision rule, this can be used to predict the new state that is the more likely to follow the current one, given the context (see predict.vlmc()). The quality of these predictions is evaluated using standard metrics including:

- accuracy
- the full confusion matrix
- the area under the roc curve (AUC), considering the context based model as a (conditional) probability estimator. We use Hand and Till (2001) multiclass AUC in case of a state space with more than 2 states

# Value

An object of class metrics.vlmc with the following components:

- accuracy: the accuracy of the predictions
- conf\_mat: the confusion matrix of the predictions, with predicted values in rows and true values in columns
- auc: the AUC of the predictive model

The object has a print method that recalls basic information about the model together with the values of the components above.

### Methods (by generic)

• print(metrics.vlmc): Prints the predictive metrics of the VLMC model.

# **Extended contexts**

As explained in details in loglikelihood.vlmc() documentation and in the dedicated vignette("likelihood", package = "mixvlmc"), the first initial values of a time series do not in general have a proper context for a VLMC with a non zero order. In order to predict something meaningful for those values, we rely on the notion of extended context defined in the documents mentioned above. This follows the same logic as using loglikelihood.vlmc() with the parameter initial="extended". All vlmc functions that need to manipulate initial values with no proper context use the same approach.

#### References

David J. Hand and Robert J. Till (2001). "A Simple Generalisation of the Area Under the ROC Curve for Multiple Class Classification Problems." *Machine Learning* 45(2), p. 171–186. DOI: doi:10.1023/A:1010920819831.

# See Also

```
metrics.vlmc(), metrics.ctx_node(), contexts.vlmc(), predict.vlmc().
```

# Examples

```
pc <- powerconsumption[powerconsumption$week == 5, ]
breaks <- c(
    0,
    median(powerconsumption$active_power, na.rm = TRUE),
    max(powerconsumption$active_power, na.rm = TRUE)
)
labels <- c(0, 1)
dts <- cut(pc$active_power, breaks = breaks, labels = labels)
model <- vlmc(dts)
metrics(model)</pre>
```

```
model
```

# Logistic model of a COVLMC context

# Description

This function returns a representation of the logistic model associated to a COVLMC context from its node in the associated context tree.

# Usage

model(node, type = c("coef", "full"))

### Arguments

node	A ctx_node_covlmc object as returned by find_sequence() or contexts.covlmc()
type	specifies the model information to return, either the coefficients only (type="coef"
	default case) or the full model object (type="full")

# Details

Full model extraction is only possible if the COVLMC model what not fully trimmed (see trim.covlmc()). Notice that find\_sequence.covlmc() can produce node that are not context: in this case this function return NULL.

# Value

if node is a context, the coefficients of the logistic model (as a vector or a matrix depending on the size of the state space) or a logistic model as a R object. If node is not a context, NULL.

#### parent

#### Examples

```
pc <- powerconsumption[powerconsumption$week == 5, ]
dts <- cut(pc$active_power, breaks = c(0, quantile(pc$active_power, probs = c(0.5, 1))))
dts_cov <- data.frame(day_night = (pc$hour >= 7 & pc$hour <= 17))
m_cov <- covlmc(dts, dts_cov, min_size = 10)
vals <- states(m_cov)
node <- find_sequence(m_cov, c(vals[1], vals[1]))
node
model(node)
model(node, type = "full")</pre>
```

parent

Find the parent of a node in a context tree

#### Description

This function returns the parent node of the node represented by the node parameter. The result is NULL if node is the root node of its context tree (representing the empty sequence).

### Usage

parent(node)
## S3 method for class 'ctx\_node'
parent(node)
## S3 method for class 'ctx\_node\_cpp'
parent(node)

# Arguments

node a ctx\_node object as returned by find\_sequence()

### Details

Each node of a context tree represents a sequence. When find\_sequence() is called with success, the returned object represents the corresponding node in the context tree. Unless the original sequence is empty, this node has a parent node which is returned as a ctx\_node object by the present function. Another interpretation is that the function returns the node object associated to the sequence obtained by removing the oldest value from the original sequence.

#### Value

a ctx\_node object if node does correspond to the empty sequence or NULL when this is not the case

# Examples

```
dts <- c(0, 1, 1, 1, 0, 0, 1, 0, 1, 0)
dts_ctree <- ctx_tree(dts, min_size = 1, max_depth = 3)
ctx_00 <- find_sequence(dts_ctree, c(0, 0))
## the parent sequence/node corresponds to the 0 context
parent(ctx_00)
identical(parent(ctx_00), find_sequence(dts_ctree, c(0)))
## C++ backend
dts <- c(0, 1, 1, 1, 0, 0, 1, 0, 1, 0)
dts_ctree <- ctx_tree(dts, min_size = 1, max_depth = 3, backend = "C++")
ctx_00 <- find_sequence(dts_ctree, c(0, 0))
## the parent sequence/node corresponds to the 0 context
parent(ctx_00)
identical(parent(ctx_00), find_sequence(dts_ctree, c(0)))</pre>
```

plot.tune\_vlmc Plot the results of automatic (CO)VLMC complexity selection

### Description

This function plots the results of tune\_vlmc() or tune\_covlmc().

### Usage

```
## S3 method for class 'tune_vlmc'
plot(
    x,
    value = c("criterion", "likelihood"),
    cutoff = c("quantile", "native"),
    ...
)
## S3 method for class 'tune_covlmc'
plot(
    x,
    value = c("criterion", "likelihood"),
    cutoff = c("quantile", "native"),
    ...
)
```

# Arguments

Х	a tune_vlmc object
value	the criterion to plot (default "criterion").
cutoff	the scale used for the cut off criterion (default "quantile")
	additional parameters passed to base::plot()

### plot.tune\_vlmc

### Details

The standard plot consists in showing the evolution of the criterion used to select the model (AIC() or BIC()) as a function of the cut off criterion expressed in the quantile scale (the quantile is used by default to offer a common default behaviour between vlmc() and covlmc()). Parameters can be used to display instead the loglikelihood() of the model (by setting value="likelihood") and to use the native scale for the cut off when available (by setting cutoff="native").

### Value

the tune\_vlmc object invisibly

### Customisation

The function sets several default before calling base::plot(), namely:

- type: "l" by default to use a line representation;
- xlab: "Cut off (quantile scale)" by default, adapted to the actual scale;
- ylab: the name of the criterion or "Log likelihood".

These parameters can be overridden by specifying other values when calling the function. All parameters specified in addition to x, value and cutoff are passed to base::plot().

```
dts <- sample(as.factor(c("A", "B", "C")), 100, replace = TRUE)</pre>
tune_result <- tune_vlmc(dts)</pre>
## default plot
plot(tune_result)
## likelihood
plot(tune_result, value = "likelihood")
## parameters overriding
plot(tune_result,
 value = "likelihood",
 xlab = "Cut off", type = "b"
)
pc <- powerconsumption[powerconsumption$week %in% 10:12, ]</pre>
dts <- cut(pc$active_power, breaks = c(0, quantile(pc$active_power, probs = c(0.5, 1)))
dts_cov <- data.frame(day_night = (pc$hour >= 7 & pc$hour <= 17))</pre>
dts_best_model_tune <- tune_covlmc(dts, dts_cov, criterion = "AIC")</pre>
plot(dts_best_model_tune)
plot(dts_best_model_tune, value = "likelihood")
```

```
positions
```

# Description

This function returns the positions of the sequence represented by node in the time series used to build the context tree in which the sequence is represented. This is only possible is those positions were saved during the construction of the context tree. In positions were not saved, a call to this function produces an error.

#### Usage

```
positions(node)
## S3 method for class 'ctx_node'
positions(node)
## S3 method for class 'ctx_node_cpp'
positions(node)
```

# Arguments

node

a ctx\_node object as returned by find\_sequence()

# Details

A position of a sequence ctx in the time series x is an index value t such that the sequence ends with x[t]. Thus x[t+1] is after the context. For instance if x=c(0, 0, 1, 1) and ctx=c(0, 1) (in standard state order), then the position of ctx in x is 3.

### Value

positions of the sequence represented by node is the original time series as a integer vector

```
dts <- sample(as.factor(c("A", "B", "C")), 100, replace = TRUE)
dts_tree <- ctx_tree(dts, max_depth = 3, min_size = 5)
subseq <- find_sequence(dts_tree, factor(c("B", "A"), levels = c("A", "B", "C")))
if (!is.null(subseq)) {
    positions(subseq)
}</pre>
```

powerconsumption Individual household electric power consumption

### Description

A data set containing measurements of the electric power consumption of one household with a time resolution of 10 minutes for the full year of 2008.

#### Usage

powerconsumption

### Format

A data frame with 52704 rows and 15 variables:

month month of 2008

month\_day day of the month

**hour** hour (0 to 23)

minute starting minute of the 10 minutes period of this row

active\_power global average active power on the 10 minute period (in kilowatt)

reactive\_power global average reactive power on the 10 minute period (in kilowatt)

voltage Average voltage on the 10 minute period (in volt)

intensity global average current intensity on the 10 minute period (in ampere)

- sub\_metering\_1 energy sub-metering No. 1 (in watt-hour of active energy averaged over the 10 minute period). It corresponds to the kitchen, containing mainly a dishwasher, an oven and a microwave (hot plates are not electric but gas powered)
- sub\_metering\_2 energy sub-metering No. 2 (in watt-hour of active energy averaged over the 10 minute period). It corresponds to the laundry room, containing a washing-machine, a tumble-drier, a refrigerator and a light.
- sub\_metering\_3 energy sub-metering No. 3 (in watt-hour of active energy averaged over the 10 minute period). It corresponds to an electric water-heater and an air-conditioner.

week week number

week\_day day of the week from 1 = Sunday to 7 = Saturday

year\_day day of the year from 1 to 366 (2008 is a leap year)

date\_time Date and time in POSIXct format

# Details

This is a simplified version of the full data available on the UCI Machine Learning Repository under a Creative Commons Attribution 4.0 International (CC BY 4.0) license, and provided by Georges Hebrail and Alice Berard.

The original data have been averaged over a 10 minute time period (discarding missing data in each period). The data set contains only the measurements from year 2008.

Notice that the different variables are expressed in the adapted units. In particular, the sub-meters are measuring active energy (in watt-hour) while the global active power is expressed in kilowatt.

### Source

Individual household electric power consumption, 2012, G. Hebrail and A. Berard, UC Irvine Machine Learning repository. doi:10.24432/C58K54

<pre>predict.covlmc</pre>	Next state prediction in a discrete time series for a VLMC with covari-
	ates

#### Description

This function computes one step ahead predictions for a discrete time series based on a VLMC with covariates.

### Usage

```
## S3 method for class 'covlmc'
predict(
   object,
   newdata,
   newcov,
   type = c("raw", "probs"),
   final_pred = TRUE,
   ...
)
```

# Arguments

object	a fitted covlmc object.
newdata	a time series adapted to the covlmc object.
newcov	a data frame with the new values for the covariates.
type	character indicating the type of prediction required. The default "raw" returns actual predictions in the form of a new time series. The alternative "probs" returns a matrix of prediction probabilities (see details).
final_pred	if TRUE (default value), the predictions include a final prediction step, made by computing the context of the full time series. When FALSE this final prediction is not included.
	additional arguments.

#### predict.vlmc

#### Details

Given a time series X, at time step t, a context is computed using observations from X[1] to X[t-1] (see the dedicated section). The prediction is then the most probable state for X[t] given this logistic model of the context and the corresponding values of the covariates. The time series of predictions is returned by the function when type="raw" (default case).

When type="probs", the function returns of the probabilities of each state for X[t] as estimated by the logistic models. Those probabilities are returned as a matrix of probabilities with column names given by the state names.

# Value

A vector of predictions if type="raw" or a matrix of state probabilities if type="probs".

### **Extended contexts**

As explained in details in loglikelihood.covlmc() documentation and in the dedicated vignette("likelihood", package = "mixvlmc"), the first initial values of a time series do not in general have a proper context for a COVLMC with a non zero order. In order to predict something meaningful for those values, we rely on the notion of extended context defined in the documents mentioned above. This follows the same logic as using loglikelihood.covlmc() with the parameter initial="extended". All covlmc functions that need to manipulate initial values with no proper context use the same approach.

# Examples

```
pc <- powerconsumption[powerconsumption$week == 10, ]
dts <- cut(pc$active_power, breaks = c(0, quantile(pc$active_power, probs = c(0.2, 0.7, 1))))
dts_cov <- data.frame(day_night = (pc$hour >= 7 & pc$hour <= 17))
m_cov <- covlmc(dts, dts_cov, min_size = 5, alpha = 0.5)
dts_probs <- predict(m_cov, dts[1:144], dts_cov[1:144, , drop = FALSE], type = "probs")
dts_preds <- predict(m_cov, dts[1:144], dts_cov[1:144, , drop = FALSE],
type = "raw", final_pred = FALSE
)</pre>
```

predict.vlmc

Next state prediction in a discrete time series for a VLMC

### Description

This function computes one step ahead predictions for a discrete time series based on a VLMC.

### Usage

```
## S3 method for class 'vlmc'
predict(object, newdata, type = c("raw", "probs"), final_pred = TRUE, ...)
## S3 method for class 'vlmc_cpp'
predict(object, newdata, type = c("raw", "probs"), final_pred = TRUE, ...)
```

#### Arguments

object	a fitted vlmc object.
newdata	a time series adapted to the vlmc object.
type	character indicating the type of prediction required. The default "raw" returns actual predictions in the form of a new time series. The alternative "probs" returns a matrix of prediction probabilities (see details).
final_pred	if TRUE (default value), the predictions include a final prediction step, made by computing the context of the full time series. When FALSE this final prediction is not included.
	additional arguments.

# Details

Given a time series X, at time step t, a context is computed using observations from X[1] to X[t-1] (see the dedicated section). The prediction is then the most probable state for X[t] given this contexts. Ties are broken according to the natural order in the state space, favouring "small" values. The time series of predictions is returned by the function when type="raw" (default case).

When type="probs", each X[t] is associated to the conditional probabilities of the next state given the context. Those probabilities are returned as a matrix of probabilities with column names given by the state names.

### Value

A vector of predictions if type="raw" or a matrix of state probabilities if type="probs".

# **Extended contexts**

As explained in details in loglikelihood.vlmc() documentation and in the dedicated vignette("likelihood", package = "mixvlmc"), the first initial values of a time series do not in general have a proper context for a VLMC with a non zero order. In order to predict something meaningful for those values, we rely on the notion of extended context defined in the documents mentioned above. This follows the same logic as using loglikelihood.vlmc() with the parameter initial="extended". All vlmc functions that need to manipulate initial values with no proper context use the same approach.

```
pc <- powerconsumption[powerconsumption$week == 5, ]
dts <- cut(pc$active_power, breaks = c(0, quantile(pc$active_power, probs = c(0.25, 0.5, 0.75, 1))))
model <- vlmc(dts, min_size = 5)
predict(model, dts[1:5])
predict(model, dts[1:5], "probs")
## C++ backend
pc <- powerconsumption[powerconsumption$week == 5, ]
dts <- cut(pc$active_power, breaks = c(0, quantile(pc$active_power, probs = c(0.25, 0.5, 0.75, 1))))
model <- vlmc(dts, min_size = 5, backend = "C++")
predict(model, dts[1:5], "probs")</pre>
```

print.contexts Print a context list

# Description

This function prints a list of contexts i.e. a contexts object listing ctx\_node objects.

# Usage

```
## S3 method for class 'contexts'
print(x, reverse = TRUE, ...)
```

# Arguments

х	the contexts object to print
reverse	specifies whether the contexts should be reported in temporal order (FALSE, de- fault value) or in reverse temporal order (TRUE). If the parameter is not specified, the contexts are displayed in order specified by the call to contexts() used to build the context list.
	additional arguments for the print function.

# Value

the x object, invisibly

# See Also

contexts()

# Examples

```
dts <- c("A", "B", "C", "A", "A", "B", "B", "C", "C", "A")
dts_tree <- ctx_tree(dts, max_depth = 3)
print(contexts(dts_tree))</pre>
```

```
prune
```

Prune a Variable Length Markov Chain (VLMC)

# Description

This function prunes a VLMC.

prune

# Usage

```
prune(vlmc, alpha = 0.05, cutoff = NULL, ...)
## S3 method for class 'vlmc'
prune(vlmc, alpha = 0.05, cutoff = NULL, ...)
## S3 method for class 'vlmc_cpp'
prune(vlmc, alpha = 0.05, cutoff = NULL, ...)
```

# Arguments

vlmc	a fitted VLMC model.
alpha	number in (0,1] (default: 0.05) cut off value in quantile scale for pruning.
cutoff	positive number: cut off value in native (log likelihood ratio) scale for pruning. Defaults to the value obtained from alpha. Takes precedence over alpha if specified.
	additional arguments for the prune function.

# Details

In general, pruning a VLMC is more efficient than constructing two VLMC (the base one and pruned one). Up to numerical instabilities, building a VLMC with a a cut off and then pruning it with a b cut off (with a>b) should produce the same VLMC than building directly the VLMC with a b cut off. Interesting cut off values can be extracted from a VLMC using the cutoff() function.

As automated model selection is provided by  $tune_vlmc()$ , the direct use of cutoff should be reserved to advanced exploration of the set of trees that can be obtained from a complex one, e.g. to implement model selection techniques that are not provided by  $tune_vlmc()$ .

### Value

a pruned VLMC

### See Also

cutoff() and tune\_vlmc()

# Examples

```
pc <- powerconsumption[powerconsumption$week == 5, ]
dts <- cut(pc$active_power, breaks = c(0, quantile(pc$active_power, probs = c(0.25, 0.5, 0.75, 1))))
base_model <- vlmc(dts, alpha = 0.1)
model_cuts <- cutoff(base_model)
pruned_model <- prune(base_model, model_cuts[3])
draw(pruned_model)
direct_simple <- vlmc(dts, alpha = model_cuts[3])
draw(direct_simple)
# pruned_model and direct_simple should be identical
all.equal(pruned_model, direct_simple)</pre>
```

prune.covlmc

### Description

This function prunes a vlmc with covariates. This model must have been estimated with keep\_data=TRUE to enable the pruning.

# Usage

## S3 method for class 'covlmc'
prune(vlmc, alpha = 0.05, cutoff = NULL, ...)

# Arguments

vlmc	a fitted VLMC model with covariates.
alpha	number in $(0,1)$ (default: 0.05) cutoff value in quantile scale for pruning.
cutoff	not supported by the vlmc with covariates.
	additional arguments for the prune function.

#### Details

Post pruning a VLMC with covariates is not as straightforward as the same procedure applied to vlmc() (see cutoff.vlmc() and prune.vlmc()). For efficiency reasons, covlmc() estimates only the logistic models that are considered useful for a given set construction parameters. With a more aggressive pruning threshold, some contexts become leaves of the context tree and new logistic models must be estimated. Thus the pruning opportunities given by cutoff.covlmc() are only a subset of interesting cut offs for a given covlmc.

Nevertheless, covlmc share with vlmc() the principle that post pruning a covlmc should give the same model as building directly the covlmc, provided that the post pruning alpha is smaller than the alpha used to build the initial model.

### Value

a pruned covlmc.

```
pc <- powerconsumption[powerconsumption$week == 5, ]
dts <- cut(pc$active_power, breaks = c(0, quantile(pc$active_power, probs = c(0.5, 1))))
dts_cov <- data.frame(day_night = (pc$hour >= 7 & pc$hour <= 17))
m_cov <- covlmc(dts, dts_cov, min_size = 5, keep_data = TRUE)
draw(m_cov)
m_cov_cuts <- cutoff(m_cov)
p_cov <- prune(m_cov, m_cov_cuts[1])
draw(p_cov)</pre>
```

rev.ctx\_node

#### Description

This function reverses the order in which the sequence represented by the ctx\_node parameter will be reported in other functions, mainly as\_sequence().

# Usage

## S3 method for class 'ctx\_node'
rev(x)

### Arguments

х

a ctx\_node object as returned by find\_sequence()

# Value

a ctx\_node using the opposite ordering convention as the parameter of the function

#### See Also

is\_reversed()

# Examples

```
dts <- c("A", "B", "C", "A", "A", "B", "B", "C", "C", "A")
dts_tree <- ctx_tree(dts, max_depth = 3)
res <- find_sequence(dts_tree, c("A", "B"))
print(res)
r_res <- rev(res)
print(r_res)
as_sequence(r_res)</pre>
```

simulate.covlmc Simulate a discrete time series for a covlmc

# Description

This function simulates a time series from the distribution estimated by the given covlmc object.

#### Usage

```
## S3 method for class 'covlmc'
simulate(object, nsim = 1, seed = NULL, covariate, init = NULL, ...)
```
## simulate.covlmc

#### Arguments

object	a fitted covlmc object.
nsim	length of the simulated time series (defaults to 1).
seed	an optional random seed (see the dedicated section).
covariate	values of the covariates.
init	an optional initial sequence for the time series.
	additional arguments.

## Details

A VLMC with covariates model needs covariates to compute its transition probabilities. The covariates must be submitted as a data frame using the covariate argument. In addition, the time series can be initiated by a fixed sequence specified via the init parameter.

# Value

a simulated discrete time series of the same type as the one used to build the covlmc with a seed attribute (see the Random seed section). The results has also the dts class to hide the seed attribute when using print or similar function.

# **Extended contexts**

As explained in details in loglikelihood.covlmc() documentation and in the dedicated vignette("likelihood", package = "mixvlmc"), the first initial values of a time series do not in general have a proper context for a COVLMC with a non zero order. In order to simulate something meaningful for those values, we rely on the notion of extended context defined in the documents mentioned above. This follows the same logic as using loglikelihood.covlmc() with the parameter initial="extended". All covlmc functions that need to manipulate initial values with no proper context use the same approach.

#### **Random seed**

This function reproduce the behaviour of stats::simulate(). If seed is NULL the function does not change the random generator state and returns the value of .Random.seed as a seed attribute in the return value. This can be used to reproduce exactly the simulation results by setting .Random.seed to this value. Notice that if the random seed has not be initialised by R so far, the function issues a call to runif(1) to perform this initialisation (as is done in stats::simulate()).

It seed is an integer, it is used in a call to set.seed() before the simulation takes place. The integer is saved as a seed attribute in the return value. The integer seed is completed by an attribute kind which contains the value as.list([RNGkind()]) exactly as with stats::simulate(). The random generator state is reset to its original value at the end of the call.

## See Also

stats::simulate() for details and examples on the random number generator setting

# Examples

```
pc <- powerconsumption[powerconsumption$week == 5, ]
dts <- cut(pc$active_power, breaks = c(0, quantile(pc$active_power, probs = c(0.5, 1))))
dts_cov <- data.frame(day_night = (pc$hour >= 7 & pc$hour <= 17))
m_cov <- covlmc(dts, dts_cov, min_size = 5)
# new week with day light from 6:00 to 18:00
new_cov <- data.frame(day_night = rep(c(rep(FALSE, 59), rep(TRUE, 121), rep(FALSE, 60)), times = 7))
new_dts <- simulate(m_cov, nrow(new_cov), seed = 0, covariate = new_cov, init = dts[1:10])</pre>
```

simulate.vlmc Simulate a discrete time series for a vlmc

#### Description

This function simulates a time series from the distribution estimated by the given vlmc object.

## Usage

```
## S3 method for class 'vlmc'
simulate(object, nsim = 1L, seed = NULL, init = NULL, burnin = 0L, ...)
```

## Arguments

object	a fitted vlmc object.
nsim	length of the simulated time series (defaults to 1).
seed	an optional random seed (see the dedicated section).
init	an optional initial sequence for the time series.
burnin	number of initial observations to discard or "auto" (see the dedicated section).
	additional arguments.

## Details

The time series can be initiated by a fixed sequence specified via the init parameter.

# Value

a simulated discrete time series of the same type as the one used to build the vlmc with a seed attribute (see the Random seed section). The results has also the dts class to hide the seed attribute when using print or similar function.

#### simulate.vlmc

#### Burn in (Warm up) period

When using a VLMC for simulation purposes, we are generally interested in the stationary distribution of the corresponding Markov chain. To reduce the dependence of the samples from the initial values and get closer to this stationary distribution (if it exists), it is recommended to discard the first samples which are produced in a so-called "burn in" (or "warm up") period. The burn in parameter can be used to implement this approach. The VLMC is used to produce a sample of size burn + nsim but the first burn in values are discarded. Notice that this burn in values can be partially given by the init parameter if it is specified.

If burnin is set to "auto", the burnin period is set to 64 \* context\_number(object), following the heuristic proposed in Mächler and Bühlmann (2004).

#### **Random seed**

This function reproduce the behaviour of stats::simulate(). If seed is NULL the function does not change the random generator state and returns the value of .Random.seed as a seed attribute in the return value. This can be used to reproduce exactly the simulation results by setting .Random.seed to this value. Notice that if the random seed has not be initialised by R so far, the function issues a call to runif(1) to perform this initialisation (as is done in stats::simulate()).

It seed is an integer, it is used in a call to set.seed() before the simulation takes place. The integer is saved as a seed attribute in the return value. The integer seed is completed by an attribute kind which contains the value as.list([RNGkind()]) exactly as with stats::simulate(). The random generator state is reset to its original value at the end of the call.

## **Extended contexts**

As explained in details in loglikelihood.vlmc() documentation and in the dedicated vignette("likelihood", package = "mixvlmc"), the first initial values of a time series do not in general have a proper context for a VLMC with a non zero order. In order to simulate something meaningful for those values when init is not provided, we rely on the notion of extended context defined in the documents mentioned above. This follows the same logic as using loglikelihood.vlmc() with the parameter initial="extended". All vlmc functions that need to manipulate initial values with no proper context use the same approach.

#### References

Mächler, M. and Bühlmann, P. (2004) "Variable Length Markov Chains: Methodology, Computing, and Software" Journal of Computational and Graphical Statistics, 13 (2), 435-455, doi:10.1198/1061860043524

#### See Also

stats::simulate() for details and examples on the random number generator setting

## Examples

```
pc <- powerconsumption[powerconsumption$week == 5, ]
dts <- cut(pc$active_power, breaks = c(0, quantile(pc$active_power, probs = c(0.25, 0.5, 0.75, 1))))
model <- vlmc(dts, min_size = 5)
new_dts <- simulate(model, 500, seed = 0)</pre>
```

```
new_dts_2 <- simulate(model, 500, seed = 0, init = dts[1:5])
new_dts_3 <- simulate(model, 500, seed = 0, burnin = 500)</pre>
```

simulate.vlmc\_cpp Simulate a discrete time series for a vlmc

# Description

This function simulates a time series from the distribution estimated by the given vlmc object.

## Usage

```
## S3 method for class 'vlmc_cpp'
simulate(
   object,
   nsim = 1,
   seed = NULL,
   init = NULL,
   burnin = 0L,
   sample = c("fast", "slow", "R"),
   ...
)
```

# Arguments

object	a fitted vlmc object.
nsim	length of the simulated time series (defaults to 1).
seed	an optional random seed (see the dedicated section).
init	an optional initial sequence for the time series.
burnin	number of initial observations to discard or "auto" (see the dedicated section).
sample	<pre>specifies which implementation of base::sample() to use. See the dedicated section.</pre>
	additional arguments.

# Details

The time series can be initiated by a fixed sequence specified via the init parameter.

## Value

a simulated discrete time series of the same type as the one used to build the vlmc with a seed attribute (see the Random seed section). The results has also the dts class to hide the seed attribute when using print or similar function.

#### sampling method

The R backend for vlmc() uses base::sample() to generate samples for each context. Internally, this function sorts the probabilities of each state in decreasing probability order (among other things), which is not needed in our case. The C++ backend can be used with three different implementations:

- sample="fast" uses a dedicated C++ implementation adapted to the data structures used internally. In general, the simulated time series obtained with this implementation will be different from the one generated with the R backend, even using the same seed.
- sample="slow" uses another C++ implementation that mimics base::sample() in order to maximize the chance to provide identical simulation results regardless of the backend (when using the same random seed). This process is not perfect as we use the std::lib sort algorithm which is not guaranteed to give identical results as the ones of R internal 'revsort'.
- sample="R" uses direct calls to base::sample(). Results are guaranteed to be identical between the two backends, but at the price of higher running time.

## Burn in (Warm up) period

When using a VLMC for simulation purposes, we are generally interested in the stationary distribution of the corresponding Markov chain. To reduce the dependence of the samples from the initial values and get closer to this stationary distribution (if it exists), it is recommended to discard the first samples which are produced in a so-called "burn in" (or "warm up") period. The burnin parameter can be used to implement this approach. The VLMC is used to produce a sample of size burnin + nsim but the first burnin values are discarded. Notice that this burn in values can be partially given by the init parameter if it is specified.

If burnin is set to "auto", the burnin period is set to 64 \* context\_number(object), following the heuristic proposed in Mächler and Bühlmann (2004).

## **Random seed**

This function reproduce the behaviour of stats::simulate(). If seed is NULL the function does not change the random generator state and returns the value of .Random.seed as a seed attribute in the return value. This can be used to reproduce exactly the simulation results by setting .Random.seed to this value. Notice that if the random seed has not be initialised by R so far, the function issues a call to runif(1) to perform this initialisation (as is done in stats::simulate()).

It seed is an integer, it is used in a call to set.seed() before the simulation takes place. The integer is saved as a seed attribute in the return value. The integer seed is completed by an attribute kind which contains the value as.list([RNGkind()]) exactly as with stats::simulate(). The random generator state is reset to its original value at the end of the call.

## **Extended contexts**

As explained in details in loglikelihood.vlmc() documentation and in the dedicated vignette("likelihood", package = "mixvlmc"), the first initial values of a time series do not in general have a proper context for a VLMC with a non zero order. In order to simulate something meaningful for those values when init is not provided, we rely on the notion of extended context defined in the documents

mentioned above. This follows the same logic as using loglikelihood.vlmc() with the parameter initial="extended". All vlmc functions that need to manipulate initial values with no proper context use the same approach.

# References

Mächler, M. and Bühlmann, P. (2004) "Variable Length Markov Chains: Methodology, Computing, and Software" Journal of Computational and Graphical Statistics, 13 (2), 435-455, doi:10.1198/1061860043524

## See Also

stats::simulate() for details and examples on the random number generator setting

## Examples

```
pc <- powerconsumption[powerconsumption$week == 5, ]
dts <- cut(pc$active_power, breaks = c(0, quantile(pc$active_power, probs = c(0.25, 0.5, 0.75, 1))))
model <- vlmc(dts, min_size = 5)
new_dts <- simulate(model, 500, seed = 0)
new_dts_2 <- simulate(model, 500, seed = 0, init = dts[1:5])
new_dts_3 <- simulate(model, 500, seed = 0, burnin = 500)</pre>
```

states

State space of a context tree

#### Description

This function returns the state space of a context tree.

#### Usage

states(ct)

#### Arguments

ct a context tree.

#### Value

the state space of the context tree.

## Examples

```
dts <- c(0, 1, 1, 1, 0, 0, 1, 0, 1, 0)
dts_ctree <- ctx_tree(dts, min_size = 1, max_depth = 2)
## should be c(0, 1)
states(dts_ctree)</pre>
```

trim

## Description

This function returns a trimmed context tree from which match positions have been removed.

# Usage

trim(ct, ...)

## Arguments

ct	a context tree.
	additional arguments for the trim function.

# Value

a trimmed context tree.

## Examples

```
## context tree trimming
dts <- sample(as.factor(c("A", "B", "C")), 1000, replace = TRUE)
dts_tree <- ctx_tree(dts, max_depth = 10, min_size = 5, keep_position = TRUE)
print(object.size(dts_tree))
dts_tree <- trim(dts_tree)
print(object.size(dts_tree))
```

trim.covlmc Trim a COVLMC

## Description

This function returns a trimmed COVLMC from which cached data have been removed.

## Usage

## S3 method for class 'covlmc'
trim(ct, keep\_model = FALSE, ...)

# Arguments

ct	a context tree.
keep_model	specifies whether to keep the internal models (or not)
	additional arguments for the trim function.

# Details

Called with keep\_model set to FALSE (default case), the trimming is maximal and reduces further usability of the model. In particular loglikelihood.covlmc() cannot be used for new data, contexts.covlmc() do not support model extraction, and simulate.covlmc(), metrics.covlmc() and prune.covlmc() cannot be used at all.

Called with keep\_model set to TRUE, the trimming process is less complete. In particular internal models are simplified using butcher::butcher() and some additional minor reductions. This saves less memory but enables the use of loglikelihood.covlmc() for new data as well as the use of simulate.covlmc().

# Value

a trimmed context tree.

# See Also

tune\_covlmc()

## Examples

```
pc <- powerconsumption[powerconsumption$week %in% 5:7, ]
dts <- cut(pc$active_power, breaks = c(0, quantile(pc$active_power, probs = c(0.5, 1))))
dts_cov <- data.frame(day_night = (pc$hour >= 7 & pc$hour <= 17))
m_cov <- covlmc(dts, dts_cov, min_size = 10, keep_data = TRUE)
print(object.size(m_cov), units = "Mb")
t_m_cov_model <- trim(m_cov, keep_model = TRUE)
print(object.size(t_m_cov_model), units = "Mb")
t_m_cov <- trim(m_cov)
print(object.size(t_m_cov), units = "Mb")</pre>
```

trim.vlmc	This function returns a trimmed VLMC from which match positions
	have been removed.

# Description

This function returns a trimmed context tree from which match positions have been removed.

#### Usage

```
## S3 method for class 'vlmc'
trim(ct, ...)
```

## Arguments

ct	a VLMC.
	additional arguments for the trim function.

trim.vlmc\_cpp

#### Value

a trimmed VLMC

# Examples

```
## VLMC trimming is generally useless unless match positions were kept
pc <- powerconsumption[powerconsumption$week %in% 5:6, ]
dts <- cut(pc$active_power, breaks = 4)
model <- vlmc(dts, keep_match = TRUE)
print(object.size(model))
model <- trim(model)
## memory use should be reduced
print(object.size(model))
nm_model <- vlmc(dts)
print(object.size(nm_model))
nm_model <- trim(nm_model)
## no effect when match positions are not kept
print(object.size(nm_model))</pre>
```

trim.vlmc\_cpp

This function returns a trimmed VLMC from which match positions have been removed.

# Description

This function returns a trimmed context tree from which match positions have been removed.

# Usage

```
## S3 method for class 'vlmc_cpp'
trim(ct, ...)
```

# Arguments

ct	a VLMC.
	additional arguments for the trim function.

# Details

Trimming in the C++ backend is done directly in the Rcpp managed memory and cannot be detected at R level using e.g. utils::object.size().

## Value

a trimmed VLMC

# Examples

```
## VLMC trimming is generally useless unless match positions were kept
pc <- powerconsumption[powerconsumption$week %in% 5:6, ]
dts <- cut(pc$active_power, breaks = 4)
model <- vlmc(dts, backend = "C++", keep_match = TRUE)
model <- trim(model)</pre>
```

tune_	_covlmc	2

Fit an optimal Variable Length Markov Chain with Covariates (coVLMC)

# Description

This function fits a Variable Length Markov Chain with Covariates (coVLMC) to a discrete time series coupled with a time series of covariates by optimizing an information criterion (BIC or AIC).

## Usage

```
tune_covlmc(
    x,
    covariate,
    criterion = c("BIC", "AIC"),
    initial = c("truncated", "specific", "extended"),
    alpha_init = NULL,
    min_size = 5,
    max_depth = 100,
    verbose = 0,
    save = c("best", "initial", "all"),
    trimming = c("full", "partial", "none"),
    best_trimming = c("none", "partial", "full")
)
```

# Arguments

х	a discrete time series; can be numeric, character, factor and logical.
covariate	a data frame of covariates.
criterion	criterion used to select the best model. Either "BIC" (default) or "AIC" (see details).
initial	specifies the likelihood function, more precisely the way the first few observa- tions for which contexts cannot be calculated are integrated in the likelihood. See loglikelihood() for details.
alpha_init	if non NULL used as the initial cut off parameter (in quantile scale) to build the initial VLMC
min_size	integer >= 1 (default: 5). Tune the minimum number of observations for a context in the growing phase of the context tree (see $covlmc()$ for details).

max_depth	integer >= 1 (default: 100). Longest context considered in growing phase of the initial context tree (see details).
verbose	integer $\geq 0$ (default: 0). Verbosity level of the pruning process.
save	specify which BIC models are saved during the pruning process. The default value "best" asks the function to keep only the best model according to the criterion. When save="initial" the function keeps <i>in addition</i> the initial (complex) model which is then pruned during the selection process. When save="all", the function returns all the models considered during the selection process. See details for memory occupation.
trimming	specify the type of trimming used when saving the intermediate models, see details.
best_trimming	specify the type of trimming used when saving the best model and the initial one (see details).

## Details

This function automates the process of fitting a large coVLMC to a discrete time series with covlmc() and of pruning the tree (with cutoff() and prune()) to get an optimal with respect to an information criterion. To avoid missing long term dependencies, the function uses the max\_depth parameter as an initial guess but then relies on an automatic increase of the value to make sure the initial context tree is only limited by the min\_size parameter. The initial value of the alpha parameter of covlmc() is also set to a conservative value (0.5) to avoid prior simplification of the context tree. This can be overridden by setting the alpha\_init parameter to a more adapted value.

Once the initial coVLMC is obtained, the cutoff() and prune() functions are used to build all the coVLMC models that could be generated using smaller values of the alpha parameter. The best model is selected from this collection, including the initial complex tree, as the one that minimizes the chosen information criterion.

#### Value

a list with the following components:

- best\_model: the optimal COVLMC
- criterion: the criterion used to select the optimal VLMC
- initial: the likelihood function used to select the optimal VLMC
- results: a data frame with details about the pruning process
- saved\_models: a list of intermediate COVLMCs if save="initial" or save="all". It contains an initial component with the large coVLMC obtained first and an all component with a list of all the *other* coVLMC obtained by pruning the initial one.

#### Memory occupation

covlmc objects tend to be large and saving all the models during the search for the optimal model can lead to an unreasonable use of memory. To avoid this problem, models are kept in trimmed form only using trim.covlmc() with keep\_model=FALSE. Both the initial model and the best one are saved untrimmed. This default behaviour corresponds to trimming="full". Setting

trimming="partial" asks the function to use keep\_model=TRUE in trim.covlmc() for intermediate models. Finally, trimming="none" turns off trimming, which is discouraged expected for small data sets.

In parallel processing contexts (e.g. using foreach::%dopar%), the memory occupation of the results can become very large as models tend to keep environments attached to the formulas. In this situation, it is highly recommended to trim all saved models, including the best one and the initial one. This can be done via the best\_trimming parameter whose possible values are identical to the ones of trimming.

## See Also

covlmc(), cutoff() and prune()

## Examples

```
pc <- powerconsumption[powerconsumption$week %in% 6:7, ]
dts <- cut(pc$active_power, breaks = c(0, quantile(pc$active_power, probs = c(0.5, 1))))
dts_cov <- data.frame(day_night = (pc$hour >= 7 & pc$hour <= 17))
dts_best_model_tune <- tune_covlmc(dts, dts_cov)
draw(as_covlmc(dts_best_model_tune))</pre>
```

tune\_vlmc

```
Fit an optimal Variable Length Markov Chain (VLMC)
```

## Description

This function fits a Variable Length Markov Chain (VLMC) to a discrete time series by optimizing an information criterion (BIC or AIC).

## Usage

```
tune_vlmc(
    x,
    criterion = c("BIC", "AIC"),
    initial = c("truncated", "specific", "extended"),
    alpha_init = NULL,
    cutoff_init = NULL,
    min_size = 2L,
    max_depth = 100L,
    backend = getOption("mixvlmc.backend", "R"),
    verbose = 0,
    save = c("best", "initial", "all")
)
```

## tune\_vlmc

#### Arguments

x	a discrete time series; can be numeric, character, factor and logical.
criterion	criterion used to select the best model. Either "BIC" (default) or "AIC" (see details).
initial	specifies the likelihood function, more precisely the way the first few observa- tions for which contexts cannot be calculated are integrated in the likelihood. Default to "truncated". See loglikelihood() for details.
alpha_init	if non NULL used as the initial cut off parameter (in quantile scale) to build the initial VLMC
cutoff_init	if non NULL used as the initial cut off parameter to build the initial VLMC. Takes precedence over alpha_init if specified.
min_size	integer >= 1 (default: 2). Minimum number of observations for a context in the growing phase of the initial context tree.
max_depth	integer >= 1 (default: 100). Longest context considered in growing phase of the initial context tree (see details).
backend	backend "R" or "C++" (default: as specified by the "mixvlmc.backend" option). Specifies the implementation used to represent the context tree and to built it. See vlmc() for details.
verbose	integer $\geq 0$ (default: 0). Verbosity level of the pruning process.
save	specify which BIC models are saved during the pruning process. The default value "best" asks the function to keep only the best model according to the criterion. When save="initial" the function keeps <i>in addition</i> the initial (complex) model which is then pruned during the selection process. When save="all", the function returns all the models considered during the selection process.

## Details

This function automates the process of fitting a large VLMC to a discrete time series with vlmc() and of pruning the tree (with cutoff() and prune()) to get an optimal with respect to an information criterion. To avoid missing long term dependencies, the function uses the max\_depth parameter as an initial guess but then relies on an automatic increase of the value to make sure the initial context tree is only limited by the min\_size parameter. The initial value of the cutoff parameter of vlmc() is also set to conservative values (depending on the criterion) to avoid prior simplification of the context tree. This default value can be overridden using the cutoff\_init or alpha\_init parameter.

Once the initial VLMC is obtained, the cutoff() and prune() functions are used to build all the VLMC models that could be generated using larger values of the initial cut off parameter. The best model is selected from this collection, including the initial complex tree, as the one that minimizes the chosen information criterion.

# Value

a list with the following components:

• best\_model: the optimal VLMC

- criterion: the criterion used to select the optimal VLMC
- initial: the likelihood function used to select the optimal VLMC
- results: a data frame with details about the pruning process
- saved\_models: a list of intermediate VLMCs if save="initial" or save="all". It contains an initial component with the large VLMC obtained first and an all component with a list of all the *other* VLMC obtained by pruning the initial one.

## See Also

```
vlmc(), cutoff() and prune()
```

# Examples

```
dts <- sample(as.factor(c("A", "B", "C")), 100, replace = TRUE)
tune_result <- tune_vlmc(dts)
draw(tune_result$best_model)</pre>
```

```
vlmc
```

Fit a Variable Length Markov Chain (VLMC)

## Description

This function fits a Variable Length Markov Chain (VLMC) to a discrete time series.

## Usage

```
vlmc(
    x,
    alpha = 0.05,
    cutoff = NULL,
    min_size = 2L,
    max_depth = 100L,
    prune = TRUE,
    keep_match = FALSE,
    backend = getOption("mixvlmc.backend", "R")
)
```

# Arguments

x	a discrete time series; can be numeric, character, factor or logical.
alpha	number in $(0,1]$ (default: 0.05) cut off value in quantile scale in the pruning phase.
cutoff	non negative number: cut off value in native (likelihood ratio) scale in the prun- ing phase. Defaults to the value obtained from alpha. Takes precedence over alpha is specified.

min_size	integer $>= 1$ (default: 2). Minimum number of observations for a context in the growing phase of the context tree.
max_depth	integer >= 1 (default: 100). Longest context considered in growing phase of the context tree.
prune	logical: specify whether the context tree should be pruned (default behaviour).
keep_match	logical: specify whether to keep the context matches (default to FALSE)
backend	"R" or "C++" (default: as specified by the "mixvlmc.backend" option). Specifies the implementation used to represent the context tree and to built it. See details.

#### Details

The VLMC is built using Bühlmann and Wyner's algorithm which consists in fitting a context tree (see ctx\_tree()) to a time series and then pruning it in such as way that the conditional distribution of the next state of the time series given the context is significantly different from the distribution given a truncated version of the context.

The construction of the context tree is controlled by min\_size and max\_depth, exactly as in ctx\_tree(). Significativity is measured using a likelihood ratio test (threshold can be specified in terms of the ratio itself with cutoff) or in quantile scale with alpha.

Pruning can be postponed by setting prune=FALSE. Using a combination of cutoff() and prune(), the complexity of the VLMC can then be adjusted. Any VLMC model can be pruned after construction, prune=FALSE is a convenience parameter to avoid setting alpha=1 (which essentially prevents any pruning). Automated model selection is provided by tune\_vlmc().

## Value

a fitted vlmc model.

## **Back ends**

Two back ends are available to compute context trees:

- the "R" back end represents the tree in pure R data structures (nested lists) that be easily processed further in pure R (C++ helper functions are used to speed up the construction).
- the "C++" back end represents the tree with C++ classes. This back end is considered experimental. The tree is built with an optimised suffix tree algorithm which speeds up the construction by at least a factor 10 in standard settings. As the tree is kept outside of R direct reach, context trees built with the C++ back end must be restored after a saveRDS()/readRDS() sequence. This is done automatically by recomputing completely the context tree.

# References

Bühlmann, P. and Wyner, A. J. (1999), "Variable length Markov chains. Ann. Statist." 27 (2) 480-513 doi:10.1214/aos/1018031204

# See Also

cutoff(), prune() and tune\_vlmc()

# Examples

```
pc <- powerconsumption[powerconsumption$week == 5, ]
dts <- cut(pc$active_power,
    breaks = c(0, quantile(pc$active_power, probs = c(0.25, 0.5, 0.75, 1)))
)
model <- vlmc(dts)
draw(model)
depth(model)
## reduce the detph of the model
shallow_model <- vlmc(dts, max_depth = 3)
draw(shallow_model, prob = FALSE)
## improve probability estimates
robust_model <- vlmc(dts, min_size = 25)
draw(robust_model, prob = FALSE) ## show the frequencies
draw(robust_model)</pre>
```

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