

# Package ‘mgwrsar’

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**Type** Package

**Title** GWR, Mixed GWR and Multiscale GWR with Spatial Autocorrelation

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**Description**

Functions for computing (Mixed and Multiscale) Geographically Weighted Regression with spatial autocorrelation, Geniaux and Martinetti (2017) <[doi:10.1016/j.regsciurbeco.2017.04.001](https://doi.org/10.1016/j.regsciurbeco.2017.04.001)>.

**License** GPL (>= 2)

**Depends** R (>= 3.5.0), Rcpp, sp, leaflet, Matrix

**Imports** ggplot2, sf, knitr, methods, doParallel, foreach, htmltools, nabor, mapview, microbenchmark, rlang, dplyr, gridExtra, grid, mboost, mgcv, caret, stringr, SMUT

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**VignetteBuilder** R.rsp

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**atds\_gwr***atds\_gwr Top-Down Scaling approach of GWR***Description**

This function performs a Geographically Weighted Regression (GWR) using a top-down scaling approach, adjusting GWR coefficients with a progressively decreasing bandwidth as long as the AICc criterion improves.

**Usage**

```
atds_gwr(formula,data,coords,kernels='triangle',fixed_vars=NULL,
control_tds=list(nns=30),control=list(adaptive=TRUE,verbose=FALSE))
```

**Arguments**

formula	a formula.
data	a dataframe.
coords	default NULL, a dataframe or a matrix with coordinates
kernels	A vector containing the kernel types. Possible types: triangle ("triangle"), bisquare ("bisq"), tricube ("tcub"), epanechnikov ("epane").
fixed_vars	a vector with the names of spatially constant coefficient for mixed model. All other variables present in formula are supposed to be spatially varying. If empty or NULL (default), all variables in formula are supposed to be spatially varying.

control\_tds      list of extra control arguments for tds\_mgwr model - see tds\_gwr Help  
 control          list of extra control arguments for MGWRSAR wrapper - see MGWRSAR Help

## See Also

`tds_mgwr`, `gwr_multiscale`, `MGWRSAR`, `bandwidths_mgwrsar`, `summary_mgwrsar`.

`coef,mgwrsar-method`      *coeff for mgwrsar model*

## Description

`coef` for `mgwrsar` model

## Usage

```
## S4 method for signature 'mgwrsar'
coef(object, ...)
```

## Arguments

`object`      A model of class `mgwrsar-class`.  
`...`          `coef` parameters forwarded.

## Value

A named list with a matrix of varying coefficients and a vector or non varying coefficients.

`find_TP`      *Search of a suitable set of target points. `find_TP` is a wrapper function that identifies a set of target points based on spatial smoothed OLS residuals.*

## Description

Search of a suitable set of target points. `find_TP` is a wrapper function that identifies a set of target points based on spatial smoothed OLS residuals.

## Usage

```
find_TP(formula, data, coords, kt, ks=16, Wtp=NULL, type='residuals',
model_residuals=NULL, verbose=0, prev_TP=NULL, nTP=NULL)
```

## Arguments

formula	a formula
data	a dataframe or a spatial dataframe (SP package)
coords	a dataframe or a matrix with coordinates, not required if data is a spatial dataframe
kt	the minimum number of first neighbors with lower (resp.higer) absolute value of the smoothed residuals.
ks	the number of first neighbors for computing the smoothed residuals, default 16.
Wtp	a precomputed matrix of weights, default NULL.
type	method for choosing TP, could be 'residuals', ' kdtree','random', default 'residuals'
model_residuals	(optional) a vector of residuals.
verbose	verbose mode, default FALSE.
prev_TP	index of already used TP (version length(kt)>1), default NULL.
nTP	numbeer of target points for random choice of target points, default NULL.

## Details

*find\_TP* is a wrapper function that identifies a set of target points, based on spatial smoothed residuals by default. If no vector of residuals are provided, OLS residuals are computed. The function first computes the smooth of model residuals using a Shepard's kernel with ks neighbors (default 16). Then it identifies local maxima (resp. minima) that fits the requirement of having at least kt neighbors with lower (resp.higer) absolute value of the smoothed residuals. As kt increases the number of target points decreases.

## Value

*find\_TP* returns an index vector of Target Points set.

## Examples

```
library(mgwrssar)
## loading data example
data(mydata)
coords=as.matrix(mydata[,c("x","y")])
TP=find_TP(formula = 'Y_gwr~X1+X2+X3', data =mydata,coords=coords,kt=6,
type='residuals')
# only 60 targets points are used
length(TP)

model_GWR_tp<-MGWRSSAR(formula = 'Y_gwr~X1+X2+X3', data = mydata,
coords=coords, fixed_vars=NULL,kernels=c('gauss'), H=0.03, Model = 'GWR',
control=list(SE=TRUE,TP=TP,ks=12))
summary(model_GWR_tp@Betav)
```

---

fitted,mgwrsar-method *fitted for mgwrsar model*

---

**Description**

fitted for mgwrsar model

**Usage**

```
## S4 method for signature 'mgwrsar'  
fitted(object, ...)
```

**Arguments**

object	A model of class <a href="#">mgwrsar-class</a> .
...	fitted parameters forwarded.

**Value**

A vector of fitted values.

---

golden\_search\_bandwidth

*golden\_search\_bandwidth to be documented*

---

**Description**

golden\_search\_bandwidth to be documented

**Usage**

```
golden_search_bandwidth(formula,H2=NULL,data, coords, fixed_vars,  
kernels, Model, control,lower.bound, upper.bound,tolerance=0.000001)
```

**Arguments**

formula	to be documented
H2	to be documented
data	to be documented
coords	to be documented
fixed_vars	to be documented
kernels	to be documented
Model	to be documented

control	to be documented
lower.bound	to be documented
upper.bound	to be documented
tolerance	to be documented

**Value**

a list(minimum=res,objective=objective,model=model).

kernel_matW	<i>kernel_matW</i> A function that returns a sparse weight matrix based computed with a specified kernel (gauss,bisq,tcub,epane,rectangle,triangle) considering coordinates provides in S and a given bandwidth. If NN<nrow(S) only NN firts neighbours are considered. If Type!=’GD’ then S should have additional columns and several kernels and bandwidths should be be specified by the user.
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**Description**

kernel\_matW A function that returns a sparse weight matrix based computed with a specified kernel (gauss,bisq,tcub,epane,rectangle,triangle) considering coordinates provides in S and a given bandwidth. If NN<nrow(S) only NN firts neighbours are considered. If Type!=’GD’ then S should have additional columns and several kernels and bandwidths should be be specified by the user.

**Usage**

```
kernel_matW(H,kernels,coords,NN,TP=NULL,Type='GD',adaptive=FALSE,
diagnull=TRUE,alpha=1,theta=1,dists=NULL,indexG=NULL,extrapol=FALSE,QP=NULL,K=0)
```

**Arguments**

H	A vector of bandwidths
kernels	A vector of kernel types
coords	A matrix with variables used in kernel (reference)
NN	Number of spatial Neighbours for kernels computations
TP	A vector with index of target points
Type	Type of Genelarized kernel product ('GD' only spatial,'GDC' spatial + a categorical variable,'GDX' spatial + a continuous variable, 'GDT' spatial + a time index, and other combinations 'GDXC','GDTX',...)
adaptive	A vector of boolean to choose adaptive version for each kernel
diagnull	Zero on diagonal, default FALSE
alpha	TO BE DOCUMENTED
theta	TO BE DOCUMENTED

dists	TO BE DOCUMENTED
indexG	TO BE DOCUMENTED
extrapol	TO BE DOCUMENTED
QP	A matrix with variables used in kernel (neighbors), default NULL (if NULL coord_j=coord_i)
K	TO BE DOCUMENTED

**Value**

A sparse Matrix of weights (dgCMatrix).

**Examples**

```
library(mgwrsar)
## loading data example
data(mydata)
coords=as.matrix(mydata[,c("x","y")])
## Creating a spatial weight matrix (sparse dgCMatrix) of 4 nearest neighbors with 0 in diagonal
W=kernel_matW(H=4,kernels='rectangle',coords=coords,NN=4,adaptive=TRUE,diagnull=TRUE)
```

MGWRSAR

*Estimation of linear and local linear model with spatial autocorrelation model (mgwrsar).*

**Description**

MGWRSAR is a wrapper function for estimating linear and local linear models with spatial autocorrelation (SAR models with spatially varying coefficients).

**Usage**

```
MGWRSAR(formula, data, coords, fixed_vars = NULL, kernels, H,
Model = "GWR", control = list())
```

**Arguments**

formula	a formula.
data	a dataframe or a spatial dataframe (sp package).
coords	default NULL, a dataframe or a matrix with coordinates, not required if data is a spatial dataframe.
fixed_vars	a vector with the names of spatially constant coefficient for mixed model. All other variables present in formula are supposed to be spatially varying. If empty or NULL (default), all variables in formula are supposed to be spatially varying.

kernel	A vector containing the kernel types. Possible types: rectangle ("rectangle"), bisquare ("bisq"), tricube ("tcub"), epanechnikov ("epane"), gaussian ("gauss"))
H	vector containing the bandwidth parameters for the kernel functions.
Model	character containing the type of model: Possible values are "OLS", "SAR", "GWR" (default), "MGWR" , "MGWRSAR_0_0_kv", "MGWRSAR_1_0_kv", "MGWRSAR_0_kc_kv", "MGWRSAR_1_kc_kv", "MGWRSAR_1_kc_0". See Details for more explanation.
control	list of extra control arguments for MGWRSAR wrapper - see Details below

## Details

**Z** A matrix of variables for generalized kernel product, default NULL.

**W** A row-standardized spatial weight matrix for Spatial Auto-correlation, default NULL.

**type** Verbose mode, default FALSE.

**adaptive** A vector of boolean to choose adaptive version for each kernel.

**kernel\_w** The type of kernel for computing W, default NULL.

**h\_w** The bandwidth value for computing W, default 0.

**Method** Estimation method for computing the models with Spatial Dependence. '2SLS' or 'B2SLS', default '2SLS'.

**TP** A vector of target points, default NULL.

**doMC** Parallel computation, default FALSE. If TRUE and control\_tds\$doMC is also TRUE, then control\$doMC is set to FALSE.

**ncore** Number of CPU core for parallel computation, default 1

**isgev** If TRUE, compute a LOOCV criteria, default FALSE.

**isfgev** If TRUE, simplify the computation of CV criteria (remove or not i when using local instruments for model with lambda spatially varying), default TRUE.

**maxknn** When n > NmaxDist, only the maxknn first neighbours are used for distance computation, default 500.

**NmaxDist** When n > NmaxDist only the maxknn first neighbours are used for distance computation, default 5000

**verbose** Verbose mode, default FALSE.

## Value

MGWRSAR returns an object of class mgwrsar with at least the following components:

**Betav** matrix of coefficients of dim(n,kv) x kv.

**Betac** vector of coefficients of length kc.

**Model** The sum of square residuals.

**Y** The dependent variable.

**XC** The explanatory variables with constant coefficients.

**XV** The explanatory variables with varying coefficients.

**X** The explanatory variables.

**W** The spatial weight matrix for spatial dependence.

**isgev** if gcv has been computed.

**edf** The estimated degrees of freedom.

**formula** The formula.

**data** The dataframe used for computation.

**Method** The type of model.

**coords** The spatial coordinates of observations.

**H** The bandwidth vector.

**fixed\_vars** The names of constant coefficients.

**kernels** The kernel vector.

**SSR** The sum of square residuals.

**residuals** The vector of residuals.

**fit** the vector of fitted values.

**sev** local standard error of parameters.

**get\_ts** Boolean, if trace of hat matrix  $\text{Tr}(S)$  should be stored.

**NN** Maximum number of neighbors for weights computation

MGWRSAR is a wrapper function for estimating linear and local linear model with spatial autocorrelation that allows to estimate the following models :  $y = \beta_c X_c + \epsilon_i$  (OLS)

$$y = \beta_v(u_i, v_i)X_v + \epsilon_i \text{ (GWR)}$$

$$y = \beta_c X_c + \beta_v(u_i, v_i)X_v + \epsilon_i \text{ (MGWR)}$$

$$y = \lambda W y + \beta_c X_c + \epsilon_i \text{ (MGWR-SAR(0,k,0))}$$

$$y = \lambda W y + \beta_v(u_i, v_i)X_v + \epsilon_i \text{ (MGWR-SAR(0,0,k))}$$

$$y = \lambda W y + \beta_c X_c + \beta_v(u_i, v_i)X_v + \epsilon_i \text{ (MGWR-SAR(0,k_c,k_v))}$$

$$y = \lambda(u_i, v_i)W y + \beta_c X_c + \epsilon_i \text{ (MGWR-SAR(1,k,0))}$$

$$y = \lambda(u_i, v_i)W y + \beta_v(u_i, v_i)X_v + \epsilon_i \text{ (MGWR-SAR(1,0,k))}$$

$$y = \lambda(u_i, v_i)W y + \beta_c X_c + \beta_v(u_i, v_i)X_v + \epsilon_i \text{ (MGWR-SAR(1,k_c,k_v))}$$

When model imply spatial autocorrelation, a row normalized spatial weight matrix must be provided. 2SLS and Best 2SLS method can be used. When model imply local regression, a bandwidth and a kernel type must be provided. Optimal bandwidth can be estimated using bandwidths\_mgwsar function. When model imply mixed local regression, the names of stationary covariates must be provided.

#' In addition to the ability of considering spatial autocorrelation in GWR/MGWR like models, MGWRSAR function introduces several useful technics for estimating local regression with space coordinates:

- it uses RCCP and RCCPeigen code that speed up computation and allows parallel computing via doMC package;

- it allows to drop out variables with not enough local variance in local regression, which allows to consider dummies in GWR/MGWR framework without trouble.
- it allows to drop out local outliers in local regression.
- it allows to consider additional variable for kernel, including time (asymmetric kernel) and categorical variables (see Li and Racine 2010). Experimental version.

## References

- Geniaux, G. and Martinetti, D. (2017). A new method for dealing simultaneously with spatial auto-correlation and spatial heterogeneity in regression models. *Regional Science and Urban Economics*. (<https://doi.org/10.1016/j.regsciurbeco.2017.04.001>)
- McMillen, D. and Soppelsa, M. E. (2015). A conditionally parametric probit model of microdata land use in chicago. *Journal of Regional Science*, 55(3):391-415.
- Loader, C. (1999). Local regression and likelihood, volume 47. Springer New York.
- Franke, R. and Nielson, G. (1980). Smooth interpolation of large sets of scattered data. *International journal for numerical methods in engineering*, 15(11):1691-1704.

## See Also

`bandwidths_mgwrsar`, `summary`, `plot`, `predict`, `kernel_matW`

## Examples

```
library(mgwrsar)
## loading data example
data(mydata)
coords=as.matrix(mydata[,c("x","y")])
## Creating a spatial weight matrix (sparse dgCMatrix)
## of 4 nearest neighbors with 0 in diagonal
W=kernel_matW(H=4,kernels='rectangle',coords=coords,NN=4,adaptive=TRUE,
diagnull=TRUE)
mgwrsar_0_kc_kv<-MGWRSAR(formula = 'Y_mgwrsar_0_kc_kv~X1+X2+X3', data = mydata,
coords=coords, fixed_vars='X2',kernels=c('gauss'),H=20, Model = 'MGWRSAR_0_kc_kv',
control=list(SE=FALSE,adaptive=TRUE,W=W))
summary(mgwrsar_0_kc_kv)
```

## Description

Class of mgwrsar Model.

## Slots

**Betav** matrix, the estimated varying coefficients, dim(n,kv).  
**Betac** numeric, the estimated constant coefficients, length kc.  
**Model** character, The type of model.  
**fixed\_vars** character, a vector with name of constant covariate.  
**Y** numeric, the dependent variable.  
**XC** matrix, the explanatory variables with constant coefficients.  
**XV** matrix, the explanatory variables with varying coefficients.  
**X** matrix, the explanatory variables.  
**W** SparseMatrix, the spatial weight matrix for spatial dependence.  
**isgcv** logical, if gcv has been computed.  
**edf** numeric, the estimated degrees of freedom.  
**formula** formula  
**data** dataframe, The dataframe used for computation.  
**Method** character, the estimation technique for computing the models with Spatial Dependence.  
'2SLS' or 'B2SLS', default '2SLS'.  
**coords** matrix, the spatial coordinates of observations.  
**H** numeric, the bandwidth vector.  
**H2** numeric, the time bandwidth vector.  
**kernels** character, the type of kernel.  
**adaptive** logical, adaptive kernel.  
**Type** character, the type of General Kernel Product.  
**TP** numeric, index of target points.  
**SSRtp** numeric, the sum of square residuals for TP.  
**SSR** numeric, the sum of square residuals.  
**residuals** numeric, the vector of residuals.  
**fit** numeric, the vector of fitted values.  
**pred** numeric, the vector of predicted values.  
**sev** matrix, local standard error of varying coefficients.  
**se** numeric, standard error of constant coefficients.  
**tS** numeric, Trace(S).  
**Shat**, hat matrix  
**R\_k**, list of hat matrix by var  
**h\_w** numeric, the bandwidth value for computing W, default 0.  
**kernel\_w** the type of kernel for computing W, default NULL.  
**RMSE** numeric, Root Mean Square Error for Target Points.  
**RMSEtp** numeric, Root Mean Square Error for all Points.

CV numeric, Leave One Out CV.

AIC numeric, Akaike Criteria.

AICc numeric, Corrected Akaike Criteria.

AICctp numeric, Corrected Akaike Criteria for TP

BIC numeric, Bayesian Information Criteria.

R2 numeric, R2.

R2\_adj numeric, adjusted R2.

get\_ts logical, if trace of hat matrix Tr(S) should be stored.

NN numeric, the maximum number of neighbors for weights computation

doMC logical, parallel computation.

ncore numeric, number of cores.

mycall a call, the call of the model.

ctime numeric, the computing times in seconds.

HRMSE matrix, RMSE log.

HBETA list, estimated BETA at each iteration.

loglik numeric, value of loglik.

G list, list of neighboring index and distances (knn object from nabor package).

V numeric, neighbors sequence for TDS.

Vt numeric, neighbors sequence for TDS.

Z numeric, time for GDT kernel type

TS numeric, Diagonal of Hat Matrix

alpha numeric, ratio for GDT kernels

theta numeric, ratio for GDT kernels

**mgwrsar\_bootstrap\_test**

*A bootstrap test for Betas for mgwrsar class model.*

**Description**

A bootstrap test for Betas for mgwrsar class model.

**Usage**

```
mgwrsar_bootstrap_test(x0,x1,B=100,doMC=FALSE,ncore=1,type='standard'
,eps='H1',df='H1',focal='median',D=NULL)
```

**Arguments**

x0	The H0 mgwrsar model
x1	The H1 mgwrsar model
B	number of bootstrap repetitions, default 100
doMC	If TRUE, doParallel parallelization
ncore	number of cores
type	type of bootstrap : 'wild', 'Rademacher', 'spatial' or 'standard' (default)
eps	Hypothesis under which residuals are simulated, 'H0' or 'H1' (default)
df	Hypothesis under which degree of freedom is estimated.
focal	see sample_stat help
D	A matrix of distance

**Value**

The value of the statictics test and a p ratio.

**See Also**

mgwrsar\_bootstrap\_test\_all

mgwrsar\_bootstrap\_test\_all

*A bootstrap test for testing nullity of all Betas for mgwrsar class model,*

**Description**

A bootstrap test for testing nullity of all Betas for mgwrsar class model,

**Usage**

```
mgwrsar_bootstrap_test_all(model,B=100,doMC=FALSE,ncore=1,
type='standard')
```

**Arguments**

model	A mgwrsar model
B	number of bootstrap replications, default 100
doMC	If TRUE, doMC parallelization
ncore	number of cores.
type	type of bootstrap ('spatial', 'wild', 'random')

**Value**

a matrix with statistical test values and p ratios

**See Also**

`mgwrsar_bootstrap_test`

`modc`

*modc is a set of models to correct approximation of hat matrix trace*

**Description**

`modc` is a set of models to correct approximation of hat matrix trace

**Author(s)**

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**References**

[doi:10.1016/j.regsciurbeco.2017.04.001](https://doi.org/10.1016/j.regsciurbeco.2017.04.001)

`multiscale_gwr`

*multiscale\_gwr This function adapts the multiscale Geographically Weighted Regression (GWR) methodology proposed by Fotheringham et al. in 2017, employing a backward fitting procedure within the MGWRSAR subroutines. The consecutive bandwidth optimizations are performed by minimizing the corrected Akaike criteria.*

**Description**

`multiscale_gwr` This function adapts the multiscale Geographically Weighted Regression (GWR) methodology proposed by Fotheringham et al. in 2017, employing a backward fitting procedure within the MGWRSAR subroutines. The consecutive bandwidth optimizations are performed by minimizing the corrected Akaike criteria.

**Usage**

```
multiscale_gwr(formula,data,coords,kernels='bisq',init='GWR',
maxiter=20,nstable=6,tolerance=0.000001,doMC=FALSE,ncore=1,HF=NULL,
H0=NULL,H2=NULL,Model=NULL,model=NULL,get_AICg=FALSE,verbose=FALSE,
control=list(SE=FALSE,adaptive=TRUE,NN=800,isgcv=FALSE,family=gaussian()))
```

**Arguments**

formula	A formula.
data	A dataframe.
coords	default NULL, a dataframe or a matrix with coordinates.
kernels	A vector containing the kernel types. Possible types: rectangle ("rectangle"), bisquare ("bisq"), tricube ("tcub"), epanechnikov ("epane")
init	starting model (lm or GWR)
maxiter	maximum number of iterations in the back-fitting procedure.
nstable	required number of consecutive unchanged optimal bandwidth (by covariate) before leaving optimisation of bandwidth size, default 3.
tolerance	value to terminate the back-fitting iterations (ratio of change in RMSE)
doMC	A boolean for Parallel computation, default FALSE.
ncore	number of CPU cores for parallel computation, default 1.
HF	if available, a vector containing the optimal bandwidth parameters for each covariate, default NULL.
H0	A bandwidth value for the starting GWR model, default NULL.
H2	A bandwidth temporal value for the starting GWR model, default NULL.
Model	Type of Model.
model	A previous model estimated using multiscale_gwr function, default NULL
get_AICg	Boolean, should Global AICc be estimated.
verbose	Boolean, verbose mode.
control	a list of extra control arguments, see MGWRsar help.

**Value**

Return an object of class mgwrsar

mydata

*mydata is a simulated data set of a mgwrsar model*

**Description**

mydata is a simulated data set of a mgwrsar model

**Format**

A data frames with 1000 rows 22 variables and a matrix of coordinates with two columns

**Author(s)**

Ghislain Geniaux and Davide Martinetti <ghislain.geniaux@inrae.fr>

**References**

[doi:10.1016/j.regsciurbeco.2017.04.001](https://doi.org/10.1016/j.regsciurbeco.2017.04.001)

**mydataf**

*mydataf* is a Simple Feature object with real estate data in south of France.

### Description

`mydataf` is a Simple Feature object with real estate data in south of France.

### Format

A sf object with 1403 rows, 5 columns

### Author(s)

Ghislain Geniaux <[ghislain.geniaux@inrea.fr](mailto:ghislain.geniaux@inrea.fr)>

### References

<https://www.data.gouv.fr/fr/datasets/demandes-de-valeurs-foncieres/>

**normW**

*normW* row normalization of dgCMatrix

### Description

`normW` row normalization of dgCMatrix

### Usage

`normW(W)`

### Arguments

`W` A dgCMatrix class matrix

### Value

A row normalized dgCMatrix

---

**plot,mgwrsar,missing-method**  
*Plot method for mgwrsar model*

---

## Description

Plot method for mgwrsar model

## Usage

```
## S4 method for signature 'mgwrsar,missing'
plot(
  x,
  y,
  type = "coef",
  var = NULL,
  crs = NULL,
  mypalette = "RdYlGn",
  opacity = 0.5,
  fopacity = 0.5,
  nbins = 8,
  radius = 500,
  mytile = "Stadia.StamenTonerBackground",
  myzoom = 8,
  myresolution = 150,
  LayersControl = TRUE,
  myzoomControl = TRUE,
  mytile2 = NULL,
  ScaleBar = NULL,
  ScaleBarOptions = list(maxWidth = 200, metric = TRUE, imperial = FALSE, updateWhenIdle
    = TRUE),
  MyLegendTitle = NULL,
  lopacity = 0.5
)
```

## Arguments

x	A model of class <a href="#">mgwrsar-class</a> .
y	missing
type	default 'coef', for plotting the value of the coefficients. Local t-Student could also be plot using 't_coef', residuals using 'residuals' and fitted using 'fitted'.
var	Names of variable to plot.
crs	A CRS projection.
mypalette	A leaflet palette.
opacity	Opacity of border color.

fopacity	Opacity of fill color.
nbins	nbins.
radius	radius of circle for plot of points.
mytile	tile 1.
myzoom	level of zoom for tile 1.
myresolution	resolution for tile 1.
LayersControl	layers controls.
myzoomControl	zoom control.
mytile2	tile 2.
ScaleBar	ScaleBar.
ScaleBarOptions	options for ScaleBar.
MyLegendTitle	Legend title.
lopacity	opacity for legend.

**Value**

A Interactive Web Maps with local parameters plot and Open Street Map layer.

<b>plot_effect</b>	<i>plot_effect</i> <i>plot_effect</i> is a function that plots the effect of a variable $X_k$ with spatially varying coefficient, i.e $X_k * Beta_k(u_i, v_i)$ for comparing the magnitude of effects of between variables.
--------------------	---

**Description**

*plot\_effect* *plot\_effect* is a function that plots the effect of a variable  $X_k$  with spatially varying coefficient, i.e  $X_k * Beta_k(u_i, v_i)$  for comparing the magnitude of effects of between variables.

**Usage**

```
plot_effect(model, sampling=TRUE, nsample=2000, nsample_max=5000, title='')
```

**Arguments**

model	a model of mgwrsar class with some spatially varying coefficients.
sampling	Boolean, if nrow(model@Betav)> nsample_max a sample of size nsample is randomly selected, default TRUE.
nsample	integer, size of the sample if sampling is TRUE, default 2000.
nsample_max	integer, size max to engage sampling if sampling is TRUE, default 5000.
title	a title for the plot.

## Examples

```
library(mgwrsar)
## loading data example
data(mydata)
coords=as.matrix(mydata[,c("x","y")])
## Creating a spatial weight matrix (sparce dgCMatrix)
## of 8 nearest neighbors with 0 in diagonal
model_GWR0<-MGWRSAR(formula = 'Y_gwr~X1+X2+X3', data = mydata,coords=coords,
fixed_vars=NULL,kernels=c('gauss'),H=0.13, Model = 'GWR',control=list(SE=TRUE))
plot_effect(model_GWR0)
```

**predict,mgwrsar-method**

*predict method for mgwrsar model*

## Description

predict method for mgwrsar model

## Usage

```
## S4 method for signature 'mgwrsar'
predict(
  object,
  newdata,
  newdata_coords,
  W = NULL,
  type = "BPN",
  h_w = 100,
  kernel_w = "rectangle",
  maxobs = 4000,
  beta_proj = FALSE,
  method_pred = "TP",
  k_extra = 8,
  ...
)
```

## Arguments

<b>object</b>	A model of class <a href="#">mgwrsar-class</a> .
<b>newdata</b>	a matrix or data.frame of new data.
<b>newdata_coords</b>	a matrix of new coordinates, and eventually other variables if a General Kernel Product is used.
<b>W</b>	the spatial weight matrix for models with spatial autocorrelation.
<b>type</b>	Type for BLUP estimator, default "BPN". If NULL use predictions without spatial bias correction.

<code>h_w</code>	A bandwidth value for the spatial weight matrix
<code>kernel_w</code>	kernel type for the spatial weight matrix. Possible types: rectangle ("rectangle"), bisquare ("bisq"), tricube ("tcub"), epanechnikov ("epane"), gaussian ("gauss"))
<code>.</code>	
<code>maxobs</code>	maximum number of observations for exact calculation of solve(I- rho*W), default maxobs=4000.
<code>beta_proj</code>	A boolean, if TRUE the function then return a two elements list(Y_predicted,Beta_proj_out)
<code>method_pred</code>	If method_pred = 'TP' (default) prediction is done by recomputing a MGWR-SAR model with new-data as target points, else if method_pred in ('tWtp_model','model','shepard') a matrix for projecting estimated betas is used (see details).
<code>k_extra</code>	number of neighbours for local parameter extrapolation if shepard kernel is used, default 8.
<code>...</code>	predict parameters forwarded.

### Details

if method\_pred = 'tWtp\_model', the weighting matrix for prediction is based on the expected weights of outsample data if they were had been added to insample data to estimate the corresponding MG-WRSAR (see Geniaux 2022 for further detail), if method\_pred = 'shepard' a shepard kernel with k\_extra neighbours (default 8) is used and if method\_pred='kernel\_model' the same kernel and number of neighbors as for computing the MGWRSAR model is used.

### Value

A vector of predictions if beta\_proj is FALSE or a list with a vector named Y\_predicted and a matrix named Beta\_proj\_out.

A vector of predictions.

### residuals,mgwrsar-method

*residuals for mgwrsar model*

### Description

residuals for mgwrsar model

### Usage

```
## S4 method for signature 'mgwrsar'
residuals(object, ...)
```

### Arguments

<code>object</code>	A model of class <a href="#">mgwrsar-class</a> .
<code>...</code>	residuals parameters forwarded.

**Value**

A vector of residuals.

simu_multiscale	<i>Estimation of linear and local linear model with spatial autocorrelation model (mgwrsar).</i>
-----------------	--

**Description**

The simu\_multiscale function is designed for simulating a spatially varying coefficient DGP (Data Generating Process) based on formulations proposed by Fotheringham et al. (2017), Gao et al. (2021), or Geniaux (2024).

**Usage**

```
simu_multiscale(n=1000,myseed=1,type='GG2024',constant=NULL,
nuls=NULL,config_beta='default',config_snr=0.7,config_eps='normal',
ratiotime=1)
```

**Arguments**

n	An integer number of observations
myseed	An integer seed used for the simulation.
type	Type of DGP used 'FT2017', 'Gao2021' or 'GG2024', default 'GG2024'.
constant	A boolean parameter indicating whether the intercept term should be spatially varying (TRUE) or not (FALSE).
nuls	A vector of null parameters, default NULL
config_beta	name of the type of spatial pattern of Beta coefficients
config_snr	a value of signal noise ratio
config_eps	name of the distribution of error ('normal', 'unif' or 'Chi2')
ratiotime	multiplicating factor, for spacetime DGP.

**Value**

A named list with simulated data ('mydata') and coords ('coords')

**Examples**

```
library(mgwrsar)
library(ggplot2)
library(gridExtra)
library(grid)
simu=simu_multiscale(1000)
mydata=simu$mydata
coords=simu$coords
```

```
p1<-ggplot(mydata,aes(x,y,col=Beta1))+geom_point() +scale_color_viridis_c()
p2<-ggplot(mydata,aes(x,y,col=Beta2))+geom_point() +scale_color_viridis_c()
p3<-ggplot(mydata,aes(x,y,col=Beta3))+geom_point() +scale_color_viridis_c()
p4<-ggplot(mydata,aes(x,y,col=Beta4))+geom_point() +scale_color_viridis_c()
grid.arrange(p1,p2,p3,p4,nrow=2,ncol=2, top = textGrob("DGP Geniaux (2024)"
,gp=gpar(fontsize=20,font=3)))
```

---

**summary,mgwrsar-method**

*summary for mgwrsar model*

---

## Description

summary for mgwrsar model

## Usage

```
## S4 method for signature 'mgwrsar'
summary(object, ...)
```

## Arguments

object	A model of class <a href="#">mgwrsar-class</a> .
...	summary parameters forwarded.

## Value

A summary object.

---

**summary\_Matrix**

*summary\_Matrix to be documented*

---

## Description

summary\_Matrix to be documented

## Usage

```
summary_Matrix(object, ...)
```

## Arguments

object	to be documented
...	to be documented

## Value

to be documented

---

tds\_mgwr*Top-Down Scaling approach of multiscale GWR*

---

## Description

This function performs a multiscale Geographically Weighted Regression (GWR) using a top-down scaling approach, adjusting GWR coefficients with a progressively decreasing bandwidth as long as the AICc criterion improves.

## Usage

```
tds_mgwr(formula,data,coords,Model='tds_mgwr',kernels='triangle',
fixed_vars=NULL,H2=NULL,control_tds=list(nns=30,get_AIC=FALSE),
control=list(adaptive=TRUE))
```

## Arguments

formula	a formula.
data	a dataframe.
coords	default NULL, a dataframe or a matrix with coordinates
Model	character containing the type of model: Possible values are "tds_mgwr" and "atds_mgwr", See Details for more explanation.
kernels	A vector containing the kernel types. Possible types: triangle ("triangle"), rectangle ("rectangle"), bisquare ("bisq"), tricube ("tcub"), gaussian ("gauss"), epanechnikov ("epane").
fixed_vars	a vector with the names of spatially constant coefficient for mixed model. All other variables present in formula are supposed to be spatially varying. If empty or NULL (default), all variables in formula are supposed to be spatially varying.
H2	A scalar or vector of time bandwidths.
control_tds	list of extra control arguments for tds_mgwr models
control	list of extra control arguments for MGWRSAR wrapper

## Details

**nns** Length of the sequence of decreasing bandwidth. Should be between 20 and 100, default 30

**get\_AIC** Boolean, if the Global AICc using Yu et al 2019 should be computed. Required if the second stage 'atds\_mgwr' has to be estimated. default FALSE

**init\_model** Starting model, 'GWR' or 'OLS', 'default OLS'.

**model\_stage1** If model='tds\_mgwr', model\_stage1 can be used as a starting model (either a GWR model or a previous tds\_mgwr model). For model='atds\_mgwr', the user can specified an tds\_mgwr model already computed with get\_AIC=TRUE. default NULL.

**doMC** Parallel computation, default FALSE.

**ncore** number of CPU core for parallel computation, default 1

**tol** Tolerance for stopping criteria, default 0.0001

**nrounds** Number of nrounds for 'atds\_mgwr' model. Default 3.

**verbose** verbose mode, default FALSE.

**V** A vector of decreasing bandwidths given by the user, default NULL

**first\_nn** The value of the highest bandwidth for the sequence of decreasing bandwidth, default NULL.

**minv** The value of the smallest bandwidth for the sequence of decreasing bandwidth, default number of covariates + 2 .

**H** A vector of bandwidth, default NULL

**Z** A matrix of variables for generalized kernel product, default NULL.

**W** A row-standardized spatial weight matrix for Spatial Auto-correlation, default NULL.

**type** Verbose mode, default FALSE.

**adaptive** A vector of boolean to choose adaptive version for each kernel.

**kernel\_w** The type of kernel for computing W, default NULL.

**h\_w** The bandwidth value for computing W, default 0.

**Method** Estimation method for computing the models with Spatial Dependence. '2SLS' or 'B2SLS', default '2SLS'.

**TP** Avector of target points, default NULL.

**doMC** Parallel computation, default FALSE. If TRUE and control\_tds\$doMC is also TRUE, then control\$doMC is set to FALSE.

**ncore** Number of CPU core for parallel computation, default 1

**isgcv** If TRUE, compute a LOOCV criteria, default FALSE.

**isfgcv** If TRUE, simplify the computation of CV criteria (remove or not i when using local instruments for model with lambda spatially varying), default TRUE.

**maxknn** When n > NmaxDist, only the maxknn first neighbours are used for distance compution, default 500.

**NmaxDist** When n > NmaxDist only the maxknn first neighbours are used for distance compution, default 5000

**verbose** Verbose mode, default FALSE.

## See Also

`gwr_multiscale`, `MGWRSAR`, `bandwidths_mgwrsar`, `summary_mgwrsar`.

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