

# Package ‘lsirm12pl’

July 8, 2025

**Type** Package

**Title** Latent Space Item Response Model

**Version** 1.3.5

**Date** 2025-07-08

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**Description** Analysis of dichotomous and continuous response data using latent factor by both 1PL LSIRM and 2PL LSIRM as described in Jeon et al. (2021) <doi:10.1007/s11336-021-09762-5>. It includes original 1PL LSIRM and 2PL LSIRM provided for binary response data and its extension for continuous response data. Bayesian model selection with spike-and-slab prior and method for dealing data with missing value under missing at random, missing completely at random are also supported. Various diagnostic plots are available to inspect the latent space and summary of estimated parameters.

**License** GPL-3

**Imports** Rcpp (>= 1.0.5), MCMCpack, ggplot2, GPArotation, dplyr (>= 1.1.4), grDevices, rlang, pROC, coda, spatstat, spatstat.geom, spatstat.random, plotly, gridExtra, grid, tidyr, fpc, kernlab, plyr, purrr

**LinkingTo** Rcpp, RcppArmadillo

**Encoding** UTF-8

**RoxygenNote** 7.3.2

**Suggests** knitr, testthat

**Depends** R (>= 3.1.0)

**LazyData** true

**NeedsCompilation** yes

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**Repository** CRAN

**Date/Publication** 2025-07-08 02:40:02 UTC

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BFPT *Big Five Personality Test*

---

### Description

A dataset containing the result of personality test for 50 questions from 1,000 random sampled people.

### Usage

```
data(BFPT)
```

### Format

A matrix with 1,015,341 rows and 50 columns.

### Details

A dataset collected in 2016-2018 through an interactive on-line personality test, containing the result of personality test for 50 questions. 1,000 people are random sampled from the original dataset containing 1,015,341 people. The scale is labeled as 1=Disagree, 3=Neutral and 5=Agree.

### Source

<https://www.kaggle.com/tunguz/big-five-personality-test>

---

diagnostic *Diagnostic the result of LSIRM.*

---

### Description

diagnostic checks the convergence of MCMC for LSIRM parameters using various diagnostic tools, such as trace plots, posterior density distributions, autocorrelation functions (ACF), and Gelman-Rubin-Brooks plots.

### Usage

```
diagnostic(  
  object,  
  draw.item = list(beta = c(1), theta = c(1)),  
  gelman.diag = FALSE  
)
```

**Arguments**

|             |  |
|-------------|--|
| object      | Object of class lsirm.   |
| draw.item   | List; Each key in the list corresponds to a specific parameters such as "beta", "theta", "gamma", "alpha", "theta_sd", "sigma" and "zw.dist". The values of the list indicate the indices of these parameters. For the key "zw.dist", the value is a matrix with two columns: the first column represents the indices of respondents, and the second column represents the indices of items. |
| gelman.diag | Logical; If TRUE, the Gelman-Rubin convergence diagnostic will be printed. Default is FALSE.   |

**Value**

diagnostic returns plots for checking MCMC convergence for selected parameters.

**Examples**

```
# Generate example item response matrix
data <- matrix(rbinom(500, size = 1, prob = 0.5), ncol=10, nrow=50)

# For 1PL LSIRM
lsirm_result <- lsirm(data ~ lsirm1pl(spikenslab = FALSE, fixed_gamma = FALSE))
diagnostic(lsirm_result)

# For 2PL LSIRM
lsirm_result <- lsirm(data ~ lsirm2pl(spikenslab = FALSE, fixed_gamma = FALSE))
diagnostic(lsirm_result)
```

---

gof

---

*Goodness-of-fit LSIRM*


---

**Description**

[gof](#) is goodness-of-fit the latent space of fitted LSIRM.

**Usage**

```
gof(object, chain.idx = 1)
```

**Arguments**

|           |   |
|-----------|---|
| object    | Object of class lsirm.                      |
| chain.idx | Numeric; Index of MCMC chain. Default is 1. |

**Value**

gof returns the boxplot or AUC plot

## Examples

```
# generate example item response matrix
data <- matrix(rbinom(500, size = 1, prob = 0.5), ncol=10, nrow=50)
lsirm_result <- lsirm(data ~ lsirm1pl())
gof(lsirm_result)
```

---

lsirm

*Fit a LSIRM ( Latent Space Item Response Model)*


---

## Description

[lsirm](#) is used to fit 1PL LSIRM and 2PL LSIRM using Bayesian method as described in Jeon et al. (2021).

## Usage

```
lsirm(formula, ...)
```

## Arguments

|         |   |
|---------|---|
| formula | The form of formula is <code>lsirm(A ~ &lt;term 1&gt;(&lt;term 2&gt;, &lt;term 3&gt; ...))</code> , where A is binary or continuous item response matrix to be analyzed, <term1> is the model you want to fit and has one of the following values: "lsirm1pl" and "lsirm2pl", and <term 2>, <term 3>, etc. are each option for the model. |
| ...     | Additional arguments for the corresponding function.  |

## Details

The descriptions of options for each model, such as <term 2> and <term 3>, are included in [lsirm1pl](#) for 1PL LSIRM and [lsirm2pl](#) for 2PL LSIRM.

## Value

`lsirm` returns an object of class `list`.

See corresponding functions such as [lsirm1pl](#) for 1PL LSIRM and [lsirm2pl](#) for 2PL LSIRM.

## See Also

[lsirm1pl](#) for 1PL LSIRM.

[lsirm2pl](#) for 2PL LSIRM.

Examples

```
# generate example item response matrix
data <- matrix(rbinom(500, size = 1, prob = 0.5), ncol=10, nrow=50)

lsirm_result <- lsirm(data~lsirm1pl())
lsirm_result <- lsirm(data~lsirm2pl())
```

---

|               |                                   |
|---------------|-----------------------------------|
| lsirm.formula | <i>Formula function for LSIRM</i> |
|---------------|-----------------------------------|

---

Description

lsirm.formula is formula object.

Usage

```
## S3 method for class 'formula'
lsirm(formula, ...)
```

Arguments

- formula      The form of formula is lsirm(A ~ <term 1>(<term 2>, <term 3> ...)), where A is binary or continuous item response matrix to be analyzed, <term1> is the model you want to fit and has one of the following values: "lsirm1pl" and "lsirm2pl"., and <term 2>, <term 3>, etc., are each option for the model.
- ...          Additional arguments for the corresponding function.

---

|           |                          |
|-----------|--------------------------|
| lsirm12pl | <i>lsirm12pl-package</i> |
|-----------|--------------------------|

---

Description

Analysis of dichotomous and continuous response data using latent factor by both 1PL LSIRM and 2PL LSIRM as described in Jeon et al. (2021) <doi:10.1007/s11336-021-09762-5>. It includes original 1PL LSIRM and 2PL LSIRM provided for binary response data and its extension for continuous response data. Bayesian model selection with spike-and-slab prior and method for dealing data with missing value under missing at random, missing completely at random are also supported. Various diagnostic plots are available to inspect the latent space and summary of estimated parameters.

lsirm1pl

*Fit a 1PL LSIRM for binary and continuous item response data***Description**

`lsirm1pl` integrates all functions related to 1PL LSIRM. Various 1PL LSIRM function can be used by setting the `spikenslab`, `fixed_gamma`, and `missing_data` arguments.

This function can be used regardless of the data type, providing a unified approach to model fitting.

**Usage**

```
lsirm1pl(
  data,
  spikenslab = FALSE,
  fixed_gamma = FALSE,
  missing_data = NA,
  chains = 1,
  multicore = 1,
  seed = NA,
  ndim = 2,
  niter = 15000,
  nburn = 2500,
  nthin = 5,
  nprint = 500,
  jump_beta = 0.4,
  jump_theta = 1,
  jump_z = 0.5,
  jump_w = 0.5,
  pr_mean_beta = 0,
  pr_sd_beta = 1,
  pr_mean_theta = 0,
  pr_a_theta = 0.001,
  pr_b_theta = 0.001,
  ...
)
```

**Arguments**

|                           |   |
|---------------------------|---|
| <code>data</code>         | Matrix; a binary or continuous item response matrix for analysis. Each row represents a respondent, and each column contains responses to the corresponding item. |
| <code>spikenslab</code>   | Logical; specifies whether to use a model selection approach. Default is FALSE.   |
| <code>fixed_gamma</code>  | Logical; indicates whether to fix gamma at 1. Default is FALSE.   |
| <code>missing_data</code> | Character; the type of missing data assumed. Options are NA, "mar", or "mcar". Default is NA.   |

|               |  |
|---------------|--|
| chains        | Integer; the number of MCMC chains to run. Default is 1.   |
| multicore     | Integer; the number of cores to use for parallel execution. Default is 1.                            |
| seed          | Integer; the seed number for MCMC fitting. Default is NA.  |
| ndim          | Integer; the dimension of the latent space. Default is 2.  |
| niter         | Integer; the total number of MCMC iterations to run. Default is 15000.                               |
| nburn         | Integer; the number of initial MCMC iterations to discard as burn-in. Default is 2500.               |
| nthin         | Integer; the number of MCMC iterations to thin. Default is 5.  |
| nprint        | Integer; the interval at which MCMC samples are displayed during execution. Default is 500.          |
| jump_beta     | Numeric; the jumping rule for the beta proposal density. Default is 0.4.                             |
| jump_theta    | Numeric; the jumping rule for the theta proposal density. Default is 1.0.                            |
| jump_z        | Numeric; the jumping rule for the z proposal density. Default is 0.5.                                |
| jump_w        | Numeric; the jumping rule for the w proposal density. Default is 0.5.                                |
| pr_mean_beta  | Numeric; the mean of the normal prior for beta. Default is 0.  |
| pr_sd_beta    | Numeric; the standard deviation of the normal prior for beta. Default is 1.0.                        |
| pr_mean_theta | Numeric; the mean of the normal prior for theta. Default is 0.                                       |
| pr_a_theta    | Numeric; the shape parameter of the inverse gamma prior for the variance of theta. Default is 0.001. |
| pr_b_theta    | Numeric; the scale parameter of the inverse gamma prior for the variance of theta. Default is 0.001. |
| ...           | Additional arguments for the for various settings. Refer to the functions in the Details.            |

## Details

Additional arguments and return values for each function are documented in the respective function's description.

\* For LSIRM with data included missing value are detailed in [lsirm1pl\\_mar](#) and [lsirm1pl\\_mcar](#).

\* For LSIRM using the spike-and-slab model selection approach are detailed in [lsirm1pl\\_ss](#).

\* For continuous version of LSIRM are detailed in [lsirm1pl\\_normal\\_o](#).

For 1PL LSIRM with binary item response data, the probability of correct response by respondent  $j$  to item  $i$  with item effect  $\beta_i$ , respondent effect  $\theta_j$  and the distance between latent position  $w_i$  of item  $i$  and latent position  $z_j$  of respondent  $j$  in the shared metric space, with  $\gamma$  represents the weight of the distance term:

$$\text{logit}(P(Y_{j,i} = 1 | \theta_j, \beta_i, \gamma, z_j, w_i)) = \theta_j + \beta_i - \gamma ||z_j - w_i||$$

For 1PL LSIRM with continuous item response data, the continuous value of response by respondent  $j$  to item  $i$  with item effect  $\beta_i$ , respondent effect  $\theta_j$  and the distance between latent position  $w_i$  of item  $i$  and latent position  $z_j$  of respondent  $j$  in the shared metric space, with  $\gamma$  represents the weight of the distance term:

$$Y_{j,i} = \theta_j + \beta_i - \gamma ||z_j - w_i|| + e_{j,i}$$

where the error  $e_{j,i} \sim N(0, \sigma^2)$ .



**Value**

lsirm1pl returns an object of list. The basic return list containing the following components:

|                      |  |
|----------------------|--|
| data                 | A data frame or matrix containing the variables used in the model.   |
| bic                  | A numeric value representing the Bayesian Information Criterion (BIC).   |
| mcmc_inf             | Details about the number of MCMC iterations, burn-in periods, and thinning intervals.  |
| map_inf              | The log maximum a posteriori (MAP) value and the iteration number at which this MAP value occurs.  |
| beta_estimate        | Posterior estimates of the beta parameter.   |
| theta_estimate       | Posterior estimates of the theta parameter.  |
| sigma_theta_estimate | Posterior estimates of the standard deviation of theta.  |
| z_estimate           | Posterior estimates of the z parameter.  |
| w_estimate           | Posterior estimates of the w parameter.  |
| beta                 | Posterior samples of the beta parameter.   |
| theta                | Posterior samples of the theta parameter.  |
| theta_sd             | Posterior samples of the standard deviation of theta.  |
| z                    | Posterior samples of the z parameter, represented as a 3-dimensional matrix where the last axis denotes the dimension of the latent space. |
| w                    | Posterior samples of the w parameter, represented as a 3-dimensional matrix where the last axis denotes the dimension of the latent space. |
| accept_beta          | Acceptance ratio for the beta parameter.   |
| accept_theta         | Acceptance ratio for the theta parameter.  |
| accept_z             | Acceptance ratio for the z parameter.  |
| accept_w             | Acceptance ratio for the w parameter.  |
| ...                  | Additional return values for various settings. Refer to the functions in the Details.  |

**Note**

If both `spikenslab` and `fixed_gamma` are set TRUE, it returns error because both are related to `gamma`.

**See Also**

The LSIRM for 1PL LSIRM for binary item response data as following:

[lsirm1pl\\_o](#), [lsirm1pl\\_fixed\\_gamma](#), [lsirm1pl\\_mar](#), [lsirm1pl\\_mcar](#), [lsirm1pl\\_fixed\\_gamma\\_mar](#), [lsirm1pl\\_fixed\\_gamma\\_mcar](#), [lsirm1pl\\_ss](#), [lsirm1pl\\_mar\\_ss](#), and [lsirm1pl\\_mcar\\_ss](#)

The LSIRM for 1PL LSIRM for continuous item response data as following:

[lsirm1pl\\_normal\\_o](#), [lsirm1pl\\_normal\\_fixed\\_gamma](#), [lsirm1pl\\_normal\\_mar](#), [lsirm1pl\\_normal\\_mcar](#), [lsirm1pl\\_normal\\_mar\\_ss](#), [lsirm1pl\\_normal\\_mcar\\_ss](#), [lsirm1pl\\_normal\\_fixed\\_gamma\\_mcar](#), [lsirm1pl\\_normal\\_ss](#), [lsirm1pl\\_normal\\_mar\\_ss](#), [lsirm1pl\\_normal\\_mcar\\_ss](#)

## Examples

```
# generate example item response matrix
data <- matrix(rbinom(500, size = 1, prob = 0.5), ncol=10, nrow=50)
lsirm_result <- lsirm1pl(data)

# The code following can achieve the same result.
lsirm_result <- lsirm(data~lsirm1pl())
```

---

lsirm1pl\_fixed\_gamma    *1PL LSIRM fixing gamma to 1.*

---

## Description

[lsirm1pl\\_fixed\\_gamma](#) is used to fit 1PL LSIRM with gamma fixed to 1. [lsirm1pl\\_fixed\\_gamma](#) factorizes item response matrix into column-wise item effect, row-wise respondent effect and further embeds interaction effect in a latent space. The resulting latent space provides an interaction map that represents interactions between respondents and items.

## Usage

```
lsirm1pl_fixed_gamma(
  data,
  ndim = 2,
  niter = 15000,
  nburn = 2500,
  nthin = 5,
  nprint = 500,
  jump_beta = 0.4,
  jump_theta = 1,
  jump_z = 0.5,
  jump_w = 0.5,
  pr_mean_beta = 0,
  pr_sd_beta = 1,
  pr_mean_theta = 0,
  pr_a_theta = 0.001,
  pr_b_theta = 0.001,
  verbose = FALSE
)
```

## Arguments

|      |   |
|------|---|
| data | Matrix; a binary or continuous item response matrix for analysis. Each row represents a respondent, and each column contains responses to the corresponding item. |
| ndim | Integer; the dimension of the latent space. Default is 2.   |

|               |  |
|---------------|--|
| niter         | Integer; the total number of MCMC iterations to run. Default is 15000.                               |
| nburn         | Integer; the number of initial MCMC iterations to discard as burn-in. Default is 2500.               |
| nthin         | Integer; the number of MCMC iterations to thin. Default is 5.  |
| nprint        | Integer; the interval at which MCMC samples are displayed during execution. Default is 500.          |
| jump_beta     | Numeric; the jumping rule for the beta proposal density. Default is 0.4.                             |
| jump_theta    | Numeric; the jumping rule for the theta proposal density. Default is 1.0.                            |
| jump_z        | Numeric; the jumping rule for the z proposal density. Default is 0.5.                                |
| jump_w        | Numeric; the jumping rule for the w proposal density. Default is 0.5.                                |
| pr_mean_beta  | Numeric; the mean of the normal prior for beta. Default is 0.  |
| pr_sd_beta    | Numeric; the standard deviation of the normal prior for beta. Default is 1.0.                        |
| pr_mean_theta | Numeric; the mean of the normal prior for theta. Default is 0.                                       |
| pr_a_theta    | Numeric; the shape parameter of the inverse gamma prior for the variance of theta. Default is 0.001. |
| pr_b_theta    | Numeric; the scale parameter of the inverse gamma prior for the variance of theta. Default is 0.001. |
| verbose       | Logical; If TRUE, MCMC samples are printed for each nprint. default value is FALSE                   |

## Details

lsirm1pl\_fixed\_gamma models the probability of correct response by respondent  $j$  to item  $i$  with item effect  $\beta_i$ , respondent effect  $\theta_j$  and the distance between latent position  $w_i$  of item  $i$  and latent position  $z_j$  of respondent  $j$  in the shared metric space:

$$\text{logit}(P(Y_{j,i} = 1 | \theta_j, \beta_i, z_j, w_i)) = \theta_j + \beta_i - ||z_j - w_i||$$

## Value

lsirm1pl\_fixed\_gamma returns an object of list containing the following components:

|                      |   |
|----------------------|---|
| data                 | Data frame or matrix containing the variables in the model.                                       |
| bic                  | Numeric value with the corresponding BIC.   |
| mcmc_inf             | Details about the number of MCMC iterations, burn-in periods, and thinning intervals.             |
| map_inf              | The log maximum a posteriori (MAP) value and the iteration number at which this MAP value occurs. |
| beta_estimate        | Posterior estimates of the beta parameter.  |
| theta_estimate       | Posterior estimates of the theta parameter.   |
| sigma_theta_estimate | Posterior estimates of the standard deviation of theta.   |
| z_estimate           | Posterior estimates of the z parameter.   |

|              |  |
|--------------|--|
| w_estimate   | Posterior estimates of the w parameter.  |
| beta         | Posterior samples of the beta parameter.   |
| theta        | Posterior samples of the theta parameter.  |
| theta_sd     | Posterior samples of the standard deviation of theta.  |
| z            | Posterior samples of the z parameter, represented as a 3-dimensional matrix where the last axis denotes the dimension of the latent space. |
| w            | Posterior samples of the w parameter, represented as a 3-dimensional matrix where the last axis denotes the dimension of the latent space. |
| accept_beta  | Acceptance ratio for the beta parameter.   |
| accept_theta | Acceptance ratio for the theta parameter.  |
| accept_z     | Acceptance ratio for the z parameter.  |
| accept_w     | Acceptance ratio for the w parameter.  |

### Examples

```
# generate example item response matrix
data <- matrix(rbinom(500, size = 1, prob = 0.5), ncol=10, nrow=50)

lsirm_result <- lsirm1pl_fixed_gamma(data)

# The code following can achieve the same result.
lsirm_result <- lsirm(data ~ lsirm1pl(spikenslab = FALSE, fixed_gamma = TRUE))
```

---

```
lsirm1pl_fixed_gamma_mar
```

*1PL LSIRM fixing gamma to 1 for missing at random data.*

---

### Description

[lsirm1pl\\_fixed\\_gamma\\_mar](#) is used to fit LSIRM with gamma fixed to 1 in incomplete data assumed to be missing at random. [lsirm1pl\\_fixed\\_gamma\\_mar](#) factorizes item response matrix into column-wise item effect, row-wise respondent effect and further embeds interaction effect in a latent space, while considering the missing element under the assumption of missing at random. The resulting latent space provides an interaction map that represents interactions between respondents and items.

### Usage

```
lsirm1pl_fixed_gamma_mar(
  data,
  ndim = 2,
  niter = 15000,
  nburn = 2500,
  nthin = 5,
  nprint = 500,
```

```

    jump_beta = 0.4,
    jump_theta = 1,
    jump_z = 0.5,
    jump_w = 0.5,
    pr_mean_beta = 0,
    pr_sd_beta = 1,
    pr_mean_theta = 0,
    pr_a_theta = 0.001,
    pr_b_theta = 0.001,
    missing.val = 99,
    verbose = FALSE
)

```

### Arguments

|               |   |
|---------------|---|
| data          | Matrix; a binary or continuous item response matrix for analysis. Each row represents a respondent, and each column contains responses to the corresponding item. |
| ndim          | Integer; the dimension of the latent space. Default is 2.   |
| niter         | Integer; the total number of MCMC iterations to run. Default is 15000.  |
| nburn         | Integer; the number of initial MCMC iterations to discard as burn-in. Default is 2500.  |
| nthin         | Integer; the number of MCMC iterations to thin. Default is 5.   |
| nprint        | Integer; the interval at which MCMC samples are displayed during execution. Default is 500.   |
| jump_beta     | Numeric; the jumping rule for the beta proposal density. Default is 0.4.  |
| jump_theta    | Numeric; the jumping rule for the theta proposal density. Default is 1.0.   |
| jump_z        | Numeric; the jumping rule for the z proposal density. Default is 0.5.   |
| jump_w        | Numeric; the jumping rule for the w proposal density. Default is 0.5.   |
| pr_mean_beta  | Numeric; the mean of the normal prior for beta. Default is 0.   |
| pr_sd_beta    | Numeric; the standard deviation of the normal prior for beta. Default is 1.0.   |
| pr_mean_theta | Numeric; the mean of the normal prior for theta. Default is 0.  |
| pr_a_theta    | Numeric; the shape parameter of the inverse gamma prior for the variance of theta. Default is 0.001.  |
| pr_b_theta    | Numeric; the scale parameter of the inverse gamma prior for the variance of theta. Default is 0.001.  |
| missing.val   | Numeric; a number to replace missing values. Default is 99.   |
| verbose       | Logical; If TRUE, MCMC samples are printed for each nprint. default value is FALSE.   |

## Details

lsirm1pl\_fixed\_gamma\_mar models the probability of correct response by respondent  $j$  to item  $i$  with item effect  $\beta_i$ , respondent effect  $\theta_j$  and the distance between latent position  $w_i$  of item  $i$  and latent position  $z_j$  of respondent  $j$  in the shared metric space:

$$\text{logit}(P(Y_{j,i} = 1 | \theta_j, \beta_i, z_j, w_i)) = \theta_j + \beta_i - ||z_j - w_i||$$

Under the assumption of missing at random, the model takes the missing element into consideration in the sampling procedure. For the details of missing at random assumption and data augmentation, see References.

## Value

lsirm1pl\_fixed\_gamma\_mar returns an object of list containing the following components:

|                      |  |
|----------------------|--|
| data                 | Data frame or matrix containing the variables in the model.  |
| missing.val          | A number to replace missing values.  |
| bic                  | Numeric value with the corresponding BIC.  |
| mcmc_inf             | Details about the number of MCMC iterations, burn-in periods, and thinning intervals.  |
| map_inf              | The log maximum a posteriori (MAP) value and the iteration number at which this MAP value occurs.  |
| beta_estimate        | Posterior estimates of the beta parameter.   |
| theta_estimate       | Posterior estimates of the theta parameter.  |
| sigma_theta_estimate | Posterior estimates of the standard deviation of theta.  |
| z_estimate           | Posterior estimates of the z parameter.  |
| w_estimate           | Posterior estimates of the w parameter.  |
| imp_estimate         | Probability of imputating a missing value with 1.  |
| beta                 | Posterior samples of the beta parameter.   |
| theta                | Posterior samples of the theta parameter.  |
| theta_sd             | Posterior samples of the standard deviation of theta.  |
| z                    | Posterior samples of the z parameter, represented as a 3-dimensional matrix where the last axis denotes the dimension of the latent space. |
| w                    | Posterior samples of the w parameter, represented as a 3-dimensional matrix where the last axis denotes the dimension of the latent space. |
| imp                  | Imputation for missing Values using posterior samples.   |
| accept_beta          | Acceptance ratio for the beta parameter.   |
| accept_theta         | Acceptance ratio for the theta parameter.  |
| accept_z             | Acceptance ratio for the z parameter.  |
| accept_w             | Acceptance ratio for the w parameter.  |

## References

Little, R. J., & Rubin, D. B. (2019). Statistical analysis with missing data (Vol. 793). John Wiley & Sons.

## Examples

```
# generate example item response matrix
data      <- matrix(rbinom(500, size = 1, prob = 0.5),ncol=10,nrow=50)

# generate example missing indicator matrix
missing_mat  <- matrix(rbinom(500, size = 1, prob = 0.2),ncol=10,nrow=50)

# make missing value with missing indicator matrix
data[missing_mat==1] <- 99

lsirm_result <- lsirm1pl_fixed_gamma_mar(data)

# The code following can achieve the same result.
lsirm_result <- lsirm(data ~ lsirm1pl(spikenslab = FALSE, fixed_gamma = TRUE,
missing_data = "mar", missing.val = 99))
```

---

```
lsirm1pl_fixed_gamma_mcar
```

*1PL LSIRM fixing gamma to 1 for missing completely at random data.*

---

## Description

[lsirm1pl\\_fixed\\_gamma\\_mcar](#) is used to fit LSIRM with gamma fixed to 1 in incomplete data assumed to be missing completely at random. [lsirm1pl\\_fixed\\_gamma\\_mcar](#) factorizes item response matrix into column-wise item effect, row-wise respondent effect and further embeds interaction effect in a latent space, while ignoring the missing element under the assumption of missing completely at random. The resulting latent space provides an interaction map that represents interactions between respondents and items.

## Usage

```
lsirm1pl_fixed_gamma_mcar(
  data,
  ndim = 2,
  niter = 15000,
  nburn = 2500,
  nthin = 5,
  nprint = 500,
  jump_beta = 0.4,
  jump_theta = 1,
  jump_z = 0.5,
  jump_w = 0.5,
```

```

pr_mean_beta = 0,
pr_sd_beta = 1,
pr_mean_theta = 0,
pr_a_theta = 0.001,
pr_b_theta = 0.001,
missing.val = 99,
verbose = FALSE
)

```

### Arguments

|               |   |
|---------------|---|
| data          | Matrix; a binary or continuous item response matrix for analysis. Each row represents a respondent, and each column contains responses to the corresponding item. |
| ndim          | Integer; the dimension of the latent space. Default is 2.   |
| niter         | Integer; the total number of MCMC iterations to run. Default is 15000.  |
| nburn         | Integer; the number of initial MCMC iterations to discard as burn-in. Default is 2500.  |
| nthin         | Integer; the number of MCMC iterations to thin. Default is 5.   |
| nprint        | Integer; the interval at which MCMC samples are displayed during execution. Default is 500.   |
| jump_beta     | Numeric; the jumping rule for the beta proposal density. Default is 0.4.  |
| jump_theta    | Numeric; the jumping rule for the theta proposal density. Default is 1.0.   |
| jump_z        | Numeric; the jumping rule for the z proposal density. Default is 0.5.   |
| jump_w        | Numeric; the jumping rule for the w proposal density. Default is 0.5.   |
| pr_mean_beta  | Numeric; the mean of the normal prior for beta. Default is 0.   |
| pr_sd_beta    | Numeric; the standard deviation of the normal prior for beta. Default is 1.0.   |
| pr_mean_theta | Numeric; the mean of the normal prior for theta. Default is 0.  |
| pr_a_theta    | Numeric; the shape parameter of the inverse gamma prior for the variance of theta. Default is 0.001.  |
| pr_b_theta    | Numeric; the scale parameter of the inverse gamma prior for the variance of theta. Default is 0.001.  |
| missing.val   | Numeric; a number to replace missing values. Default is 99.   |
| verbose       | Logical; If TRUE, MCMC samples are printed for each nprint. default value is FALSE  |

### Details

lsirm1pl\_fixed\_gamma\_mcar models the probability of correct response by respondent  $j$  to item  $i$  with item effect  $\beta_i$ , respondent effect  $\theta_j$  and the distance between latent position  $w_i$  of item  $i$  and latent position  $z_j$  of respondent  $j$  in the shared metric space:

$$\text{logit}(P(Y_{j,i} = 1 | \theta_j, \beta_i, z_j, w_i)) = \theta_j + \beta_i - ||z_j - w_i||$$

Under the assumption of missing completely at random, the model ignores the missing element in doing inference. For the details of missing completely at random assumption and data augmentation, see References.



**Value**

lsirm1pl\_fixed\_gamma\_mcar returns an object of list containing the following components:

|                      |  |
|----------------------|--|
| data                 | Data frame or matrix containing the variables in the model.  |
| missing.val          | A number to replace missing values.  |
| bic                  | Numeric value with the corresponding BIC.  |
| mcmc_inf             | Details about the number of MCMC iterations, burn-in periods, and thinning intervals.  |
| map_inf              | The log maximum a posteriori (MAP) value and the iteration number at which this MAP value occurs.  |
| beta_estimate        | Posterior estimates of the beta parameter.   |
| theta_estimate       | Posterior estimates of the theta parameter.  |
| sigma_theta_estimate | Posterior estimates of the standard deviation of theta.  |
| z_estimate           | Posterior estimates of the z parameter.  |
| w_estimate           | Posterior estimates of the w parameter.  |
| beta                 | Posterior samples of the beta parameter.   |
| theta                | Posterior samples of the theta parameter.  |
| theta_sd             | Posterior samples of the standard deviation of theta.  |
| z                    | Posterior samples of the z parameter, represented as a 3-dimensional matrix where the last axis denotes the dimension of the latent space. |
| w                    | Posterior samples of the w parameter, represented as a 3-dimensional matrix where the last axis denotes the dimension of the latent space. |
| accept_beta          | Acceptance ratio for the beta parameter.   |
| accept_theta         | Acceptance ratio for the theta parameter.  |
| accept_z             | Acceptance ratio for the z parameter.  |
| accept_w             | Acceptance ratio for the w parameter.  |

**References**

Little, R. J., & Rubin, D. B. (2019). Statistical analysis with missing data (Vol. 793). John Wiley & Sons.

**Examples**

```
# generate example item response matrix
data <- matrix(rbinom(500, size = 1, prob = 0.5), ncol=10, nrow=50)

# generate example missing indicator matrix
missing_mat <- matrix(rbinom(500, size = 1, prob = 0.2), ncol=10, nrow=50)

# make missing value with missing indicator matrix
data[missing_mat==1] <- 99
```

```
lsirm_result <- lsirm1pl_fixed_gamma_mcar(data)

# The code following can achieve the same result.
lsirm_result <- lsirm(data ~ lsirm1pl(spikenslab = FALSE, fixed_gamma = TRUE,
missing_data = "mcar", missing.val = 99))
```

---

lsirm1pl\_mar

---

*1PL LSIRM for missing at random data.*


---

### Description

[lsirm1pl\\_mar](#) is used to fit 1PL LSIRM in incomplete data assumed to be missing at random. [lsirm1pl\\_mar](#) factorizes item response matrix into column-wise item effect, row-wise respondent effect and further embeds interaction effect in a latent space, while considering the missing element under the assumption of missing at random. The resulting latent space provides an interaction map that represents interactions between respondents and items.

### Usage

```
lsirm1pl_mar(
  data,
  ndim = 2,
  niter = 15000,
  nburn = 2500,
  nthin = 5,
  nprint = 500,
  jump_beta = 0.4,
  jump_theta = 1,
  jump_gamma = 0.025,
  jump_z = 0.5,
  jump_w = 0.5,
  pr_mean_beta = 0,
  pr_sd_beta = 1,
  pr_mean_theta = 0,
  pr_mean_gamma = 0.5,
  pr_sd_gamma = 1,
  pr_a_theta = 0.001,
  pr_b_theta = 0.001,
  missing.val = 99,
  verbose = FALSE
)
```

### Arguments

|      |   |
|------|---|
| data | Matrix; a binary or continuous item response matrix for analysis. Each row represents a respondent, and each column contains responses to the corresponding item. |
|------|---|

|               |  |
|---------------|--|
| ndim          | Integer; the dimension of the latent space. Default is 2.  |
| niter         | Integer; the total number of MCMC iterations to run. Default is 15000.                               |
| nburn         | Integer; the number of initial MCMC iterations to discard as burn-in. Default is 2500.               |
| nthin         | Integer; the number of MCMC iterations to thin. Default is 5.  |
| nprint        | Integer; the interval at which MCMC samples are displayed during execution. Default is 500.          |
| jump_beta     | Numeric; the jumping rule for the beta proposal density. Default is 0.4.                             |
| jump_theta    | Numeric; the jumping rule for the theta proposal density. Default is 1.0.                            |
| jump_gamma    | Numeric; the jumping rule for the gamma proposal density. Default is 0.025                           |
| jump_z        | Numeric; the jumping rule for the z proposal density. Default is 0.5.                                |
| jump_w        | Numeric; the jumping rule for the w proposal density. Default is 0.5.                                |
| pr_mean_beta  | Numeric; the mean of the normal prior for beta. Default is 0.  |
| pr_sd_beta    | Numeric; the standard deviation of the normal prior for beta. Default is 1.0.                        |
| pr_mean_theta | Numeric; the mean of the normal prior for theta. Default is 0.                                       |
| pr_mean_gamma | Numeric; mean of log normal prior for gamma. Default is 0.5.   |
| pr_sd_gamma   | Numeric; standard deviation of log normal prior for gamma. Default is 1.0.                           |
| pr_a_theta    | Numeric; the shape parameter of the inverse gamma prior for the variance of theta. Default is 0.001. |
| pr_b_theta    | Numeric; the scale parameter of the inverse gamma prior for the variance of theta. Default is 0.001. |
| missing.val   | Numeric; a number to replace missing values. Default is 99.  |
| verbose       | Logical; If TRUE, MCMC samples are printed for each nprint. default value is FALSE.                  |

## Details

lsirm1pl\_mar models the probability of correct response by respondent  $j$  to item  $i$  with item effect  $\beta_i$ , respondent effect  $\theta_j$  and the distance between latent position  $w_i$  of item  $i$  and latent position  $z_j$  of respondent  $j$  in the shared metric space, with  $\gamma$  represents the weight of the distance term:

$$\text{logit}(P(Y_{j,i} = 1|\theta_j, \beta_i, \gamma, z_j, w_i)) = \theta_j + \beta_i - \gamma||z_j - w_i||$$

Under the assumption of missing at random, the model takes the missing element into consideration in the sampling procedure. For the details of missing at random assumption and data augmentation, see References.

## Value

lsirm1pl\_mar returns an object of list containing the following components:

|             |   |
|-------------|---|
| data        | Data frame or matrix containing the variables in the model. |
| missing.val | A number to replace missing values.                         |
| bic         | Numeric value with the corresponding BIC.                   |

|                      |  |
|----------------------|--|
| mcmc_inf             | Details about the number of MCMC iterations, burn-in periods, and thinning intervals.  |
| map_inf              | The log maximum a posteriori (MAP) value and the iteration number at which this MAP value occurs.  |
| beta_estimate        | Posterior estimates of the beta parameter.   |
| theta_estimate       | Posterior estimates of the theta parameter.  |
| sigma_theta_estimate | Posterior estimates of the standard deviation of theta.  |
| gamma_estimate       | posterior estimates of gamma parameter.  |
| z_estimate           | Posterior estimates of the z parameter.  |
| w_estimate           | Posterior estimates of the w parameter.  |
| imp_estimate         | Probability of imputating a missing value with 1.  |
| beta                 | Posterior samples of the beta parameter.   |
| theta                | Posterior samples of the theta parameter.  |
| gamma                | Posterior samples of the gamma parameter.  |
| theta_sd             | Posterior samples of the standard deviation of theta.  |
| z                    | Posterior samples of the z parameter, represented as a 3-dimensional matrix where the last axis denotes the dimension of the latent space. |
| w                    | Posterior samples of the w parameter, represented as a 3-dimensional matrix where the last axis denotes the dimension of the latent space. |
| imp                  | Imputation for missing Values using posterior samples.   |
| accept_beta          | Acceptance ratio for the beta parameter.   |
| accept_theta         | Acceptance ratio for the theta parameter.  |
| accept_z             | Acceptance ratio for the z parameter.  |
| accept_w             | Acceptance ratio for the w parameter.  |
| accept_gamma         | Acceptance ratio for the gamma parameter.  |

## References

Little, R. J., & Rubin, D. B. (2019). Statistical analysis with missing data (Vol. 793). John Wiley & Sons.

## Examples

```
# generate example item response matrix
data <- matrix(rbinom(500, size = 1, prob = 0.5),ncol=10,nrow=50)

# generate example missing indicator matrix
missing_mat <- matrix(rbinom(500, size = 1, prob = 0.2),ncol=10,nrow=50)

# make missing value with missing indicator matrix
data[missing_mat==1] <- 99

lsirm_result <- lsirm1pl_mar(data)
```

```
# The code following can achieve the same result.
lsirm_result <- lsirm(data ~ lsirm1pl(spikenslab = FALSE, fixed_gamma = FALSE,
missing_data = 'mar', missing.val = 99))
```

---

|                 |  |
|-----------------|--|
| lsirm1pl_mar_ss | <i>1PL LSIRM with model selection approach for missing at random data.</i> |
|-----------------|--|

---

## Description

[lsirm1pl\\_mar\\_ss](#) is used to fit 1PL LSIRM with model selection approach based on spike-and-slab priors in incomplete data assumed to be missing at random. [lsirm1pl\\_mar\\_ss](#) factorizes item response matrix into column-wise item effect, row-wise respondent effect and further embeds interaction effect in a latent space, while considering the missing element under the assumption of missing at random. The resulting latent space provides an interaction map that represents interactions between respondents and items.

## Usage

```
lsirm1pl_mar_ss(
  data,
  ndim = 2,
  niter = 15000,
  nburn = 2500,
  nthin = 5,
  nprint = 500,
  jump_beta = 0.4,
  jump_theta = 1,
  jump_gamma = 1,
  jump_z = 0.5,
  jump_w = 0.5,
  pr_mean_beta = 0,
  pr_sd_beta = 1,
  pr_mean_theta = 0,
  pr_spike_mean = -3,
  pr_spike_sd = 1,
  pr_slab_mean = 0.5,
  pr_slab_sd = 1,
  pr_a_theta = 0.001,
  pr_b_theta = 0.001,
  pr_xi_a = 1,
  pr_xi_b = 1,
  missing.val = 99,
  verbose = FALSE
)
```

### Arguments

|               |   |
|---------------|---|
| data          | Matrix; a binary or continuous item response matrix for analysis. Each row represents a respondent, and each column contains responses to the corresponding item. |
| ndim          | Integer; the dimension of the latent space. Default is 2.   |
| niter         | Integer; the total number of MCMC iterations to run. Default is 15000.  |
| nburn         | Integer; the number of initial MCMC iterations to discard as burn-in. Default is 2500.  |
| nthin         | Integer; the number of MCMC iterations to thin. Default is 5.   |
| nprint        | Integer; the interval at which MCMC samples are displayed during execution. Default is 500.   |
| jump_beta     | Numeric; the jumping rule for the beta proposal density. Default is 0.4.  |
| jump_theta    | Numeric; the jumping rule for the theta proposal density. Default is 1.0.   |
| jump_gamma    | Numeric; the jumping rule for the gamma proposal density. Default is 1.0.   |
| jump_z        | Numeric; the jumping rule for the z proposal density. Default is 0.5.   |
| jump_w        | Numeric; the jumping rule for the w proposal density. Default is 0.5.   |
| pr_mean_beta  | Numeric; the mean of the normal prior for beta. Default is 0.   |
| pr_sd_beta    | Numeric; the standard deviation of the normal prior for beta. Default is 1.0.   |
| pr_mean_theta | Numeric; the mean of the normal prior for theta. Default is 0.  |
| pr_spike_mean | Numeric; the mean of spike prior for log gamma. Default is -3.  |
| pr_spike_sd   | Numeric; the standard deviation of spike prior for log gamma. Default is 1.   |
| pr_slab_mean  | Numeric; the mean of spike prior for log gamma. Default is 0.5.   |
| pr_slab_sd    | Numeric; the standard deviation of spike prior for log gamma. Default is 1.   |
| pr_a_theta    | Numeric; the shape parameter of the inverse gamma prior for the variance of theta. Default is 0.001.  |
| pr_b_theta    | Numeric; the scale parameter of the inverse gamma prior for the variance of theta. Default is 0.001.  |
| pr_xi_a       | Numeric; the first shape parameter of beta prior for latent variable xi. Default is 1.  |
| pr_xi_b       | Numeric; the second shape parameter of beta prior for latent variable xi. Default is 1.   |
| missing.val   | Numeric; a number to replace missing values. Default is 99.   |
| verbose       | Logical; If TRUE, MCMC samples are printed for each nprint. Default is FALSE.   |

### Details

lsirm1pl\_mar\_ss models the probability of correct response by respondent  $j$  to item  $i$  with item effect  $\beta_i$ , respondent effect  $\theta_j$  and the distance between latent position  $w_i$  of item  $i$  and latent position  $z_j$  of respondent  $j$  in the shared metric space, with  $\gamma$  represents the weight of the distance term:

$$\text{logit}(P(Y_{j,i} = 1 | \theta_j, \beta_i, \gamma, z_j, w_i)) = \theta_j + \beta_i - \gamma ||z_j - w_i||$$

Under the assumption of missing at random, the model takes the missing element into consideration in the sampling procedure. For the details of missing at random assumption and data augmentation, see References. lsirm1pl\_mar\_ss model include model selection approach based on spike-and-slab priors for log gamma. For detail of spike-and-slab priors, see References.

### Value

lsirm1pl\_mar\_ss returns an object of list containing the following components:

|                      |   |
|----------------------|---|
| data                 | Data frame or matrix containing the variables in the model.   |
| missing.val          | A number to replace missing values.   |
| bic                  | Numeric value with the corresponding BIC.   |
| mcmc_inf             | Details about the number of MCMC iterations, burn-in periods, and thinning intervals.   |
| map_inf              | The log maximum a posteriori (MAP) value and the iteration number at which this MAP value occurs.   |
| beta_estimate        | Posterior estimates of the beta parameter.  |
| theta_estimate       | Posterior estimates of the theta parameter.   |
| sigma_theta_estimate | Posterior estimates of the standard deviation of theta.   |
| gamma_estimate       | posterior estimates of gamma parameter.   |
| z_estimate           | Posterior estimates of the z parameter.   |
| w_estimate           | Posterior estimates of the w parameter.   |
| beta                 | Posterior samples of the beta parameter.  |
| theta                | Posterior samples of the theta parameter.   |
| gamma                | Posterior samples of the gamma parameter.   |
| theta_sd             | Posterior samples of the standard deviation of theta.   |
| z                    | Posterior samples of the z parameter, represented as a 3-dimensional matrix where the last axis denotes the dimension of the latent space.  |
| w                    | Posterior samples of the w parameter, represented as a 3-dimensional matrix where the last axis denotes the dimension of the latent space.  |
| pi                   | Posterior samples of phi which is indicator of spike and slab prior. If phi is 1, log gamma follows the slab prior, otherwise follows the spike prior.                              |
| imp                  | Imputation for missing Values using posterior samples.  |
| accept_beta          | Acceptance ratio for the beta parameter.  |
| accept_theta         | Acceptance ratio for the theta parameter.   |
| accept_z             | Acceptance ratio for the z parameter.   |
| accept_w             | Acceptance ratio for the w parameter.   |
| accept_gamma         | Acceptance ratio for the gamma parameter.   |
| pi_estimate          | Posterior estimation of phi. inclusion probability of gamma. if estimation of phi is less than 0.5, choose Rasch model with gamma = 0, otherwise latent space model with gamma > 0. |
| imp_estimate         | Probability of imputating a missing value with 1.   |

## References

Little, R. J., & Rubin, D. B. (2019). Statistical analysis with missing data (Vol. 793). John Wiley & Sons. Ishwaran, H., & Rao, J. S. (2005). Spike and slab variable selection: frequentist and Bayesian strategies. The Annals of Statistics, 33(2), 730-773.

## Examples

```
# generate example item response matrix
data      <- matrix(rbinom(500, size = 1, prob = 0.5),ncol=10,nrow=50)

# generate example missing indicator matrix
missing_mat  <- matrix(rbinom(500, size = 1, prob = 0.2),ncol=10,nrow=50)

# make missing value with missing indicator matrix
data[missing_mat==1] <- 99

lsirm_result <- lsirm1pl_mar_ss(data)

# The code following can achieve the same result.
lsirm_result <- lsirm(data ~ lsirm1pl(spikenslab = TRUE, fixed_gamma = FALSE,
missing_data = 'mar', missing = 99))
```

---

lsirm1pl\_mcar

---

1PL LSIRM for missing completely at random data.

---

## Description

[lsirm1pl\\_mcar](#) is used to fit 1PL LSIRM in incomplete data assumed to be missing completely at random. [lsirm1pl\\_mcar](#) factorizes item response matrix into column-wise item effect, row-wise respondent effect and further embeds interaction effect in a latent space, while ignoring the missing element under the assumption of missing completely at random. The resulting latent space provides an interaction map that represents interactions between respondents and items.

## Usage

```
lsirm1pl_mcar(
  data,
  ndim = 2,
  niter = 15000,
  nburn = 2500,
  nthin = 5,
  nprint = 500,
  jump_beta = 0.4,
  jump_theta = 1,
  jump_gamma = 0.025,
  jump_z = 0.5,
  jump_w = 0.5,
```



```

pr_mean_beta = 0,
pr_sd_beta = 1,
pr_mean_theta = 0,
pr_mean_gamma = 0.5,
pr_sd_gamma = 1,
pr_a_theta = 0.001,
pr_b_theta = 0.001,
missing.val = 99,
verbose = FALSE
)

```

### Arguments

|               |   |
|---------------|---|
| data          | Matrix; a binary or continuous item response matrix for analysis. Each row represents a respondent, and each column contains responses to the corresponding item. |
| ndim          | Integer; the dimension of the latent space. Default is 2.   |
| niter         | Integer; the total number of MCMC iterations to run. Default is 15000.  |
| nburn         | Integer; the number of initial MCMC iterations to discard as burn-in. Default is 2500.  |
| nthin         | Integer; the number of MCMC iterations to thin. Default is 5.   |
| nprint        | Integer; the interval at which MCMC samples are displayed during execution. Default is 500.   |
| jump_beta     | Numeric; the jumping rule for the beta proposal density. Default is 0.4.  |
| jump_theta    | Numeric; the jumping rule for the theta proposal density. Default is 1.0.   |
| jump_gamma    | Numeric; the jumping rule for the gamma proposal density. Default is 0.025.   |
| jump_z        | Numeric; the jumping rule for the z proposal density. Default is 0.5.   |
| jump_w        | Numeric; the jumping rule for the w proposal density. Default is 0.5.   |
| pr_mean_beta  | Numeric; the mean of the normal prior for beta. Default is 0.   |
| pr_sd_beta    | Numeric; the standard deviation of the normal prior for beta. Default is 1.0.   |
| pr_mean_theta | Numeric; the mean of the normal prior for theta. Default is 0.  |
| pr_mean_gamma | Numeric; mean of log normal prior for gamma. Default is 0.5.  |
| pr_sd_gamma   | Numeric; standard deviation of log normal prior for gamma. Default is 1.0.  |
| pr_a_theta    | Numeric; the shape parameter of the inverse gamma prior for the variance of theta. Default is 0.001.  |
| pr_b_theta    | Numeric; the scale parameter of the inverse gamma prior for the variance of theta. Default is 0.001.  |
| missing.val   | Numeric; A number to replace missing values. Default is 99.   |
| verbose       | Logical; If TRUE, MCMC samples are printed for each nprint. Default is FALSE.   |

## Details

lsirm1pl\_mcar models the probability of correct response by respondent  $j$  to item  $i$  with item effect  $\beta_i$ , respondent effect  $\theta_j$  and the distance between latent position  $w_i$  of item  $i$  and latent position  $z_j$  of respondent  $j$  in the shared metric space, with  $\gamma$  represents the weight of the distance term:

$$\text{logit}(P(Y_{j,i} = 1 | \theta_j, \beta_i, \gamma, z_j, w_i)) = \theta_j + \beta_i - \gamma ||z_j - w_i||$$

Under the assumption of missing completely at random, the model ignores the missing element in doing inference. For the details of missing completely at random assumption and data augmentation, see References.

## Value

lsirm1pl\_mcar returns an object of list containing the following components:

|                      |  |
|----------------------|--|
| data                 | A data frame or matrix containing the variables used in the model.   |
| missing.val          | A number to replace missing values.  |
| bic                  | Numeric value with the corresponding BIC.  |
| mcmc_inf             | Details about the number of MCMC iterations, burn-in periods, and thinning intervals.  |
| map_inf              | The log maximum a posteriori (MAP) value and the iteration number at which this MAP value occurs.  |
| beta_estimate        | Posterior estimates of the beta parameter.   |
| theta_estimate       | Posterior estimates of the theta parameter.  |
| sigma_theta_estimate | Posterior estimates of the standard deviation of theta.  |
| gamma_estimate       | Posterior estimates of gamma parameter.  |
| z_estimate           | Posterior estimates of the z parameter.  |
| w_estimate           | Posterior estimates of the w parameter.  |
| beta                 | Posterior samples of the beta parameter.   |
| theta                | Posterior samples of the theta parameter.  |
| theta_sd             | Posterior samples of the standard deviation of theta.  |
| gamma                | Posterior samples of the gamma parameter.  |
| z                    | Posterior samples of the z parameter, represented as a 3-dimensional matrix where the last axis denotes the dimension of the latent space. |
| w                    | Posterior samples of the w parameter, represented as a 3-dimensional matrix where the last axis denotes the dimension of the latent space. |
| accept_beta          | Acceptance ratio for the beta parameter.   |
| accept_theta         | Acceptance ratio for the theta parameter.  |
| accept_z             | Acceptance ratio for the z parameter.  |
| accept_w             | Acceptance ratio for the w parameter.  |
| accept_gamma         | Acceptance ratio for the gamma parameter.  |

## References

Little, R. J., & Rubin, D. B. (2019). Statistical analysis with missing data (Vol. 793). John Wiley & Sons.

## Examples

```
# generate example item response matrix
data      <- matrix(rbinom(500, size = 1, prob = 0.5),ncol=10,nrow=50)

# generate example missing indicator matrix
missing_mat  <- matrix(rbinom(500, size = 1, prob = 0.2),ncol=10,nrow=50)

# make missing value with missing indicator matrix
data[missing_mat==1] <- 99

lsirm_result <- lsirm1pl_mcar(data)

# The code following can achieve the same result.
lsirm_result <- lsirm(data ~ lsirm1pl(spikenslab = FALSE, fixed_gamma = FALSE,
missing_data = 'mcar', missing.val = 99))
```

---

|                  |   |
|------------------|---|
| lsirm1pl_mcar_ss | <i>1PL LSIRM with model selection approach for missing completely at random data.</i> |
|------------------|---|

---

## Description

[lsirm1pl\\_mcar\\_ss](#) is used to fit 1PL LSIRM with model selection approach based on spike-and-slab priors in incomplete data assumed to be missing completely at random. [lsirm1pl\\_mcar\\_ss](#) factorizes item response matrix into column-wise item effect, row-wise respondent effect and further embeds interaction effect in a latent space, while ignoring the missing element under the assumption of missing completely at random. The resulting latent space provides an interaction map that represents interactions between respondents and items.

## Usage

```
lsirm1pl_mcar_ss(
  data,
  ndim = 2,
  niter = 15000,
  nburn = 2500,
  nthin = 5,
  nprint = 500,
  jump_beta = 0.4,
  jump_theta = 1,
  jump_gamma = 1,
  jump_z = 0.5,
```

```

jump_w = 0.5,
pr_mean_beta = 0,
pr_sd_beta = 1,
pr_mean_theta = 0,
pr_spike_mean = -3,
pr_spike_sd = 1,
pr_slab_mean = 0.5,
pr_slab_sd = 1,
pr_a_theta = 0.001,
pr_b_theta = 0.001,
pr_xi_a = 1,
pr_xi_b = 1,
missing.val = 99,
verbose = FALSE
)

```

### Arguments

|               |   |
|---------------|---|
| data          | Matrix; a binary or continuous item response matrix for analysis. Each row represents a respondent, and each column contains responses to the corresponding item. |
| ndim          | Integer; the dimension of the latent space. Default is 2.   |
| niter         | Integer; the total number of MCMC iterations to run. Default is 15000.  |
| nburn         | Integer; the number of initial MCMC iterations to discard as burn-in. Default is 2500.  |
| nthin         | Integer; the number of MCMC iterations to thin. Default is 5.   |
| nprint        | Integer; the interval at which MCMC samples are displayed during execution. Default is 500.   |
| jump_beta     | Numeric; the jumping rule for the beta proposal density. Default is 0.4.  |
| jump_theta    | Numeric; the jumping rule for the theta proposal density. Default is 1.0.   |
| jump_gamma    | Numeric; the jumping rule for the gamma proposal density. Default is 1.0.   |
| jump_z        | Numeric; the jumping rule for the z proposal density. Default is 0.5.   |
| jump_w        | Numeric; the jumping rule for the w proposal density. Default is 0.5.   |
| pr_mean_beta  | Numeric; the mean of the normal prior for beta. Default is 0.   |
| pr_sd_beta    | Numeric; the standard deviation of the normal prior for beta. Default is 1.0.   |
| pr_mean_theta | Numeric; the mean of the normal prior for theta. Default is 0.  |
| pr_spike_mean | Numeric; the mean of spike prior for log gamma. Default is -3.  |
| pr_spike_sd   | Numeric; the standard deviation of spike prior for log gamma. Default is 1.   |
| pr_slab_mean  | Numeric; the mean of spike prior for log gamma. Default is 0.5.   |
| pr_slab_sd    | Numeric; the standard deviation of spike prior for log gamma. Default is 1.   |
| pr_a_theta    | Numeric; the shape parameter of the inverse gamma prior for the variance of theta. Default is 0.001.  |

|             |  |
|-------------|--|
| pr_b_theta  | Numeric; the scale parameter of the inverse gamma prior for the variance of theta. Default is 0.001. |
| pr_xi_a     | Numeric; the first shape parameter of beta prior for latent variable xi. Default is 1.               |
| pr_xi_b     | Numeric; the second shape parameter of beta prior for latent variable xi. Default is 1.              |
| missing.val | Numeric; a number to replace missing values. Default is 99.  |
| verbose     | Logical; If TRUE, MCMC samples are printed for each nprint. Default is FALSE.                        |

### Details

lsirm1pl\_mcar\_ss models the probability of correct response by respondent  $j$  to item  $i$  with item effect  $\beta_i$ , respondent effect  $\theta_j$  and the distance between latent position  $w_i$  of item  $i$  and latent position  $z_j$  of respondent  $j$  in the shared metric space, with  $\gamma$  represents the weight of the distance term:

$$\text{logit}(P(Y_{j,i} = 1 | \theta_j, \beta_i, \gamma, z_j, w_i)) = \theta_j + \beta_i - \gamma ||z_j - w_i||$$

Under the assumption of missing completely at random, the model ignores the missing element in doing inference. For the details of missing completely at random assumption and data augmentation, see References. lsirm1pl\_mcar\_ss model include model selection approach based on spike-and-slab priors for log gamma. For detail of spike-and-slab priors, see References.

### Value

lsirm1pl\_mcar\_ss returns an object of list containing the following components:

|                      |   |
|----------------------|---|
| data                 | Data frame or matrix containing the variables in the model.                                       |
| missing.val          | A number to replace missing values.   |
| bic                  | Numeric value with the corresponding BIC.   |
| mcmc_inf             | Details about the number of MCMC iterations, burn-in periods, and thinning intervals.             |
| map_inf              | The log maximum a posteriori (MAP) value and the iteration number at which this MAP value occurs. |
| beta_estimate        | Posterior estimates of the beta parameter.  |
| theta_estimate       | Posterior estimates of the theta parameter.   |
| sigma_theta_estimate | Posterior estimates of the standard deviation of theta.   |
| gamma_estimate       | posterior estimates of gamma parameter.   |
| z_estimate           | Posterior estimates of the z parameter.   |
| w_estimate           | Posterior estimates of the w parameter.   |
| beta                 | Posterior samples of the beta parameter.  |
| theta                | Posterior samples of the theta parameter.   |
| gamma                | Posterior samples of the gamma parameter.   |

|              |  |
|--------------|--|
| theta_sd     | Posterior samples of the standard deviation of theta.  |
| z            | Posterior samples of the z parameter, represented as a 3-dimensional matrix where the last axis denotes the dimension of the latent space.             |
| w            | Posterior samples of the w parameter, represented as a 3-dimensional matrix where the last axis denotes the dimension of the latent space.             |
| pi           | Posterior samples of phi which is indicator of spike and slab prior. If phi is 1, log gamma follows the slab prior, otherwise follows the spike prior. |
| accept_beta  | Acceptance ratio for the beta parameter.   |
| accept_theta | Acceptance ratio for the theta parameter.  |
| accept_z     | Acceptance ratio for the z parameter.  |
| accept_w     | Acceptance ratio for the w parameter.  |
| accept_gamma | Acceptance ratio for the gamma parameter.  |

## References

Little, R. J., & Rubin, D. B. (2019). Statistical analysis with missing data (Vol. 793). John Wiley & Sons. Ishwaran, H., & Rao, J. S. (2005). Spike and slab variable selection: frequentist and Bayesian strategies. The Annals of Statistics, 33(2), 730-773.

## Examples

```
# generate example item response matrix
data <- matrix(rbinom(500, size = 1, prob = 0.5), ncol=10, nrow=50)

# generate example missing indicator matrix
missing_mat <- matrix(rbinom(500, size = 1, prob = 0.2), ncol=10, nrow=50)

# make missing value with missing indicator matrix
data[missing_mat==1] <- 99

lsirm_result <- lsirm1pl_mcar_ss(data)

# The code following can achieve the same result.
lsirm_result <- lsirm(data ~ lsirm1pl(spikenslab = TRUE, fixed_gamma = FALSE,
missing_data = 'mcar', missing.val = 99))
```

---

```
lsirm1pl_normal_fixed_gamma
```

*1PL LSIRM fixing gamma to 1 with normal likelihood*

---

## Description

[lsirm1pl\\_normal\\_fixed\\_gamma](#) is used to fit 1PL LSIRM for continuous variable with gamma fixed to 1. [lsirm1pl\\_normal\\_fixed\\_gamma](#) factorizes continuous item response matrix into column-wise item effect, row-wise respondent effect and further embeds interaction effect in a latent space, while ignoring the missing element under the assumption of missing at random. The resulting latent space provides an interaction map that represents interactions between respondents and items.

**Usage**

```
lsirm1pl_normal_fixed_gamma(
  data,
  ndim = 2,
  niter = 15000,
  nburn = 2500,
  nthin = 5,
  nprint = 500,
  jump_beta = 0.4,
  jump_theta = 1,
  jump_z = 0.5,
  jump_w = 0.5,
  pr_mean_beta = 0,
  pr_sd_beta = 1,
  pr_mean_theta = 0,
  pr_a_theta = 0.001,
  pr_b_theta = 0.001,
  pr_a_eps = 0.001,
  pr_b_eps = 0.001,
  verbose = FALSE
)
```

**Arguments**

|               |   |
|---------------|---|
| data          | Matrix; a binary or continuous item response matrix for analysis. Each row represents a respondent, and each column contains responses to the corresponding item. |
| ndim          | Integer; the dimension of the latent space. Default is 2.   |
| niter         | Integer; the total number of MCMC iterations to run. Default is 15000.  |
| nburn         | Integer; the number of initial MCMC iterations to discard as burn-in. Default is 2500.  |
| nthin         | Integer; the number of MCMC iterations to thin. Default is 5.   |
| nprint        | Integer; the interval at which MCMC samples are displayed during execution. Default is 500.   |
| jump_beta     | Numeric; the jumping rule for the beta proposal density. Default is 0.4.  |
| jump_theta    | Numeric; the jumping rule for the theta proposal density. Default is 1.0.   |
| jump_z        | Numeric; the jumping rule for the z proposal density. Default is 0.5.   |
| jump_w        | Numeric; the jumping rule for the w proposal density. Default is 0.5.   |
| pr_mean_beta  | Numeric; the mean of the normal prior for beta. Default is 0.   |
| pr_sd_beta    | Numeric; the standard deviation of the normal prior for beta. Default is 1.0.   |
| pr_mean_theta | Numeric; the mean of the normal prior for theta. Default is 0.  |
| pr_a_theta    | Numeric; the shape parameter of the inverse gamma prior for the variance of theta. Default is 0.001.  |

|            |  |
|------------|--|
| pr_b_theta | Numeric; the scale parameter of the inverse gamma prior for the variance of theta. Default is 0.001.   |
| pr_a_eps   | Numeric; the shape parameter of inverse gamma prior for variance of data likelihood. Default is 0.001. |
| pr_b_eps   | Numeric; the scale parameter of inverse gamma prior for variance of data likelihood. Default is 0.001. |
| verbose    | Logical; If TRUE, MCMC samples are printed for each nprint. default value is FALSE.                    |

### Details

lsirm1pl\_normal\_fixed\_gamma models the continuous value of response by respondent  $j$  to item  $i$  with item effect  $\beta_i$ , respondent effect  $\theta_j$  and the distance between latent position  $w_i$  of item  $i$  and latent position  $z_j$  of respondent  $j$  in the shared metric space:

$$Y_{j,i} = \theta_j + \beta_i - ||z_j - w_i|| + e_{j,i}$$

where the error  $e_{j,i} \sim N(0, \sigma^2)$ .

### Value

lsirm1pl\_normal\_fixed\_gamma returns an object of list containing the following components:

|                      |  |
|----------------------|--|
| data                 | A data frame or matrix containing the variables used in the model.   |
| bic                  | A numeric value representing the Bayesian Information Criterion (BIC).   |
| mcmc_inf             | Details about the number of MCMC iterations, burn-in periods, and thinning intervals.  |
| map_inf              | The log maximum a posteriori (MAP) value and the iteration number at which this MAP value occurs.  |
| beta_estimate        | Posterior estimates of the beta parameter.   |
| theta_estimate       | Posterior estimates of the theta parameter.  |
| sigma_theta_estimate | Posterior estimates of the standard deviation of theta.  |
| z_estimate           | Posterior estimates of the z parameter.  |
| w_estimate           | Posterior estimates of the w parameter.  |
| beta                 | Posterior samples of the beta parameter.   |
| theta                | Posterior samples of the theta parameter.  |
| theta_sd             | Posterior samples of the standard deviation of theta.  |
| z                    | Posterior samples of the z parameter, represented as a 3-dimensional matrix where the last axis denotes the dimension of the latent space. |
| w                    | Posterior samples of the w parameter, represented as a 3-dimensional matrix where the last axis denotes the dimension of the latent space. |
| accept_beta          | Acceptance ratio for the beta parameter.   |
| accept_theta         | Acceptance ratio for the theta parameter.  |



|                |  |
|----------------|--|
| accept_z       | Acceptance ratio for the z parameter.          |
| accept_w       | Acceptance ratio for the w parameter.          |
| sigma_estimate | Posterior estimates of the standard deviation. |
| sigma          | Posterior samples of the standard deviation.   |

### Examples

```
# generate example (continuous) item response matrix
data <- matrix(rnorm(500, mean = 0, sd = 1), ncol=10, nrow=50)

# generate example missing indicator matrix
missing_mat <- matrix(rbinom(500, size = 1, prob = 0.2), ncol=10, nrow=50)

# make missing value with missing indicator matrix
data[missing_mat==1] <- 99

lsirm_result <- lsirm1pl_normal_fixed_gamma(data)

# The code following can achieve the same result.
lsirm_result <- lsirm(data ~ lsirm1pl(spikenslab = FALSE, fixed_gamma = TRUE))
```

---

```
lsirm1pl_normal_fixed_gamma_mar
```

*1PL LSIRM fixing gamma to 1 with normal likelihood for missing at random data.*

---

### Description

[lsirm1pl\\_normal\\_fixed\\_gamma\\_mar](#) is used to fit 1PL LSIRM for continuous variable with gamma fixed to 1 in incomplete data assumed to be missing at random.

[lsirm1pl\\_normal\\_fixed\\_gamma\\_mar](#) factorizes continuous item response matrix into column-wise item effect, row-wise respondent effect and further embeds interaction effect in a latent space, while considering the missing element under the assumption of missing at random. The resulting latent space provides an interaction map that represents interactions between respondents and items.

### Usage

```
lsirm1pl_normal_fixed_gamma_mar(
  data,
  ndim = 2,
  niter = 15000,
  nburn = 2500,
  nthin = 5,
  nprint = 500,
  jump_beta = 0.4,
  jump_theta = 1,
```

```

jump_z = 0.5,
jump_w = 0.5,
pr_mean_beta = 0,
pr_sd_beta = 1,
pr_mean_theta = 0,
pr_a_theta = 0.001,
pr_b_theta = 0.001,
pr_a_eps = 0.001,
pr_b_eps = 0.001,
missing.val = 99,
verbose = FALSE
)

```

### Arguments

|                            |   |
|----------------------------|---|
| <code>data</code>          | Matrix; a binary or continuous item response matrix for analysis. Each row represents a respondent, and each column contains responses to the corresponding item. |
| <code>ndim</code>          | Integer; the dimension of the latent space. Default is 2.   |
| <code>niter</code>         | Integer; the total number of MCMC iterations to run. Default is 15000.  |
| <code>nburn</code>         | Integer; the number of initial MCMC iterations to discard as burn-in. Default is 2500.  |
| <code>nthin</code>         | Integer; the number of MCMC iterations to thin. Default is 5.   |
| <code>nprint</code>        | Integer; the interval at which MCMC samples are displayed during execution. Default is 500.   |
| <code>jump_beta</code>     | Numeric; the jumping rule for the beta proposal density. Default is 0.4.  |
| <code>jump_theta</code>    | Numeric; the jumping rule for the theta proposal density. Default is 1.0.   |
| <code>jump_z</code>        | Numeric; the jumping rule for the z proposal density. Default is 0.5.   |
| <code>jump_w</code>        | Numeric; the jumping rule for the w proposal density. Default is 0.5.   |
| <code>pr_mean_beta</code>  | Numeric; the mean of the normal prior for beta. Default is 0.   |
| <code>pr_sd_beta</code>    | Numeric; the standard deviation of the normal prior for beta. Default is 1.0.   |
| <code>pr_mean_theta</code> | Numeric; the mean of the normal prior for theta. Default is 0.  |
| <code>pr_a_theta</code>    | Numeric; the shape parameter of the inverse gamma prior for the variance of theta. Default is 0.001.  |
| <code>pr_b_theta</code>    | Numeric; the scale parameter of the inverse gamma prior for the variance of theta. Default is 0.001.  |
| <code>pr_a_eps</code>      | Numeric; the shape parameter of inverse gamma prior for variance of data likelihood. Default is 0.001.  |
| <code>pr_b_eps</code>      | Numeric; the scale parameter of inverse gamma prior for variance of data likelihood. Default is 0.001.  |
| <code>missing.val</code>   | Numeric; a number to replace missing values. Default is 99.   |
| <code>verbose</code>       | Logical; If TRUE, MCMC samples are printed for each nprint. Default is FALSE.   |

## Details

lsirm1pl\_normal\_fixed\_gamma\_mar models the continuous value of response by respondent  $j$  to item  $i$  with item effect  $\beta_i$ , respondent effect  $\theta_j$  and the distance between latent position  $w_i$  of item  $i$  and latent position  $z_j$  of respondent  $j$  in the shared metric space:

$$Y_{j,i} = \theta_j + \beta_i - ||z_j - w_i|| + e_{ji}$$

where the error  $e_{ji} \sim N(0, \sigma^2)$ . Under the assumption of missing at random, the model takes the missing element into consideration in the sampling procedure. For the details of missing at random assumption and data augmentation, see References.

## Value

lsirm1pl\_normal\_fixed\_gamma\_mar returns an object of list containing the following components:

|                      |  |
|----------------------|--|
| data                 | Data frame or matrix containing the variables in the model.  |
| missing.val          | A number to replace missing values.  |
| bic                  | Numeric value with the corresponding BIC.  |
| mcmc_inf             | Details about the number of MCMC iterations, burn-in periods, and thinning intervals.  |
| map_inf              | The log maximum a posteriori (MAP) value and the iteration number at which this MAP value occurs.  |
| beta_estimate        | Posterior estimates of the beta parameter.   |
| theta_estimate       | Posterior estimates of the theta parameter.  |
| sigma_theta_estimate | Posterior estimates of the standard deviation of theta.  |
| z_estimate           | Posterior estimates of the z parameter.  |
| w_estimate           | Posterior estimates of the w parameter.  |
| imp_estimate         | Probability of imputating a missing value with 1.  |
| beta                 | Posterior samples of the beta parameter.   |
| theta                | Posterior samples of the theta parameter.  |
| theta_sd             | Posterior samples of the standard deviation of theta.  |
| z                    | Posterior samples of the z parameter, represented as a 3-dimensional matrix where the last axis denotes the dimension of the latent space. |
| w                    | Posterior samples of the w parameter, represented as a 3-dimensional matrix where the last axis denotes the dimension of the latent space. |
| imp                  | Imputation for missing Values using posterior samples.   |
| accept_beta          | Acceptance ratio for the beta parameter.   |
| accept_theta         | Acceptance ratio for the theta parameter.  |
| accept_z             | Acceptance ratio for the z parameter.  |
| accept_w             | Acceptance ratio for the w parameter.  |
| sigma_estimate       | Posterior estimates of the standard deviation.   |
| sigma                | Posterior samples of the standard deviation.   |

## Examples

```
# generate example (continuous) item response matrix
data      <- matrix(rnorm(500, mean = 0, sd = 1), ncol=10, nrow=50)

# generate example missing indicator matrix
missing_mat <- matrix(rbinom(500, size = 1, prob = 0.2), ncol=10, nrow=50)

# make missing value with missing indicator matrix
data[missing_mat==1] <- 99

lsirm_result <- lsirm1pl_normal_fixed_gamma_mar(data)

# The code following can achieve the same result.
lsirm_result <- lsirm(data ~ lsirm1pl(spikenslab = FALSE, fixed_gamma = TRUE,
missing_data = "mar", missing.val = 99))
```

---

```
lsirm1pl_normal_fixed_gamma_mcar
```

*1PL LSIRM fixing gamma to 1 with normal likelihood for missing completely at random data.*

---

## Description

[lsirm1pl\\_normal\\_fixed\\_gamma\\_mcar](#) is used to fit 1PL LSIRM for continuous variable with gamma fixed to 1 in incomplete data assumed to be missing completely at random.

[lsirm1pl\\_normal\\_fixed\\_gamma\\_mcar](#) factorizes continuous item response matrix into column-wise item effect, row-wise respondent effect and further embeds interaction effect in a latent space, while ignoring the missing element under the assumption of missing completely at random. The resulting latent space provides an interaction map that represents interactions between respondents and items.

## Usage

```
lsirm1pl_normal_fixed_gamma_mcar(
  data,
  ndim = 2,
  niter = 15000,
  nburn = 2500,
  nthin = 5,
  nprint = 500,
  jump_beta = 0.4,
  jump_theta = 1,
  jump_z = 0.5,
  jump_w = 0.5,
  pr_mean_beta = 0,
  pr_sd_beta = 1,
  pr_mean_theta = 0,
  pr_a_theta = 0.001,
```

```

    pr_b_theta = 0.001,
    pr_a_eps = 0.001,
    pr_b_eps = 0.001,
    missing.val = 99,
    verbose = FALSE
)

```

### Arguments

|               |   |
|---------------|---|
| data          | Matrix; a binary or continuous item response matrix for analysis. Each row represents a respondent, and each column contains responses to the corresponding item. |
| ndim          | Integer; the dimension of the latent space. Default is 2.   |
| niter         | Integer; the total number of MCMC iterations to run. Default is 15000.  |
| nburn         | Integer; the number of initial MCMC iterations to discard as burn-in. Default is 2500.  |
| nthin         | Integer; the number of MCMC iterations to thin. Default is 5.   |
| nprint        | Integer; the interval at which MCMC samples are displayed during execution. Default is 500.   |
| jump_beta     | Numeric; the jumping rule for the beta proposal density. Default is 0.4.  |
| jump_theta    | Numeric; the jumping rule for the theta proposal density. Default is 1.0.   |
| jump_z        | Numeric; the jumping rule for the z proposal density. Default is 0.5.   |
| jump_w        | Numeric; the jumping rule for the w proposal density. Default is 0.5.   |
| pr_mean_beta  | Numeric; the mean of the normal prior for beta. Default is 0.   |
| pr_sd_beta    | Numeric; the standard deviation of the normal prior for beta. Default is 1.0.   |
| pr_mean_theta | Numeric; the mean of the normal prior for theta. Default is 0.  |
| pr_a_theta    | Numeric; the shape parameter of the inverse gamma prior for the variance of theta. Default is 0.001.  |
| pr_b_theta    | Numeric; the scale parameter of the inverse gamma prior for the variance of theta. Default is 0.001.  |
| pr_a_eps      | Numeric; the shape parameter of inverse gamma prior for variance of data likelihood. Default is 0.001.  |
| pr_b_eps      | Numeric; the scale parameter of inverse gamma prior for variance of data likelihood. Default is 0.001.  |
| missing.val   | Numeric; a number to replace missing values. Default is 99.   |
| verbose       | Logical; If TRUE, MCMC samples are printed for each nprint. Default is FALSE.   |

### Details

lsirm1pl\_normal\_fixed\_gamma\_mcar models the continuous value of response by respondent  $j$  to item  $i$  with item effect  $\beta_i$ , respondent effect  $\theta_j$  and the distance between latent position  $w_i$  of item  $i$  and latent position  $z_j$  of respondent  $j$  in the shared metric space:

$$Y_{j,i} = \theta_j + \beta_i - ||z_j - w_i|| + e_{j,i}$$

where the error  $e_{j,i} \sim N(0, \sigma^2)$ . Under the assumption of missing completely at random, the model ignores the missing element in doing inference. For the details of missing completely at random assumption and data augmentation, see References.

### Value

`lsirm1pl_normal_fixed_gamma_mcar` returns an object of list containing the following components:

|                                   |  |
|-----------------------------------|--|
| <code>data</code>                 | Data frame or matrix containing the variables in the model.  |
| <code>missing.val</code>          | A number to replace missing values.  |
| <code>bic</code>                  | Numeric value with the corresponding BIC.  |
| <code>mcmc_inf</code>             | Details about the number of MCMC iterations, burn-in periods, and thinning intervals.  |
| <code>map_inf</code>              | The log maximum a posteriori (MAP) value and the iteration number at which this MAP value occurs.  |
| <code>beta_estimate</code>        | Posterior estimates of the beta parameter.   |
| <code>theta_estimate</code>       | Posterior estimates of the theta parameter.  |
| <code>sigma_theta_estimate</code> | Posterior estimates of the standard deviation of theta.  |
| <code>z_estimate</code>           | Posterior estimates of the z parameter.  |
| <code>w_estimate</code>           | Posterior estimates of the w parameter.  |
| <code>beta</code>                 | Posterior samples of the beta parameter.   |
| <code>theta</code>                | Posterior samples of the theta parameter.  |
| <code>theta_sd</code>             | Posterior samples of the standard deviation of theta.  |
| <code>z</code>                    | Posterior samples of the z parameter, represented as a 3-dimensional matrix where the last axis denotes the dimension of the latent space. |
| <code>w</code>                    | Posterior samples of the w parameter, represented as a 3-dimensional matrix where the last axis denotes the dimension of the latent space. |
| <code>accept_beta</code>          | Acceptance ratio for the beta parameter.   |
| <code>accept_theta</code>         | Acceptance ratio for the theta parameter.  |
| <code>accept_z</code>             | Acceptance ratio for the z parameter.  |
| <code>accept_w</code>             | Acceptance ratio for the w parameter.  |
| <code>sigma_estimate</code>       | Posterior estimates of the standard deviation.   |
| <code>sigma</code>                | Posterior samples of the standard deviation.   |

### Examples

```
# generate example (continuous) item response matrix
data      <- matrix(rnorm(500, mean = 0, sd = 1), ncol=10, nrow=50)

# generate example missing indicator matrix
missing_mat <- matrix(rbinom(500, size = 1, prob = 0.2), ncol=10, nrow=50)
```

```
# make missing value with missing indicator matrix
data[missing_mat==1] <- 99

lsirm_result <- lsirm1pl_normal_fixed_gamma_mcar(data)

# The code following can achieve the same result.
lsirm_result <- lsirm(data ~ lsirm1pl(spikenslab = FALSE, fixed_gamma = TRUE,
missing_data = "mcar", missing.val = 99))
```

---

lsirm1pl\_normal\_mar      *1PL LSIRM with normal likelihood for missing at random data.*

---

### Description

[lsirm1pl\\_normal\\_mar](#) is used to fit LSIRM for continuous variable with 1pl in incomplete data assumed to be missing at random. [lsirm1pl\\_normal\\_mar](#) factorizes continuous item response matrix into column-wise item effect, row-wise respondent effect and further embeds interaction effect in a latent space, while considering the missing element under the assumption of missing at random. The resulting latent space provides an interaction map that represents interactions between respondents and items.

### Usage

```
lsirm1pl_normal_mar(
  data,
  ndim = 2,
  niter = 15000,
  nburn = 2500,
  nthin = 5,
  nprint = 500,
  jump_beta = 0.4,
  jump_theta = 1,
  jump_gamma = 1,
  jump_z = 0.5,
  jump_w = 0.5,
  pr_mean_beta = 0,
  pr_sd_beta = 1,
  pr_mean_theta = 0,
  pr_mean_gamma = 0.5,
  pr_sd_gamma = 1,
  pr_a_theta = 0.001,
  pr_b_theta = 0.001,
  pr_a_eps = 0.001,
  pr_b_eps = 0.001,
  missing.val = 99,
  verbose = FALSE
)
```

**Arguments**

|               |   |
|---------------|---|
| data          | Matrix; a binary or continuous item response matrix for analysis. Each row represents a respondent, and each column contains responses to the corresponding item. |
| ndim          | Integer; the dimension of the latent space. Default is 2.   |
| niter         | Integer; the total number of MCMC iterations to run. Default is 15000.  |
| nburn         | Integer; the number of initial MCMC iterations to discard as burn-in. Default is 2500.  |
| nthin         | Integer; the number of MCMC iterations to thin. Default is 5.   |
| nprint        | Integer; the interval at which MCMC samples are displayed during execution. Default is 500.   |
| jump_beta     | Numeric; the jumping rule for the beta proposal density. Default is 0.4.  |
| jump_theta    | Numeric; the jumping rule for the theta proposal density. Default is 1.0.   |
| jump_gamma    | Numeric; the jumping rule for the gamma proposal density. Default is 0.025  |
| jump_z        | Numeric; the jumping rule for the z proposal density. Default is 0.5.   |
| jump_w        | Numeric; the jumping rule for the w proposal density. Default is 0.5.   |
| pr_mean_beta  | Numeric; the mean of the normal prior for beta. Default is 0.   |
| pr_sd_beta    | Numeric; the standard deviation of the normal prior for beta. Default is 1.0.   |
| pr_mean_theta | Numeric; the mean of the normal prior for theta. Default is 0.  |
| pr_mean_gamma | Numeric; mean of log normal prior for gamma. Default is 0.5.  |
| pr_sd_gamma   | Numeric; standard deviation of log normal prior for gamma. Default is 1.0.  |
| pr_a_theta    | Numeric; the shape parameter of the inverse gamma prior for the variance of theta. Default is 0.001.  |
| pr_b_theta    | Numeric; the scale parameter of the inverse gamma prior for the variance of theta. Default is 0.001.  |
| pr_a_eps      | Numeric; the shape parameter of inverse gamma prior for variance of data likelihood. Default is 0.001.  |
| pr_b_eps      | Numeric; the scale parameter of inverse gamma prior for variance of data likelihood. Default is 0.001.  |
| missing.val   | Numeric; a number to replace missing values. Default is 99.   |
| verbose       | Logical; If TRUE, MCMC samples are printed for each nprint. Default is FALSE.   |

**Details**

lsirm1pl\_normal\_mar models the continuous value of response by respondent  $j$  to item  $i$  with item effect  $\beta_i$ , respondent effect  $\theta_j$  and the distance between latent position  $w_i$  of item  $i$  and latent position  $z_j$  of respondent  $j$  in the shared metric space, with  $\gamma$  represents the weight of the distance term:

$$Y_{j,i} = \theta_j + \beta_i - \gamma ||z_j - w_i|| + e_{ji}$$

where the error  $e_{ji} \sim N(0, \sigma^2)$  Under the assumption of missing at random, the model takes the missing element into consideration in the sampling procedure. For the details of missing at random assumption and data augmentation, see References.



**Value**

lsirm1pl\_normal\_mar returns an object of list containing the following components:

|                      |  |
|----------------------|--|
| data                 | Data frame or matrix containing the variables in the model.  |
| missing.val          | A number to replace missing values.  |
| bic                  | Numeric value with the corresponding BIC.  |
| mcmc_inf             | Details about the number of MCMC iterations, burn-in periods, and thinning intervals.  |
| map_inf              | The log maximum a posteriori (MAP) value and the iteration number at which this MAP value occurs.  |
| beta_estimate        | Posterior estimates of the beta parameter.   |
| theta_estimate       | Posterior estimates of the theta parameter.  |
| sigma_theta_estimate | Posterior estimates of the standard deviation of theta.  |
| gamma_estimate       | posterior estimates of gamma parameter.  |
| z_estimate           | Posterior estimates of the z parameter.  |
| w_estimate           | Posterior estimates of the w parameter.  |
| imp_estimate         | Probability of imputating a missing value with 1.  |
| beta                 | Posterior samples of the beta parameter.   |
| theta                | Posterior samples of the theta parameter.  |
| gamma                | Posterior samples of the gamma parameter.  |
| theta_sd             | Posterior samples of the standard deviation of theta.  |
| z                    | Posterior samples of the z parameter, represented as a 3-dimensional matrix where the last axis denotes the dimension of the latent space. |
| w                    | Posterior samples of the w parameter, represented as a 3-dimensional matrix where the last axis denotes the dimension of the latent space. |
| imp                  | Imputation for missing Values using posterior samples.   |
| accept_beta          | Acceptance ratio for the beta parameter.   |
| accept_theta         | Acceptance ratio for the theta parameter.  |
| accept_z             | Acceptance ratio for the z parameter.  |
| accept_w             | Acceptance ratio for the w parameter.  |
| accept_gamma         | Acceptance ratio for the gamma parameter.  |
| sigma_estimate       | Posterior estimates of the standard deviation.   |
| sigma                | Posterior samples of the standard deviation.   |

**References**

Little, R. J., & Rubin, D. B. (2019). Statistical analysis with missing data (Vol. 793). John Wiley & Sons.

### Examples

```
# generate example (continuous) item response matrix
data      <- matrix(rnorm(500, mean = 0, sd = 1), ncol=10, nrow=50)

# generate example missing indicator matrix
missing_mat <- matrix(rbinom(500, size = 1, prob = 0.2), ncol=10, nrow=50)

# make missing value with missing indicator matrix
data[missing_mat==1] <- 99

lsirm_result <- lsirm1pl_normal_mar(data)

# The code following can achieve the same result.
lsirm_result <- lsirm(data ~ lsirm1pl(spikenslab = FALSE, fixed_gamma = FALSE,
missing_data = 'mar', missing.val = 99))
```

---

lsirm1pl\_normal\_mar\_ss

*1PL LSIRM with normal likelihood and model selection approach for missing at random data.*

---

### Description

[lsirm1pl\\_normal\\_mar\\_ss](#) is used to fit 1PL LSIRM with model selection approach based on spike-and-slab priors for continuous variable with 1pl in incomplete data assumed to be missing at random. [lsirm1pl\\_normal\\_mar\\_ss](#) factorizes continuous item response matrix into column-wise item effect, row-wise respondent effect and further embeds interaction effect in a latent space, while considering the missing element under the assumption of missing at random. The resulting latent space provides an interaction map that represents interactions between respondents and items.

### Usage

```
lsirm1pl_normal_mar_ss(
  data,
  ndim = 2,
  niter = 15000,
  nburn = 2500,
  nthin = 5,
  nprint = 500,
  jump_beta = 0.4,
  jump_theta = 1,
  jump_gamma = 1,
  jump_z = 0.5,
  jump_w = 0.5,
  pr_mean_beta = 0,
  pr_sd_beta = 1,
  pr_mean_theta = 0,
```

```

pr_spike_mean = -3,
pr_spike_sd = 1,
pr_slab_mean = 0.5,
pr_slab_sd = 1,
pr_a_theta = 0.001,
pr_b_theta = 0.001,
pr_a_eps = 0.001,
pr_b_eps = 0.001,
pr_xi_a = 0.001,
pr_xi_b = 0.001,
missing.val = 99,
verbose = FALSE
)

```

### Arguments

|               |   |
|---------------|---|
| data          | Matrix; a binary or continuous item response matrix for analysis. Each row represents a respondent, and each column contains responses to the corresponding item. |
| ndim          | Integer; the dimension of the latent space. Default is 2.   |
| niter         | Integer; the total number of MCMC iterations to run. Default is 15000.  |
| nburn         | Integer; the number of initial MCMC iterations to discard as burn-in. Default is 2500.  |
| nthin         | Integer; the number of MCMC iterations to thin. Default is 5.   |
| nprint        | Integer; the interval at which MCMC samples are displayed during execution. Default is 500.   |
| jump_beta     | Numeric; the jumping rule for the beta proposal density. Default is 0.4.  |
| jump_theta    | Numeric; the jumping rule for the theta proposal density. Default is 1.0.   |
| jump_gamma    | Numeric; the jumping rule for the gamma proposal density. Default is 1.0.   |
| jump_z        | Numeric; the jumping rule for the z proposal density. Default is 0.5.   |
| jump_w        | Numeric; the jumping rule for the w proposal density. Default is 0.5.   |
| pr_mean_beta  | Numeric; the mean of the normal prior for beta. Default is 0.   |
| pr_sd_beta    | Numeric; the standard deviation of the normal prior for beta. Default is 1.0.   |
| pr_mean_theta | Numeric; the mean of the normal prior for theta. Default is 0.  |
| pr_spike_mean | Numeric; the mean of spike prior for log gamma. Default is -3.  |
| pr_spike_sd   | Numeric; the standard deviation of spike prior for log gamma. Default is 1.   |
| pr_slab_mean  | Numeric; the mean of spike prior for log gamma. Default is 0.5.   |
| pr_slab_sd    | Numeric; the standard deviation of spike prior for log gamma. Default is 1.   |
| pr_a_theta    | Numeric; the shape parameter of the inverse gamma prior for the variance of theta. Default is 0.001.  |
| pr_b_theta    | Numeric; the scale parameter of the inverse gamma prior for the variance of theta. Default is 0.001.  |

|             |  |
|-------------|--|
| pr_a_eps    | Numeric; the shape parameter of inverse gamma prior for variance of data likelihood. Default is 0.001. |
| pr_b_eps    | Numeric; the scale parameter of inverse gamma prior for variance of data likelihood. Default is 0.001. |
| pr_xi_a     | Numeric; the first shape parameter of beta prior for latent variable xi. Default is 1.                 |
| pr_xi_b     | Numeric; the second shape parameter of beta prior for latent variable xi. Default is 1.                |
| missing.val | Numeric; a number to replace missing values. Default is 99.  |
| verbose     | Logical; If TRUE, MCMC samples are printed for each nprint. Default is FALSE.                          |

### Details

lsirm1pl\_normal\_mar\_ss models the continuous value of response by respondent  $j$  to item  $i$  with item effect  $\beta_i$ , respondent effect  $\theta_j$  and the distance between latent position  $w_i$  of item  $i$  and latent position  $z_j$  of respondent  $j$  in the shared metric space, with  $\gamma$  represents the weight of the distance term:

$$Y_{j,i} = \theta_j + \beta_i - \gamma ||z_j - w_i|| + e_{j,i}$$

where the error  $e_{j,i} \sim N(0, \sigma^2)$ . Under the assumption of missing at random, the model takes the missing element into consideration in the sampling procedure. For the details of missing at random assumption and data augmentation, see References. lsirm1pl\_normal\_mar\_ss model include model selection approach based on spike-and-slab priors for log gamma. For detail of spike-and-slab priors, see References.

### Value

lsirm1pl\_normal\_mar\_ss returns an object of list containing the following components:

|                      |   |
|----------------------|---|
| data                 | Data frame or matrix containing the variables in the model.                                       |
| missing.val          | A number to replace missing values.   |
| bic                  | Numeric value with the corresponding BIC.   |
| mcmc_inf             | Details about the number of MCMC iterations, burn-in periods, and thinning intervals.             |
| map_inf              | The log maximum a posteriori (MAP) value and the iteration number at which this MAP value occurs. |
| beta_estimate        | Posterior estimates of the beta parameter.  |
| theta_estimate       | Posterior estimates of the theta parameter.   |
| sigma_theta_estimate | Posterior estimates of the standard deviation of theta.   |
| gamma_estimate       | posterior estimates of gamma parameter.   |
| z_estimate           | Posterior estimates of the z parameter.   |
| w_estimate           | Posterior estimates of the w parameter.   |
| beta                 | Posterior samples of the beta parameter.  |

|                |   |
|----------------|---|
| theta          | Posterior samples of the theta parameter.   |
| gamma          | Posterior samples of the gamma parameter.   |
| theta_sd       | Posterior samples of the standard deviation of theta.   |
| z              | Posterior samples of the z parameter, represented as a 3-dimensional matrix where the last axis denotes the dimension of the latent space.  |
| w              | Posterior samples of the w parameter, represented as a 3-dimensional matrix where the last axis denotes the dimension of the latent space.  |
| pi             | Posterior samples of phi which is indicator of spike and slab prior. If phi is 1, log gamma follows the slab prior, otherwise follows the spike prior.                              |
| imp            | Imputation for missing Values using posterior samples.  |
| accept_beta    | Acceptance ratio for the beta parameter.  |
| accept_theta   | Acceptance ratio for the theta parameter.   |
| accept_z       | Acceptance ratio for the z parameter.   |
| accept_w       | Acceptance ratio for the w parameter.   |
| accept_gamma   | Acceptance ratio for the gamma parameter.   |
| pi_estimate    | Posterior estimation of phi. inclusion probability of gamma. if estimation of phi is less than 0.5, choose Rasch model with gamma = 0, otherwise latent space model with gamma > 0. |
| imp_estimate   | Probability of imputating a missing value with 1.   |
| sigma_estimate | Posterior estimates of the standard deviation.  |
| sigma          | Posterior samples of the standard deviation.  |

## References

Little, R. J., & Rubin, D. B. (2019). Statistical analysis with missing data (Vol. 793). John Wiley & Sons. Ishwaran, H., & Rao, J. S. (2005). Spike and slab variable selection: frequentist and Bayesian strategies. *The Annals of Statistics*, 33(2), 730-773.

## Examples

```
# generate example (continuous) item response matrix
data <- matrix(rnorm(500, mean = 0, sd = 1),ncol=10,nrow=50)

# generate example missing indicator matrix
missing_mat <- matrix(rbinom(500, size = 1, prob = 0.2),ncol=10,nrow=50)

# make missing value with missing indicator matrix
data[missing_mat==1] <- 99

lsirm_result <- lsirm1pl_normal_mar_ss(data)

# The code following can achieve the same result.
lsirm_result <- lsirm(data ~ lsirm1pl(spikenslab = TRUE, fixed_gamma = FALSE,
missing_data = 'mar', missing = 99))
```

---

|                      |  |
|----------------------|--|
| lsirm1pl_normal_mcar | <i>1PL LSIRM with normal likelihood for missing completely at random data.</i> |
|----------------------|--|

---

### Description

[lsirm1pl\\_normal\\_mcar](#) is used to fit LSIRM with 1pl in incomplete data assumed to be missing completely at random. [lsirm1pl\\_normal\\_mcar](#) factorizes continuous item response matrix into column-wise item effect, row-wise respondent effect and further embeds interaction effect in a latent space, while ignoring the missing element under the assumption of missing completely at random. The resulting latent space provides an interaction map that represents interactions between respondents and items.

### Usage

```
lsirm1pl_normal_mcar(
  data,
  ndim = 2,
  niter = 15000,
  nburn = 2500,
  nthin = 5,
  nprint = 500,
  jump_beta = 0.4,
  jump_theta = 1,
  jump_gamma = 1,
  jump_z = 0.5,
  jump_w = 0.5,
  pr_mean_beta = 0,
  pr_sd_beta = 1,
  pr_mean_theta = 0,
  pr_mean_gamma = 0.5,
  pr_sd_gamma = 1,
  pr_a_theta = 0.001,
  pr_b_theta = 0.001,
  pr_a_eps = 0.001,
  pr_b_eps = 0.001,
  missing.val = 99,
  verbose = FALSE
)
```

### Arguments

|       |   |
|-------|---|
| data  | Matrix; a binary or continuous item response matrix for analysis. Each row represents a respondent, and each column contains responses to the corresponding item. |
| ndim  | Integer; the dimension of the latent space. Default is 2.   |
| niter | Integer; the total number of MCMC iterations to run. Default is 15000.  |

|               |  |
|---------------|--|
| nburn         | Integer; the number of initial MCMC iterations to discard as burn-in. Default is 2500.                 |
| nthin         | Integer; the number of MCMC iterations to thin. Default is 5.  |
| nprint        | Integer; the interval at which MCMC samples are displayed during execution. Default is 500.            |
| jump_beta     | Numeric; the jumping rule for the beta proposal density. Default is 0.4.                               |
| jump_theta    | Numeric; the jumping rule for the theta proposal density. Default is 1.0.                              |
| jump_gamma    | Numeric; the jumping rule for the gamma proposal density. Default is 0.025                             |
| jump_z        | Numeric; the jumping rule for the z proposal density. Default is 0.5.                                  |
| jump_w        | Numeric; the jumping rule for the w proposal density. Default is 0.5.                                  |
| pr_mean_beta  | Numeric; the mean of the normal prior for beta. Default is 0.  |
| pr_sd_beta    | Numeric; the standard deviation of the normal prior for beta. Default is 1.0.                          |
| pr_mean_theta | Numeric; the mean of the normal prior for theta. Default is 0.   |
| pr_mean_gamma | Numeric; mean of log normal prior for gamma. Default is 0.5.   |
| pr_sd_gamma   | Numeric; standard deviation of log normal prior for gamma. Default is 1.0.                             |
| pr_a_theta    | Numeric; the shape parameter of the inverse gamma prior for the variance of theta. Default is 0.001.   |
| pr_b_theta    | Numeric; the scale parameter of the inverse gamma prior for the variance of theta. Default is 0.001.   |
| pr_a_eps      | Numeric; the shape parameter of inverse gamma prior for variance of data likelihood. Default is 0.001. |
| pr_b_eps      | Numeric; the scale parameter of inverse gamma prior for variance of data likelihood. Default is 0.001. |
| missing.val   | Numeric; a number to replace missing values. Default is 99.  |
| verbose       | Logical; If TRUE, MCMC samples are printed for each nprint. Default is FALSE.                          |

## Details

lsirm1pl\_normal\_mcar models the continuous value of response by respondent  $j$  to item  $i$  with item effect  $\beta_i$ , respondent effect  $\theta_j$  and the distance between latent position  $w_i$  of item  $i$  and latent position  $z_j$  of respondent  $j$  in the shared metric space, with  $\gamma$  represents the weight of the distance term:

$$Y_{j,i} = \theta_j + \beta_i - \gamma ||z_j - w_i|| + e_{j,i}$$

where the error  $e_{j,i} \sim N(0, \sigma^2)$  Under the assumption of missing completely at random, the model ignores the missing element in doing inference. For the details of missing at random assumption and data augmentation, see References.

**Value**

`lsirm1pl_normal_mcar` returns an object of list containing the following components:

|                                   |  |
|-----------------------------------|--|
| <code>data</code>                 | A data frame or matrix containing the variables used in the model.   |
| <code>missing.val</code>          | A number to replace missing values.  |
| <code>bic</code>                  | Numeric value with the corresponding BIC.  |
| <code>mcmc_inf</code>             | Details about the number of MCMC iterations, burn-in periods, and thinning intervals.  |
| <code>map_inf</code>              | The log maximum a posteriori (MAP) value and the iteration number at which this MAP value occurs.  |
| <code>beta_estimate</code>        | Posterior estimates of the beta parameter.   |
| <code>theta_estimate</code>       | Posterior estimates of the theta parameter.  |
| <code>sigma_theta_estimate</code> | Posterior estimates of the standard deviation of theta.  |
| <code>gamma_estimate</code>       | Posterior estimates of gamma parameter.  |
| <code>z_estimate</code>           | Posterior estimates of the z parameter.  |
| <code>w_estimate</code>           | Posterior estimates of the w parameter.  |
| <code>beta</code>                 | Posterior samples of the beta parameter.   |
| <code>theta</code>                | Posterior samples of the theta parameter.  |
| <code>theta_sd</code>             | Posterior samples of the standard deviation of theta.  |
| <code>gamma</code>                | Posterior samples of the gamma parameter.  |
| <code>z</code>                    | Posterior samples of the z parameter, represented as a 3-dimensional matrix where the last axis denotes the dimension of the latent space. |
| <code>w</code>                    | Posterior samples of the w parameter, represented as a 3-dimensional matrix where the last axis denotes the dimension of the latent space. |
| <code>accept_beta</code>          | Acceptance ratio for the beta parameter.   |
| <code>accept_theta</code>         | Acceptance ratio for the theta parameter.  |
| <code>accept_z</code>             | Acceptance ratio for the z parameter.  |
| <code>accept_w</code>             | Acceptance ratio for the w parameter.  |
| <code>accept_gamma</code>         | Acceptance ratio for the gamma parameter.  |
| <code>sigma_estimate</code>       | Posterior estimates of the standard deviation.   |
| <code>sigma</code>                | Posterior samples of the standard deviation.   |

**References**

Little, R. J., & Rubin, D. B. (2019). Statistical analysis with missing data (Vol. 793). John Wiley & Sons.



## Examples

```
# generate example (continuous) item response matrix
data      <- matrix(rnorm(500, mean = 0, sd = 1),ncol=10,nrow=50)

# generate example missing indicator matrix
missing_mat  <- matrix(rbinom(500, size = 1, prob = 0.2),ncol=10,nrow=50)

# make missing value with missing indicator matrix
data[missing_mat==1] <- 99

lsirm_result <- lsirm1pl_normal_mcar(data)

# The code following can achieve the same result.
lsirm_result <- lsirm(data ~ lsirm1pl(spikenslab = FALSE, fixed_gamma = FALSE,
missing_data = 'mcar', missing.val = 99))
```

---

```
lsirm1pl_normal_mcar_ss
```

*1PL LSIRM with normal likelihood and model selection approach for missing completely at random data.*

---

## Description

[lsirm1pl\\_normal\\_mcar\\_ss](#) is used to fit LSIRM with model selection approach based on spike-and-slab priors for continuous variable with 1pl in incomplete data assumed to be missing completely at random. [lsirm1pl\\_normal\\_mcar\\_ss](#) factorizes continuous item response matrix into column-wise item effect, row-wise respondent effect and further embeds interaction effect in a latent space, while ignoring the missing element under the assumption of missing completely at random. The resulting latent space provides an interaction map that represents interactions between respondents and items.

## Usage

```
lsirm1pl_normal_mcar_ss(
  data,
  ndim = 2,
  niter = 15000,
  nburn = 2500,
  nthin = 5,
  nprint = 500,
  jump_beta = 0.4,
  jump_theta = 1,
  jump_gamma = 1,
  jump_z = 0.5,
  jump_w = 0.5,
  pr_mean_beta = 0,
  pr_sd_beta = 1,
  pr_mean_theta = 0,
```

```

pr_spike_mean = -3,
pr_spike_sd = 1,
pr_slab_mean = 0.5,
pr_slab_sd = 1,
pr_a_theta = 0.001,
pr_b_theta = 0.001,
pr_a_eps = 0.001,
pr_b_eps = 0.001,
pr_xi_a = 0.001,
pr_xi_b = 0.001,
missing.val = 99,
verbose = FALSE
)

```

### Arguments

|               |   |
|---------------|---|
| data          | Matrix; a binary or continuous item response matrix for analysis. Each row represents a respondent, and each column contains responses to the corresponding item. |
| ndim          | Integer; the dimension of the latent space. Default is 2.   |
| niter         | Integer; the total number of MCMC iterations to run. Default is 15000.  |
| nburn         | Integer; the number of initial MCMC iterations to discard as burn-in. Default is 2500.  |
| nthin         | Integer; the number of MCMC iterations to thin. Default is 5.   |
| nprint        | Integer; the interval at which MCMC samples are displayed during execution. Default is 500.   |
| jump_beta     | Numeric; the jumping rule for the beta proposal density. Default is 0.4.  |
| jump_theta    | Numeric; the jumping rule for the theta proposal density. Default is 1.0.   |
| jump_gamma    | Numeric; the jumping rule for the gamma proposal density. Default is 1.0.   |
| jump_z        | Numeric; the jumping rule for the z proposal density. Default is 0.5.   |
| jump_w        | Numeric; the jumping rule for the w proposal density. Default is 0.5.   |
| pr_mean_beta  | Numeric; the mean of the normal prior for beta. Default is 0.   |
| pr_sd_beta    | Numeric; the standard deviation of the normal prior for beta. Default is 1.0.   |
| pr_mean_theta | Numeric; the mean of the normal prior for theta. Default is 0.  |
| pr_spike_mean | Numeric; the mean of spike prior for log gamma. Default is -3.  |
| pr_spike_sd   | Numeric; the standard deviation of spike prior for log gamma. Default is 1.   |
| pr_slab_mean  | Numeric; the mean of spike prior for log gamma. Default is 0.5.   |
| pr_slab_sd    | Numeric; the standard deviation of spike prior for log gamma. Default is 1.   |
| pr_a_theta    | Numeric; the shape parameter of the inverse gamma prior for the variance of theta. Default is 0.001.  |
| pr_b_theta    | Numeric; the scale parameter of the inverse gamma prior for the variance of theta. Default is 0.001.  |

|             |  |
|-------------|--|
| pr_a_eps    | Numeric; the shape parameter of inverse gamma prior for variance of data likelihood. Default is 0.001. |
| pr_b_eps    | Numeric; the scale parameter of inverse gamma prior for variance of data likelihood. Default is 0.001. |
| pr_xi_a     | Numeric; the first shape parameter of beta prior for latent variable xi. Default is 1.                 |
| pr_xi_b     | Numeric; the second shape parameter of beta prior for latent variable xi. Default is 1.                |
| missing.val | Numeric; a number to replace missing values. Default is 99.  |
| verbose     | Logical; If TRUE, MCMC samples are printed for each nprint. Default is FALSE.                          |

### Details

lsirm1pl\_normal\_mcar\_ss models the continuous value of response by respondent  $j$  to item  $i$  with item effect  $\beta_i$ , respondent effect  $\theta_j$  and the distance between latent position  $w_i$  of item  $i$  and latent position  $z_j$  of respondent  $j$  in the shared metric space, with  $\gamma$  represents the weight of the distance term:

$$Y_{j,i} = \theta_j + \beta_i - \gamma ||z_j - w_i|| + e_{j,i}$$

where the error  $e_{j,i} \sim N(0, \sigma^2)$ . Under the assumption of missing completely at random, the model ignores the missing element in doing inference. For the details of missing at random assumption and data augmentation, see References. lsirm1pl\_normal\_mcar\_ss model include model selection approach based on spike-and-slab priors for log gamma. For detail of spike-and-slab priors, see References.

### Value

lsirm1pl\_normal\_mcar\_ss returns an object of list containing the following components:

|                      |   |
|----------------------|---|
| data                 | Data frame or matrix containing the variables in the model.                                       |
| missing.val          | A number to replace missing values.   |
| bic                  | Numeric value with the corresponding BIC.   |
| mcmc_inf             | Details about the number of MCMC iterations, burn-in periods, and thinning intervals.             |
| map_inf              | The log maximum a posteriori (MAP) value and the iteration number at which this MAP value occurs. |
| beta_estimate        | Posterior estimates of the beta parameter.  |
| theta_estimate       | Posterior estimates of the theta parameter.   |
| sigma_theta_estimate | Posterior estimates of the standard deviation of theta.   |
| gamma_estimate       | posterior estimates of gamma parameter.   |
| z_estimate           | Posterior estimates of the z parameter.   |
| w_estimate           | Posterior estimates of the w parameter.   |
| beta                 | Posterior samples of the beta parameter.  |

|                |  |
|----------------|--|
| theta          | Posterior samples of the theta parameter.  |
| gamma          | Posterior samples of the gamma parameter.  |
| theta_sd       | Posterior samples of the standard deviation of theta.  |
| z              | Posterior samples of the z parameter, represented as a 3-dimensional matrix where the last axis denotes the dimension of the latent space.             |
| w              | Posterior samples of the w parameter, represented as a 3-dimensional matrix where the last axis denotes the dimension of the latent space.             |
| pi             | Posterior samples of phi which is indicator of spike and slab prior. If phi is 1, log gamma follows the slab prior, otherwise follows the spike prior. |
| accept_beta    | Acceptance ratio for the beta parameter.   |
| accept_theta   | Acceptance ratio for the theta parameter.  |
| accept_z       | Acceptance ratio for the z parameter.  |
| accept_w       | Acceptance ratio for the w parameter.  |
| accept_gamma   | Acceptance ratio for the gamma parameter.  |
| sigma_estimate | Posterior estimates of the standard deviation.   |
| sigma          | Posterior samples of the standard deviation.   |

## References

Little, R. J., & Rubin, D. B. (2019). Statistical analysis with missing data (Vol. 793). John Wiley & Sons. Ishwaran, H., & Rao, J. S. (2005). Spike and slab variable selection: frequentist and Bayesian strategies. The Annals of Statistics, 33(2), 730-773.

## Examples

```
# generate example (continuous) item response matrix
data <- matrix(rnorm(500, mean = 0, sd = 1), ncol=10, nrow=50)

# generate example missing indicator matrix
missing_mat <- matrix(rbinom(500, size = 1, prob = 0.2), ncol=10, nrow=50)

# make missing value with missing indicator matrix
data[missing_mat==1] <- 99

lsirm_result <- lsirm1pl_normal_mcar_ss(data)

# The code following can achieve the same result.
lsirm_result <- lsirm(data ~ lsirm1pl(spikenslab = TRUE, fixed_gamma = FALSE,
missing_data = 'mcar', missing.val = 99))
```

---

|                   |  |
|-------------------|--|
| lsirm1pl_normal_o | <i>1PL LSIRM with normal likelihood.</i> |
|-------------------|--|

---

### Description

`lsirm1pl_normal_o` is used to fit LSIRM for continuous variable with 1pl. `lsirm1pl_normal_o` factorizes continuous item response matrix into column-wise item effect, row-wise respondent effect and further embeds interaction effect in a latent space. The resulting latent space provides an interaction map that represents interactions between respondents and items.

### Usage

```
lsirm1pl_normal_o(
  data,
  ndim = 2,
  niter = 15000,
  nburn = 2500,
  nthin = 5,
  nprint = 500,
  jump_beta = 0.4,
  jump_theta = 1,
  jump_gamma = 1,
  jump_z = 0.5,
  jump_w = 0.5,
  pr_mean_beta = 0,
  pr_sd_beta = 1,
  pr_mean_theta = 0,
  pr_mean_gamma = 0.5,
  pr_sd_gamma = 1,
  pr_a_theta = 0.001,
  pr_b_theta = 0.001,
  pr_a_eps = 0.001,
  pr_b_eps = 0.001,
  verbose = FALSE
)
```

### Arguments

|                    |   |
|--------------------|---|
| <code>data</code>  | Matrix; a binary or continuous item response matrix for analysis. Each row represents a respondent, and each column contains responses to the corresponding item. |
| <code>ndim</code>  | Integer; the dimension of the latent space. Default is 2.   |
| <code>niter</code> | Integer; the total number of MCMC iterations to run. Default is 15000.  |
| <code>nburn</code> | Integer; the number of initial MCMC iterations to discard as burn-in. Default is 2500.  |
| <code>nthin</code> | Integer; the number of MCMC iterations to thin. Default is 5.   |

|               |  |
|---------------|--|
| nprint        | Integer; the interval at which MCMC samples are displayed during execution. Default is 500.            |
| jump_beta     | Numeric; the jumping rule for the beta proposal density. Default is 0.4.                               |
| jump_theta    | Numeric; the jumping rule for the theta proposal density. Default is 1.0.                              |
| jump_gamma    | Numeric; the jumping rule for the gamma proposal density. Default is 0.025                             |
| jump_z        | Numeric; the jumping rule for the z proposal density. Default is 0.5.                                  |
| jump_w        | Numeric; the jumping rule for the w proposal density. Default is 0.5.                                  |
| pr_mean_beta  | Numeric; the mean of the normal prior for beta. Default is 0.  |
| pr_sd_beta    | Numeric; the standard deviation of the normal prior for beta. Default is 1.0.                          |
| pr_mean_theta | Numeric; the mean of the normal prior for theta. Default is 0.   |
| pr_mean_gamma | Numeric; mean of log normal prior for gamma. Default is 0.5.   |
| pr_sd_gamma   | Numeric; standard deviation of log normal prior for gamma. Default is 1.0.                             |
| pr_a_theta    | Numeric; the shape parameter of the inverse gamma prior for the variance of theta. Default is 0.001.   |
| pr_b_theta    | Numeric; the scale parameter of the inverse gamma prior for the variance of theta. Default is 0.001.   |
| pr_a_eps      | Numeric; the shape parameter of inverse gamma prior for variance of data likelihood. Default is 0.001. |
| pr_b_eps      | Numeric; the scale parameter of inverse gamma prior for variance of data likelihood. Default is 0.001. |
| verbose       | Logical; If TRUE, MCMC samples are printed for each nprint. Default is FALSE.                          |

### Details

lsirm1pl\_normal\_o models the continuous value of response by respondent  $j$  to item  $i$  with item effect  $\beta_i$ , respondent effect  $\theta_j$  and the distance between latent position  $w_i$  of item  $i$  and latent position  $z_j$  of respondent  $j$  in the shared metric space, with  $\gamma$  represents the weight of the distance term:

$$Y_{j,i} = \theta_j + \beta_i - \gamma ||z_j - w_i|| + e_{j,i}$$

where the error  $e_{j,i} \sim N(0, \sigma^2)$ .

### Value

lsirm1pl\_normal\_o returns an object of list containing the following components:

|               |   |
|---------------|---|
| data          | Data frame or matrix containing the variables used in the model.                                  |
| bic           | A numeric value representing the Bayesian Information Criterion (BIC).                            |
| mcmc_inf      | Details about the number of MCMC iterations, burn-in periods, and thinning intervals.             |
| map_inf       | The log maximum a posteriori (MAP) value and the iteration number at which this MAP value occurs. |
| beta_estimate | Posterior estimates of the beta parameter.  |

|                      |  |
|----------------------|--|
| theta_estimate       | Posterior estimates of the theta parameter.  |
| sigma_theta_estimate | Posterior estimates of the standard deviation of theta.  |
| gamma_estimate       | Posterior estimates of gamma parameter.  |
| z_estimate           | Posterior estimates of the z parameter.  |
| w_estimate           | Posterior estimates of the w parameter.  |
| beta                 | Posterior samples of the beta parameter.   |
| theta                | Posterior samples of the theta parameter.  |
| theta_sd             | Posterior samples of the standard deviation of theta.  |
| gamma                | Posterior samples of the gamma parameter.  |
| z                    | Posterior samples of the z parameter, represented as a 3-dimensional matrix where the last axis denotes the dimension of the latent space. |
| w                    | Posterior samples of the w parameter, represented as a 3-dimensional matrix where the last axis denotes the dimension of the latent space. |
| accept_beta          | Acceptance ratio for the beta parameter.   |
| accept_theta         | Acceptance ratio for the theta parameter.  |
| accept_z             | Acceptance ratio for the z parameter.  |
| accept_w             | Acceptance ratio for the w parameter.  |
| accept_gamma         | Acceptance ratio for the gamma parameter.  |
| sigma_estimate       | Posterior estimates of the standard deviation.   |
| sigma                | Posterior samples of the standard deviation.   |

### Examples

```
# generate example (continuous) item response matrix
data <- matrix(rnorm(500, mean = 0, sd = 1), ncol=10, nrow=50)

lsirm_result <- lsirm1pl_normal_o(data)

# The code following can achieve the same result.
lsirm_result <- lsirm(data ~ lsirm1pl(spikenslab = FALSE, fixed_gamma = FALSE))
```

---

|                    |   |
|--------------------|---|
| lsirm1pl_normal_ss | <i>1PL LSIRM with normal likelihood and model selection approach.</i> |
|--------------------|---|

---

### Description

[lsirm1pl\\_normal\\_ss](#) is used to fit LSIRM with model selection approach based on spike-and-slab priors for continuous variable with 1pl. LSIRM factorizes continuous item response matrix into column-wise item effect, row-wise respondent effect and further embeds interaction effect in a latent space. The resulting latent space provides an interaction map that represents interactions between respondents and items.

**Usage**

```
lsirm1pl_normal_ss(
  data,
  ndim = 2,
  niter = 15000,
  nburn = 2500,
  nthin = 5,
  nprint = 500,
  jump_beta = 0.4,
  jump_theta = 1,
  jump_gamma = 1,
  jump_z = 0.5,
  jump_w = 0.5,
  pr_mean_beta = 0,
  pr_sd_beta = 1,
  pr_mean_theta = 0,
  pr_spike_mean = -3,
  pr_spike_sd = 1,
  pr_slab_mean = 0.5,
  pr_slab_sd = 1,
  pr_a_theta = 0.001,
  pr_b_theta = 0.001,
  pr_a_eps = 0.001,
  pr_b_eps = 0.001,
  pr_xi_a = 0.001,
  pr_xi_b = 0.001,
  verbose = FALSE
)
```

**Arguments**

|                         |   |
|-------------------------|---|
| <code>data</code>       | Matrix; a binary or continuous item response matrix for analysis. Each row represents a respondent, and each column contains responses to the corresponding item. |
| <code>ndim</code>       | Integer; the dimension of the latent space. Default is 2.   |
| <code>niter</code>      | Integer; the total number of MCMC iterations to run. Default is 15000.  |
| <code>nburn</code>      | Integer; the number of initial MCMC iterations to discard as burn-in. Default is 2500.  |
| <code>nthin</code>      | Integer; the number of MCMC iterations to thin. Default is 5.   |
| <code>nprint</code>     | Integer; the interval at which MCMC samples are displayed during execution. Default is 500.   |
| <code>jump_beta</code>  | Numeric; the jumping rule for the beta proposal density. Default is 0.4.  |
| <code>jump_theta</code> | Numeric; the jumping rule for the theta proposal density. Default is 1.0.   |
| <code>jump_gamma</code> | Numeric; the jumping rule for the gamma proposal density. Default is 1.0.   |
| <code>jump_z</code>     | Numeric; the jumping rule for the z proposal density. Default is 0.5.   |



|               |  |
|---------------|--|
| jump_w        | Numeric; the jumping rule for the w proposal density. Default is 0.5.                                |
| pr_mean_beta  | Numeric; the mean of the normal prior for beta. Default is 0.  |
| pr_sd_beta    | Numeric; the standard deviation of the normal prior for beta. Default is 1.0.                        |
| pr_mean_theta | Numeric; the mean of the normal prior for theta. Default is 0.                                       |
| pr_spike_mean | Numeric; mean of spike prior for log gamma default value is -3.                                      |
| pr_spike_sd   | Numeric; standard deviation of spike prior for log gamma default value is 1.                         |
| pr_slab_mean  | Numeric; mean of spike prior for log gamma default value is 0.5.                                     |
| pr_slab_sd    | Numeric; standard deviation of spike prior for log gamma default value is 1.                         |
| pr_a_theta    | Numeric; the shape parameter of the inverse gamma prior for the variance of theta. Default is 0.001. |
| pr_b_theta    | Numeric; the scale parameter of the inverse gamma prior for the variance of theta. Default is 0.001. |
| pr_a_eps      | Numeric; shape parameter of inverse gamma prior for variance of data likelihood. Default is 0.001.   |
| pr_b_eps      | Numeric; scale parameter of inverse gamma prior for variance of data likelihood. Default is 0.001.   |
| pr_xi_a       | Numeric; first shape parameter of beta prior for latent variable xi. Default is 1.                   |
| pr_xi_b       | Numeric; second shape parameter of beta prior for latent variable xi. Default is 1.                  |
| verbose       | Logical; If TRUE, MCMC samples are printed for each nprint. Default is FALSE.                        |

### Details

lsirm1pl\_normal\_ss models the continuous value of response by respondent  $j$  to item  $i$  with item effect  $\beta_i$ , respondent effect  $\theta_j$  and the distance between latent position  $w_i$  of item  $i$  and latent position  $z_j$  of respondent  $j$  in the shared metric space, with  $\gamma$  represents the weight of the distance term:

$$Y_{j,i} = \theta_j + \beta_i - \gamma||z_j - w_i|| + e_{j,i}$$

where the error  $e_{j,i} \sim N(0, \sigma^2)$ . lsirm1pl\_normal\_ss model include model selection approach based on spike-and-slab priors for log gamma. For detail of spike-and-slab priors, see References.

### Value

lsirm1pl\_normal\_ss returns an object of list containing the following components:

|                |   |
|----------------|---|
| data           | Data frame or matrix containing the variables in the model.                               |
| bic            | Numeric value with the corresponding BIC.   |
| mcmc_inf       | number of mcmc iteration, burn-in periods, and thinning intervals.                        |
| map_inf        | value of log maximum a posterior and iteration number which have log maximum a posterior. |
| beta_estimate  | posterior estimation of beta.   |
| theta_estimate | posterior estimation of theta.  |

|                                   |   |
|-----------------------------------|---|
| <code>sigma_theta_estimate</code> | posterior estimation of standard deviation of theta.  |
| <code>sigma_estimate</code>       | posterior estimation of standard deviation.   |
| <code>gamma_estimate</code>       | posterior estimation of gamma.  |
| <code>z_estimate</code>           | posterior estimation of z.  |
| <code>w_estimate</code>           | posterior estimation of w.  |
| <code>pi_estimate</code>          | posterior estimation of phi. inclusion probability of gamma. if estimation of phi is less than 0.5, choose Rasch model with gamma = 0, otherwise latent space model with gamma > 0. |
| <code>beta</code>                 | posterior samples of beta.  |
| <code>theta</code>                | posterior samples of theta.   |
| <code>theta_sd</code>             | posterior samples of standard deviation of theta.   |
| <code>sigma</code>                | posterior samples of standard deviation.  |
| <code>gamma</code>                | posterior samples of gamma.   |
| <code>z</code>                    | posterior samples of z. The output is 3-dimensional matrix with last axis represent the dimension of latent space.  |
| <code>w</code>                    | posterior samples of w. The output is 3-dimensional matrix with last axis represent the dimension of latent space.  |
| <code>pi</code>                   | posterior samples of phi which is indicator of spike and slab prior. If phi is 1, log gamma follows the slab prior, otherwise follows the spike prior.                              |
| <code>accept_beta</code>          | accept ratio of beta.   |
| <code>accept_theta</code>         | accept ratio of theta.  |
| <code>accept_w</code>             | accept ratio of w.  |
| <code>accept_z</code>             | accept ratio of z.  |
| <code>accept_gamma</code>         | accept ratio of gamma.  |

## References

Ishwaran, H., & Rao, J. S. (2005). Spike and slab variable selection: Frequentist and Bayesian strategies (Vol. 33). The Annals of Statistics

## Examples

```
# generate example (continuous) item response matrix
data <- matrix(rnorm(500, mean = 0, sd = 1), ncol=10, nrow=50)

lsirm_result <- lsirm1pl_normal_ss(data)

# The code following can achieve the same result.
lsirm_result <- lsirm(data ~ lsirm1pl(spikenslab = TRUE, fixed_gamma = FALSE))
```

---

|            |                   |
|------------|-------------------|
| lsirm1pl_o | <i>1PL LSIRM.</i> |
|------------|-------------------|

---

### Description

`lsirm1pl_o` is used to fit 1PL LSIRM. `lsirm1pl_o` factorizes item response matrix into column-wise item effect, row-wise respondent effect and further embeds interaction effect in a latent space. The resulting latent space provides an interaction map that represents interactions between respondents and items.

### Usage

```
lsirm1pl_o(
  data,
  ndim = 2,
  niter = 15000,
  nburn = 2500,
  nthin = 5,
  nprint = 500,
  jump_beta = 0.4,
  jump_theta = 1,
  jump_gamma = 0.025,
  jump_z = 0.5,
  jump_w = 0.5,
  pr_mean_beta = 0,
  pr_sd_beta = 1,
  pr_mean_theta = 0,
  pr_mean_gamma = 0.5,
  pr_sd_gamma = 1,
  pr_a_theta = 0.001,
  pr_b_theta = 0.001,
  verbose = FALSE
)
```

### Arguments

|                     |   |
|---------------------|---|
| <code>data</code>   | Matrix; a binary or continuous item response matrix for analysis. Each row represents a respondent, and each column contains responses to the corresponding item. |
| <code>ndim</code>   | Integer; the dimension of the latent space. Default is 2.   |
| <code>niter</code>  | Integer; the total number of MCMC iterations to run. Default is 15000.  |
| <code>nburn</code>  | Integer; the number of initial MCMC iterations to discard as burn-in. Default is 2500.  |
| <code>nthin</code>  | Integer; the number of MCMC iterations to thin. Default is 5.   |
| <code>nprint</code> | Integer; the interval at which MCMC samples are displayed during execution. Default is 500.   |

|               |  |
|---------------|--|
| jump_beta     | Numeric; the jumping rule for the beta proposal density. Default is 0.4.                             |
| jump_theta    | Numeric; the jumping rule for the theta proposal density. Default is 1.0.                            |
| jump_gamma    | Numeric; the jumping rule for the gamma proposal density. Default is 0.025.                          |
| jump_z        | Numeric; the jumping rule for the z proposal density. Default is 0.5.                                |
| jump_w        | Numeric; the jumping rule for the w proposal density. Default is 0.5.                                |
| pr_mean_beta  | Numeric; the mean of the normal prior for beta. Default is 0.  |
| pr_sd_beta    | Numeric; the standard deviation of the normal prior for beta. Default is 1.0.                        |
| pr_mean_theta | Numeric; the mean of the normal prior for theta. Default is 0.                                       |
| pr_mean_gamma | Numeric; mean of log normal prior for gamma. Default is 0.5.   |
| pr_sd_gamma   | Numeric; standard deviation of log normal prior for gamma. Default is 1.0.                           |
| pr_a_theta    | Numeric; the shape parameter of the inverse gamma prior for the variance of theta. Default is 0.001. |
| pr_b_theta    | Numeric; the scale parameter of the inverse gamma prior for the variance of theta. Default is 0.001. |
| verbose       | Logical; If TRUE, MCMC samples are printed for each nprint. Default is FALSE.                        |

### Details

lsirm1pl\_o models the probability of correct response by respondent  $j$  to item  $i$  with item effect  $\beta_i$ , respondent effect  $\theta_j$  and the distance between latent position  $w_i$  of item  $i$  and latent position  $z_j$  of respondent  $j$  in the shared metric space, with  $\gamma$  represents the weight of the distance term:

$$\text{logit}(P(Y_{j,i} = 1 | \theta_j, \beta_i, \gamma, z_j, w_i)) = \theta_j + \beta_i - \gamma ||z_j - w_i||$$

### Value

lsirm1pl\_o returns an object of list containing the following components:

|                      |   |
|----------------------|---|
| data                 | Data frame or matrix containing the variables used in the model.                                  |
| bic                  | A numeric value representing the Bayesian Information Criterion (BIC).                            |
| mcmc_inf             | Details about the number of MCMC iterations, burn-in periods, and thinning intervals.             |
| map_inf              | The log maximum a posteriori (MAP) value and the iteration number at which this MAP value occurs. |
| beta_estimate        | Posterior estimates of the beta parameter.  |
| theta_estimate       | Posterior estimates of the theta parameter.   |
| sigma_theta_estimate | Posterior estimates of the standard deviation of theta.   |
| gamma_estimate       | Posterior estimates of gamma parameter.   |
| z_estimate           | Posterior estimates of the z parameter.   |
| w_estimate           | Posterior estimates of the w parameter.   |
| beta                 | Posterior samples of the beta parameter.  |

|              |  |
|--------------|--|
| theta        | Posterior samples of the theta parameter.  |
| theta_sd     | Posterior samples of the standard deviation of theta.  |
| gamma        | Posterior samples of the gamma parameter.  |
| z            | Posterior samples of the z parameter, represented as a 3-dimensional matrix where the last axis denotes the dimension of the latent space. |
| w            | Posterior samples of the w parameter, represented as a 3-dimensional matrix where the last axis denotes the dimension of the latent space. |
| accept_beta  | Acceptance ratio for the beta parameter.   |
| accept_theta | Acceptance ratio for the theta parameter.  |
| accept_z     | Acceptance ratio for the z parameter.  |
| accept_w     | Acceptance ratio for the w parameter.  |
| accept_gamma | Acceptance ratio for the gamma parameter.  |

### Examples

```
# generate example item response matrix
data <- matrix(rbinom(500, size = 1, prob = 0.5), ncol=10, nrow=50)

lsirm_result <- lsirm1pl_o(data)

# The code following can achieve the same result.
lsirm_result <- lsirm(data ~ lsirm1pl(spikenslab = FALSE, fixed_gamma = FALSE))
```

---

|             |   |
|-------------|---|
| lsirm1pl_ss | <i>1PL LSIRM with model selection approach.</i> |
|-------------|---|

---

### Description

[lsirm1pl\\_ss](#) is used to fit 1PL LSIRM with model selection approach based on spike-and-slab priors. LSIRM factorizes item response matrix into column-wise item effect, row-wise respondent effect and further embeds interaction effect in a latent space. The resulting latent space provides an interaction map that represents interactions between respondents and items.

### Usage

```
lsirm1pl_ss(
  data,
  ndim = 2,
  niter = 15000,
  nburn = 2500,
  nthin = 5,
  nprint = 500,
  jump_beta = 0.4,
  jump_theta = 1,
```

```

    jump_gamma = 1,
    jump_z = 0.5,
    jump_w = 0.5,
    pr_mean_beta = 0,
    pr_sd_beta = 1,
    pr_mean_theta = 0,
    pr_spike_mean = -3,
    pr_spike_sd = 1,
    pr_slab_mean = 0.5,
    pr_slab_sd = 1,
    pr_a_theta = 0.001,
    pr_b_theta = 0.001,
    pr_xi_a = 1,
    pr_xi_b = 1,
    verbose = FALSE
)

```

### Arguments

|               |   |
|---------------|---|
| data          | Matrix; a binary or continuous item response matrix for analysis. Each row represents a respondent, and each column contains responses to the corresponding item. |
| ndim          | Integer; the dimension of the latent space. Default is 2.   |
| niter         | Integer; the total number of MCMC iterations to run. Default is 15000.  |
| nburn         | Integer; the number of initial MCMC iterations to discard as burn-in. Default is 2500.  |
| nthin         | Integer; the number of MCMC iterations to thin. Default is 5.   |
| nprint        | Integer; the interval at which MCMC samples are displayed during execution. Default is 500.   |
| jump_beta     | Numeric; the jumping rule for the beta proposal density. Default is 0.4.  |
| jump_theta    | Numeric; the jumping rule for the theta proposal density. Default is 1.0.   |
| jump_gamma    | Numeric; the jumping rule for the gamma proposal density. Default is 1.0.   |
| jump_z        | Numeric; the jumping rule for the z proposal density. Default is 0.5.   |
| jump_w        | Numeric; the jumping rule for the w proposal density. Default is 0.5.   |
| pr_mean_beta  | Numeric; the mean of the normal prior for beta. Default is 0.   |
| pr_sd_beta    | Numeric; the standard deviation of the normal prior for beta. Default is 1.0.   |
| pr_mean_theta | Numeric; the mean of the normal prior for theta. Default is 0.  |
| pr_spike_mean | Numeric; the mean of spike prior for log gamma. Default is -3.  |
| pr_spike_sd   | Numeric; the standard deviation of spike prior for log gamma. Default is 1.   |
| pr_slab_mean  | Numeric; the mean of spike prior for log gamma. Default is 0.5.   |
| pr_slab_sd    | Numeric; the standard deviation of spike prior for log gamma. Default is 1.   |
| pr_a_theta    | Numeric; the shape parameter of the inverse gamma prior for the variance of theta. Default is 0.001.  |

|            |  |
|------------|--|
| pr_b_theta | Numeric; the scale parameter of the inverse gamma prior for the variance of theta. Default is 0.001. |
| pr_xi_a    | Numeric; the first shape parameter of beta prior for latent variable xi. Default is 1.               |
| pr_xi_b    | Numeric; the second shape parameter of beta prior for latent variable xi. Default is 1.              |
| verbose    | Logical; If TRUE, MCMC samples are printed for each nprint. Default is FALSE.                        |

### Details

lsirm1pl\_ss models the probability of correct response by respondent  $j$  to item  $i$  with item effect  $\beta_i$ , respondent effect  $\theta_j$  and the distance between latent position  $w_i$  of item  $i$  and latent position  $z_j$  of respondent  $j$  in the shared metric space, with  $\gamma$  represents the weight of the distance term:

$$\text{logit}(P(Y_{j,i} = 1 | \theta_j, \beta_i, \gamma, z_j, w_i)) = \theta_j + \beta_i - \gamma ||z_j - w_i||$$

lsirm1pl\_ss model include model selection approach based on spike-and-slab priors for log gamma. For detail of spike-and-slab priors, see References.

### Value

lsirm1pl\_ss returns an object of list containing the following components:

|                      |  |
|----------------------|--|
| data                 | Data frame or matrix containing the variables used in the model.   |
| bic                  | A numeric value representing the Bayesian Information Criterion (BIC).   |
| mcmc_inf             | Details about the number of MCMC iterations, burn-in periods, and thinning intervals.  |
| map_inf              | The log maximum a posteriori (MAP) value and the iteration number at which this MAP value occurs.  |
| beta_estimate        | Posterior estimates of the beta parameter.   |
| theta_estimate       | Posterior estimates of the theta parameter.  |
| sigma_theta_estimate | Posterior estimates of the standard deviation of theta.  |
| gamma_estimate       | Posterior estimates of gamma parameter.  |
| z_estimate           | Posterior estimates of the z parameter.  |
| w_estimate           | Posterior estimates of the w parameter.  |
| beta                 | Posterior samples of the beta parameter.   |
| theta                | Posterior samples of the theta parameter.  |
| theta_sd             | Posterior samples of the standard deviation of theta.  |
| gamma                | Posterior samples of the gamma parameter.  |
| z                    | Posterior samples of the z parameter, represented as a 3-dimensional matrix where the last axis denotes the dimension of the latent space. |
| w                    | Posterior samples of the w parameter, represented as a 3-dimensional matrix where the last axis denotes the dimension of the latent space. |

|              |   |
|--------------|---|
| accept_beta  | Acceptance ratio for the beta parameter.  |
| accept_theta | Acceptance ratio for the theta parameter.   |
| accept_z     | Acceptance ratio for the z parameter.   |
| accept_w     | Acceptance ratio for the w parameter.   |
| accept_gamma | Acceptance ratio for the gamma parameter.   |
| pi_estimate  | Posterior estimation of phi. inclusion probability of gamma. if estimation of phi is less than 0.5, choose Rasch model with gamma = 0, otherwise latent space model with gamma > 0. |
| pi           | Posterior samples of phi which is indicator of spike and slab prior. If phi is 1, log gamma follows the slab prior, otherwise follows the spike prior.                              |

## References

Ishwaran, H., & Rao, J. S. (2005). Spike and slab variable selection: Frequentist and Bayesian strategies (Vol. 33). The Annals of Statistics

## Examples

```
# generate example item response matrix
data <- matrix(rbinom(500, size = 1, prob = 0.5), ncol=10, nrow=50)

lsirm_result <- lsirm1pl_ss(data)

# The code following can achieve the same result.
lsirm_result <- lsirm(data ~ lsirm1pl(spikenslab = TRUE, fixed_gamma = FALSE))
```

---

lsirm2pl

---

*Fit a 2pl LSIRM for binary and continuous item response data*


---

## Description

[lsirm2pl](#) integrates all functions related to 2PL LSIRM. Various 2PL LSIRM function can be used by setting the `spikenslab`, `fixed_gamma`, and `missing_data` arguments.

This function can be used regardless of the data type, providing a unified approach to model fitting.

## Usage

```
lsirm2pl(
  data,
  spikenslab = FALSE,
  fixed_gamma = FALSE,
  missing_data = NA,
  chains = 1,
  multicore = 1,
  seed = NA,
```



```

    ndim = 2,
    niter = 15000,
    nburn = 2500,
    nthin = 5,
    nprint = 500,
    jump_beta = 0.4,
    jump_theta = 1,
    jump_alpha = 1,
    jump_z = 0.5,
    jump_w = 0.5,
    pr_mean_beta = 0,
    pr_sd_beta = 1,
    pr_mean_theta = 0,
    pr_a_theta = 0.001,
    pr_b_theta = 0.001,
    pr_mean_alpha = 0.5,
    pr_sd_alpha = 1,
    ...
)

```

### Arguments

|              |   |
|--------------|---|
| data         | Matrix; a binary or continuous item response matrix for analysis. Each row represents a respondent, and each column contains responses to the corresponding item. |
| spikenslab   | Logical; specifies whether to use a model selection approach. Default is FALSE.   |
| fixed_gamma  | Logical; indicates whether to fix gamma at 1. Default is FALSE.   |
| missing_data | Character; the type of missing data assumed. Options are NA, "mar", or "mcar". Default is NA.   |
| chains       | Integer; the number of MCMC chains to run. Default is 1.  |
| multicore    | Integer; the number of cores to use for parallel execution. Default is 1.   |
| seed         | Integer; the seed number for MCMC fitting. Default is NA.   |
| ndim         | Integer; the dimension of the latent space. Default is 2.   |
| niter        | Integer; the total number of MCMC iterations to run. Default is 15000.  |
| nburn        | Integer; the number of initial MCMC iterations to discard as burn-in. Default is 2500.  |
| nthin        | Integer; the number of MCMC iterations to thin. Default is 5.   |
| nprint       | Integer; the interval at which MCMC samples are displayed during execution. Default is 500.   |
| jump_beta    | Numeric; the jumping rule for the beta proposal density. Default is 0.4.  |
| jump_theta   | Numeric; the jumping rule for the theta proposal density. Default is 1.0.   |
| jump_alpha   | Numeric; the jumping rule for the alpha proposal density. Default is 1.0.   |
| jump_z       | Numeric; the jumping rule for the z proposal density. Default is 0.5.   |
| jump_w       | Numeric; the jumping rule for the w proposal density. Default is 0.5.   |

|               |  |
|---------------|--|
| pr_mean_beta  | Numeric; the mean of the normal prior for beta. Default is 0.  |
| pr_sd_beta    | Numeric; the standard deviation of the normal prior for beta. Default is 1.0.                        |
| pr_mean_theta | Numeric; the mean of the normal prior for theta. Default is 0.                                       |
| pr_a_theta    | Numeric; the shape parameter of the inverse gamma prior for the variance of theta. Default is 0.001. |
| pr_b_theta    | Numeric; the scale parameter of the inverse gamma prior for the variance of theta. Default is 0.001. |
| pr_mean_alpha | Numeric; the mean of the log normal prior for alpha. Default is 0.5.                                 |
| pr_sd_alpha   | Numeric; the standard deviation of the log normal prior for alpha. Default is 1.0.                   |
| ...           | Additional arguments for the for various settings. Refer to the functions in the Details.            |

## Details

Additional arguments and return values for each function are documented in the respective function's description.

\* For 2PL LSIRM with data included missing value are detailed in [lsirm2pl\\_mar](#) and [lsirm2pl\\_mcar](#).

\* For 2PL LSIRM using the spike-and-slab model selection approach are detailed in [lsirm2pl\\_ss](#).

\* For continuous version of 2PL LSIRM are detailed in [lsirm2pl\\_normal\\_o](#).

For 2PL LSIRM with binary item response data, the probability of correct response by respondent  $j$  to item  $i$  with item effect  $\beta_i$ , respondent effect  $\theta_j$  and the distance between latent position  $w_i$  of item  $i$  and latent position  $z_j$  of respondent  $j$  in the shared metric space, with  $\gamma$  represents the weight of the distance term. For 2pl model, the the item effect is assumed to have additional discrimination parameter  $\alpha_i$  multiplied by  $\theta_j$ :

$$\text{logit}(P(Y_{j,i} = 1 | \theta_j, \alpha_i, \beta_i, \gamma, z_j, w_i)) = \theta_j * \alpha_i + \beta_i - \gamma ||z_j - w_i||$$

For 2PL LSIRM with continuous item response data, the continuous value of response by respondent  $j$  to item  $i$  with item effect  $\beta_i$ , respondent effect  $\theta_j$  and the distance between latent position  $w_i$  of item  $i$  and latent position  $z_j$  of respondent  $j$  in the shared metric space, with  $\gamma$  represents the weight of the distance term. For 2pl model, the the item effect is assumed to have additional discrimination parameter  $\alpha_i$  multiplied by  $\theta_j$ :

$$Y_{j,i} = \theta_j + \beta_i - \gamma ||z_j - w_i|| + e_{j,i}$$

where the error  $e_{j,i} \sim N(0, \sigma^2)$

## Value

lsirm2pl returns an object of list. The basic return list containing the following components:

|          |   |
|----------|---|
| data     | A data frame or matrix containing the variables used in the model.                    |
| bic      | A numeric value representing the Bayesian Information Criterion (BIC).                |
| mcmc_inf | Details about the number of MCMC iterations, burn-in periods, and thinning intervals. |

|                      |  |
|----------------------|--|
| map_inf              | The log maximum a posteriori (MAP) value and the iteration number at which this MAP value occurs.  |
| beta_estimate        | Posterior estimates of the beta parameter.   |
| theta_estimate       | Posterior estimates of the theta parameter.  |
| sigma_theta_estimate | Posterior estimates of the standard deviation of theta.  |
| alpha_estimate       | posterior estimates of alpha parameter..   |
| z_estimate           | Posterior estimates of the z parameter.  |
| w_estimate           | Posterior estimates of the w parameter.  |
| beta                 | Posterior samples of the beta parameter.   |
| theta                | Posterior samples of the theta parameter.  |
| theta_sd             | Posterior samples of the standard deviation of theta.  |
| alpha                | Posterior samples of the alpha parameter.  |
| z                    | Posterior samples of the z parameter, represented as a 3-dimensional matrix where the last axis denotes the dimension of the latent space. |
| w                    | Posterior samples of the w parameter, represented as a 3-dimensional matrix where the last axis denotes the dimension of the latent space. |
| accept_beta          | Acceptance ratio for the beta parameter.   |
| accept_theta         | Acceptance ratio for the theta parameter.  |
| accept_z             | Acceptance ratio for the z parameter.  |
| accept_w             | Acceptance ratio for the w parameter.  |
| accept_alpha         | Acceptance ratio for the alpha parameter.  |
| ...                  | Additional return values for various settings. Refer to the functions in the Details.  |

### Note

If both `spikenslab` and `fixed_gamma` are set TRUE, it returns error because both are related to `gamma`.

### See Also

The 2PL LSIRM for binary item response data as following:

`lsirm2pl_o`, `lsirm2pl_fixed_gamma`, `lsirm2pl_mar`, `lsirm2pl_mcar`, `lsirm2pl_fixed_gamma_mar`, `lsirm2pl_fixed_gamma_mcar`, `lsirm2pl_ss`, `lsirm2pl_mar_ss`, and `lsirm2pl_mcar_ss`

The 2PL LSIRM for continuous item response data as following:

`lsirm2pl_normal_o`, `lsirm2pl_normal_fixed_gamma`, `lsirm2pl_normal_mar`, `lsirm2pl_normal_mcar`, `lsirm1pl_normal`, `lsirm2pl_normal_fixed_gamma_mcar`, `lsirm2pl_normal_ss`, `lsirm2pl_normal_mar_ss`, `lsirm2pl_normal_mcar_ss`

## Examples

```
# generate example item response matrix
data <- matrix(rbinom(500, size = 1, prob = 0.5), ncol=10, nrow=50)
lsirm_result <- lsirm2pl(data)

# The code following can achieve the same result.
lsirm_result <- lsirm(data~lsirm2pl())
```

---

lsirm2pl\_fixed\_gamma    *2PL LSIRM fixing gamma to 1.*

---

## Description

[lsirm2pl\\_fixed\\_gamma](#) is used to fit 2PL LSIRM fixing gamma to 1. [lsirm2pl\\_fixed\\_gamma](#) factorizes item response matrix into column-wise item effect, row-wise respondent effect and further embeds interaction effect in a latent space. Unlike 1PL model, 2PL model assumes the item effect can vary according to respondent, allowing additional parameter multiplied with respondent effect. The resulting latent space provides an interaction map that represents interactions between respondents and items.

## Usage

```
lsirm2pl_fixed_gamma(
  data,
  ndim = 2,
  niter = 15000,
  nburn = 2500,
  nthin = 5,
  nprint = 500,
  jump_beta = 0.4,
  jump_theta = 1,
  jump_alpha = 1,
  jump_z = 0.5,
  jump_w = 0.5,
  pr_mean_beta = 0,
  pr_sd_beta = 1,
  pr_mean_theta = 0,
  pr_mean_alpha = 0.5,
  pr_sd_alpha = 1,
  pr_a_theta = 0.001,
  pr_b_theta = 0.001,
  verbose = FALSE
)
```

**Arguments**

|               |   |
|---------------|---|
| data          | Matrix; a binary or continuous item response matrix for analysis. Each row represents a respondent, and each column contains responses to the corresponding item. |
| ndim          | Integer; the dimension of the latent space. Default is 2.   |
| niter         | Integer; the total number of MCMC iterations to run. Default is 15000.  |
| nburn         | Integer; the number of initial MCMC iterations to discard as burn-in. Default is 2500.  |
| nthin         | Integer; the number of MCMC iterations to thin. Default is 5.   |
| nprint        | Integer; the interval at which MCMC samples are displayed during execution. Default is 500.   |
| jump_beta     | Numeric; the jumping rule for the beta proposal density. Default is 0.4.  |
| jump_theta    | Numeric; the jumping rule for the theta proposal density. Default is 1.0.   |
| jump_alpha    | Numeric; the jumping rule for the alpha proposal density. Default is 1.0.   |
| jump_z        | Numeric; the jumping rule for the z proposal density. Default is 0.5.   |
| jump_w        | Numeric; the jumping rule for the w proposal density. Default is 0.5.   |
| pr_mean_beta  | Numeric; the mean of the normal prior for beta. Default is 0.   |
| pr_sd_beta    | Numeric; the standard deviation of the normal prior for beta. Default is 1.0.   |
| pr_mean_theta | Numeric; the mean of the normal prior for theta. Default is 0.  |
| pr_mean_alpha | Numeric; the mean of the log normal prior for alpha. Default is 0.5.  |
| pr_sd_alpha   | Numeric; the standard deviation of the log normal prior for alpha. Default is 1.0.  |
| pr_a_theta    | Numeric; the shape parameter of the inverse gamma prior for the variance of theta. Default is 0.001.  |
| pr_b_theta    | Numeric; the scale parameter of the inverse gamma prior for the variance of theta. Default is 0.001.  |
| verbose       | Logical; If TRUE, MCMC samples are printed for each nprint. Default is FALSE.   |

**Details**

lsirm2pl\_fixed\_gamma models the probability of correct response by respondent  $j$  to item  $i$  with item effect  $\beta_i$ , respondent effect  $\theta_j$  and the distance between latent position  $w_i$  of item  $i$  and latent position  $z_j$  of respondent  $j$  in the shared metric space. For 2pl model, the item effect is assumed to have additional discrimination parameter  $\alpha_i$  multiplied by  $\theta_j$ :

$$\text{logit}(P(Y_{j,i} = 1 | \theta_j, \alpha_i, \beta_i, z_j, w_i)) = \theta_j * \alpha_i + \beta_i - ||z_j - w_i||$$

**Value**

lsirm2pl\_fixed\_gamma returns an object of list containing the following components:

lsirm1pl\_fixed\_gamma returns an object of list containing the following components:

|                                   |  |
|-----------------------------------|--|
| <code>data</code>                 | Data frame or matrix containing the variables in the model.  |
| <code>bic</code>                  | Numeric value with the corresponding BIC.  |
| <code>mcmc_inf</code>             | Details about the number of MCMC iterations, burn-in periods, and thinning intervals.  |
| <code>map_inf</code>              | The log maximum a posteriori (MAP) value and the iteration number at which this MAP value occurs.  |
| <code>beta_estimate</code>        | Posterior estimates of the beta parameter.   |
| <code>theta_estimate</code>       | Posterior estimates of the theta parameter.  |
| <code>sigma_theta_estimate</code> | Posterior estimates of the standard deviation of theta.  |
| <code>z_estimate</code>           | Posterior estimates of the z parameter.  |
| <code>w_estimate</code>           | Posterior estimates of the w parameter.  |
| <code>beta</code>                 | Posterior samples of the beta parameter.   |
| <code>theta</code>                | Posterior samples of the theta parameter.  |
| <code>theta_sd</code>             | Posterior samples of the standard deviation of theta.  |
| <code>z</code>                    | Posterior samples of the z parameter, represented as a 3-dimensional matrix where the last axis denotes the dimension of the latent space. |
| <code>w</code>                    | Posterior samples of the w parameter, represented as a 3-dimensional matrix where the last axis denotes the dimension of the latent space. |
| <code>accept_beta</code>          | Acceptance ratio for the beta parameter.   |
| <code>accept_theta</code>         | Acceptance ratio for the theta parameter.  |
| <code>accept_z</code>             | Acceptance ratio for the z parameter.  |
| <code>accept_w</code>             | Acceptance ratio for the w parameter.  |
| <code>alpha_estimate</code>       | Posterior estimates of the alpha parameter.  |
| <code>alpha</code>                | Posterior estimates of the alpha parameter.  |
| <code>accept_alpha</code>         | Acceptance ratio for the alpha parameter.  |

## Examples

```
# generate example item response matrix
data <- matrix(rbinom(500, size = 1, prob = 0.5), ncol=10, nrow=50)

lsirm_result <- lsirm2pl_fixed_gamma(data)

# The code following can achieve the same result.
lsirm_result <- lsirm(data ~ lsirm2pl(spikenslab = FALSE, fixed_gamma = TRUE))
```

---

lsirm2pl\_fixed\_gamma\_mar

2PL LSIRM fixing gamma to 1 for missing at random data.

---

## Description

[lsirm2pl\\_fixed\\_gamma\\_mar](#) is used to fit 2PL LSIRM fixing gamma to 1 in incomplete data assumed to be missing at random. [lsirm2pl\\_fixed\\_gamma\\_mar](#) factorizes item response matrix into column-wise item effect, row-wise respondent effect and further embeds interaction effect in a latent space, while considering the missing element under the assumption of missing at random. Unlike 1pl model, 2pl model assumes the item effect can vary according to respondent, allowing additional parameter multiplied with respondent effect. The resulting latent space provides an interaction map that represents interactions between respondents and items.

## Usage

```
lsirm2pl_fixed_gamma_mar(
  data,
  ndim = 2,
  niter = 15000,
  nburn = 2500,
  nthin = 5,
  nprint = 500,
  jump_beta = 0.4,
  jump_theta = 1,
  jump_alpha = 1,
  jump_z = 0.5,
  jump_w = 0.5,
  pr_mean_beta = 0,
  pr_sd_beta = 1,
  pr_mean_theta = 0,
  pr_mean_alpha = 0.5,
  pr_sd_alpha = 1,
  pr_a_theta = 0.001,
  pr_b_theta = 0.001,
  missing.val = 99,
  verbose = FALSE
)
```

## Arguments

|       |   |
|-------|---|
| data  | Matrix; a binary or continuous item response matrix for analysis. Each row represents a respondent, and each column contains responses to the corresponding item. |
| ndim  | Integer; the dimension of the latent space. Default is 2.   |
| niter | Integer; the total number of MCMC iterations to run. Default is 15000.  |

|               |  |
|---------------|--|
| nburn         | Integer; the number of initial MCMC iterations to discard as burn-in. Default is 2500.               |
| nthin         | Integer; the number of MCMC iterations to thin. Default is 5.  |
| nprint        | Integer; the interval at which MCMC samples are displayed during execution. Default is 500.          |
| jump_beta     | Numeric; the jumping rule for the beta proposal density. Default is 0.4.                             |
| jump_theta    | Numeric; the jumping rule for the theta proposal density. Default is 1.0.                            |
| jump_alpha    | Numeric; the jumping rule for the alpha proposal density. Default is 1.0.                            |
| jump_z        | Numeric; the jumping rule for the z proposal density. Default is 0.5.                                |
| jump_w        | Numeric; the jumping rule for the w proposal density. Default is 0.5.                                |
| pr_mean_beta  | Numeric; the mean of the normal prior for beta. Default is 0.  |
| pr_sd_beta    | Numeric; the standard deviation of the normal prior for beta. Default is 1.0.                        |
| pr_mean_theta | Numeric; the mean of the normal prior for theta. Default is 0.                                       |
| pr_mean_alpha | Numeric; the mean of the log normal prior for alpha. Default is 0.5.                                 |
| pr_sd_alpha   | Numeric; the standard deviation of the log normal prior for alpha. Default is 1.0.                   |
| pr_a_theta    | Numeric; the shape parameter of the inverse gamma prior for the variance of theta. Default is 0.001. |
| pr_b_theta    | Numeric; the scale parameter of the inverse gamma prior for the variance of theta. Default is 0.001. |
| missing.val   | Numeric; A number to replace missing values. Default is 99.  |
| verbose       | Logical; If TRUE, MCMC samples are printed for each nprint. Default is FALSE.                        |

## Details

lsirm2pl\_fixed\_gamma\_mar models the probability of correct response by respondent  $j$  to item  $i$  with item effect  $\beta_i$ , respondent effect  $\theta_j$  and the distance between latent position  $w_i$  of item  $i$  and latent position  $z_j$  of respondent  $j$  in the shared metric space. For 2pl model, the item effect is assumed to have additional discrimination parameter  $\alpha_i$  multiplied by  $\theta_j$ :

$$\text{logit}(P(Y_{j,i} = 1 | \theta_j, \alpha_i, \beta_i, z_j, w_i)) = \theta_j * \alpha_i + \beta_i - ||z_j - w_i||$$

Under the assumption of missing at random, the model takes the missing element into consideration in the sampling procedure. For the details of missing at random assumption and data augmentation, see References.

## Value

lsirm2pl\_fixed\_gamma\_mar returns an object of list containing the following components:

|             |   |
|-------------|---|
| data        | Data frame or matrix containing the variables in the model. |
| missing.val | A number to replace missing values.                         |
| bic         | Numeric value with the corresponding BIC.                   |



|                      |  |
|----------------------|--|
| mcmc_inf             | Details about the number of MCMC iterations, burn-in periods, and thinning intervals.  |
| map_inf              | The log maximum a posteriori (MAP) value and the iteration number at which this MAP value occurs.  |
| beta_estimate        | Posterior estimates of the beta parameter.   |
| theta_estimate       | Posterior estimates of the theta parameter.  |
| sigma_theta_estimate | Posterior estimates of the standard deviation of theta.  |
| z_estimate           | Posterior estimates of the z parameter.  |
| w_estimate           | Posterior estimates of the w parameter.  |
| imp_estimate         | Probability of imputating a missing value with 1.  |
| beta                 | Posterior samples of the beta parameter.   |
| theta                | Posterior samples of the theta parameter.  |
| theta_sd             | Posterior samples of the standard deviation of theta.  |
| z                    | Posterior samples of the z parameter, represented as a 3-dimensional matrix where the last axis denotes the dimension of the latent space. |
| w                    | Posterior samples of the w parameter, represented as a 3-dimensional matrix where the last axis denotes the dimension of the latent space. |
| imp                  | Imputation for missing Values using posterior samples.   |
| accept_beta          | Acceptance ratio for the beta parameter.   |
| accept_theta         | Acceptance ratio for the theta parameter.  |
| accept_z             | Acceptance ratio for the z parameter.  |
| accept_w             | Acceptance ratio for the w parameter.  |
| alpha_estimate       | Posterior estimates of the alpha parameter.  |
| alpha                | Posterior estimates of the alpha parameter.  |
| accept_alpha         | Acceptance ratio for the alpha parameter.  |

## References

Little, R. J., & Rubin, D. B. (2019). Statistical analysis with missing data (Vol. 793). John Wiley & Sons.

## Examples

```
# generate example item response matrix
data <- matrix(rbinom(500, size = 1, prob = 0.5),ncol=10,nrow=50)

# generate example missing indicator matrix
missing_mat <- matrix(rbinom(500, size = 1, prob = 0.2),ncol=10,nrow=50)

# make missing value with missing indicator matrix
data[missing_mat==1] <- 99

lsirm_result <- lsirm2pl_fixed_gamma_mar(data)
```

```
# The code following can achieve the same result.
lsirm_result <- lsirm(data ~ lsirm2pl(spikenslab = FALSE, fixed_gamma = TRUE,
                                     missing_data = "mar"))
```

---

```
lsirm2pl_fixed_gamma_mcar
```

*2PL LSIRM fixing gamma to 1 for missing completely at random data.*

---

## Description

[lsirm2pl\\_fixed\\_gamma\\_mcar](#) is used to fit 2PL LSIRM fixing gamma to 1 in incomplete data assumed to be missing completely at random. [lsirm2pl\\_fixed\\_gamma\\_mcar](#) factorizes item response matrix into column-wise item effect, row-wise respondent effect and further embeds interaction effect in a latent space, while ignoring the missing element under the assumption of missing completely at random. Unlike 1pl model, 2pl model assumes the item effect can vary according to respondent, allowing additional parameter multiplied with respondent effect. The resulting latent space provides an interaction map that represents interactions between respondents and items.

## Usage

```
lsirm2pl_fixed_gamma_mcar(
  data,
  ndim = 2,
  niter = 15000,
  nburn = 2500,
  nthin = 5,
  nprint = 500,
  jump_beta = 0.4,
  jump_theta = 1,
  jump_alpha = 1,
  jump_z = 0.5,
  jump_w = 0.5,
  pr_mean_beta = 0,
  pr_sd_beta = 1,
  pr_mean_theta = 0,
  pr_mean_alpha = 0.5,
  pr_sd_alpha = 1,
  pr_a_theta = 0.001,
  pr_b_theta = 0.001,
  missing.val = 99,
  verbose = FALSE
)
```

**Arguments**

|               |   |
|---------------|---|
| data          | Matrix; a binary or continuous item response matrix for analysis. Each row represents a respondent, and each column contains responses to the corresponding item. |
| ndim          | Integer; the dimension of the latent space. Default is 2.   |
| niter         | Integer; the total number of MCMC iterations to run. Default is 15000.  |
| nburn         | Integer; the number of initial MCMC iterations to discard as burn-in. Default is 2500.  |
| nthin         | Integer; the number of MCMC iterations to thin. Default is 5.   |
| nprint        | Integer; the interval at which MCMC samples are displayed during execution. Default is 500.   |
| jump_beta     | Numeric; the jumping rule for the beta proposal density. Default is 0.4.  |
| jump_theta    | Numeric; the jumping rule for the theta proposal density. Default is 1.0.   |
| jump_alpha    | Numeric; the jumping rule for the alpha proposal density. Default is 1.0.   |
| jump_z        | Numeric; the jumping rule for the z proposal density. Default is 0.5.   |
| jump_w        | Numeric; the jumping rule for the w proposal density. Default is 0.5.   |
| pr_mean_beta  | Numeric; the mean of the normal prior for beta. Default is 0.   |
| pr_sd_beta    | Numeric; the standard deviation of the normal prior for beta. Default is 1.0.   |
| pr_mean_theta | Numeric; the mean of the normal prior for theta. Default is 0.  |
| pr_mean_alpha | Numeric; the mean of the log normal prior for alpha. Default is 0.5.  |
| pr_sd_alpha   | Numeric; the standard deviation of the log normal prior for alpha. Default is 1.0.  |
| pr_a_theta    | Numeric; the shape parameter of the inverse gamma prior for the variance of theta. Default is 0.001.  |
| pr_b_theta    | Numeric; the scale parameter of the inverse gamma prior for the variance of theta. Default is 0.001.  |
| missing.val   | Numeric; A number to replace missing values. Default is 99.   |
| verbose       | Logical; If TRUE, MCMC samples are printed for each nprint. Default is FALSE.   |

**Details**

lsirm2pl\_fixed\_gamma\_mcar models the probability of correct response by respondent  $j$  to item  $i$  with item effect  $\beta_i$ , respondent effect  $\theta_j$  and the distance between latent position  $w_i$  of item  $i$  and latent position  $z_j$  of respondent  $j$  in the shared metric space. For 2pl model, the item effect is assumed to have additional discrimination parameter  $\alpha_i$  multiplied by  $\theta_j$ :

$$\text{logit}(P(Y_{j,i} = 1 | \theta_j, \alpha_i, \beta_i, z_j, w_i)) = \theta_j * \alpha_i + \beta_i - ||z_j - w_i||$$

Under the assumption of missing completely at random, the model ignores the missing element in doing inference. For the details of missing completely at random assumption and data augmentation, see References.

**Value**

`lsirm2pl_fixed_gamma_mar` returns an object of list containing the following components:

|                                   |  |
|-----------------------------------|--|
| <code>data</code>                 | Data frame or matrix containing the variables in the model.  |
| <code>missing.val</code>          | A number to replace missing values.  |
| <code>bic</code>                  | Numeric value with the corresponding BIC.  |
| <code>mcmc_inf</code>             | Details about the number of MCMC iterations, burn-in periods, and thinning intervals.  |
| <code>map_inf</code>              | The log maximum a posteriori (MAP) value and the iteration number at which this MAP value occurs.  |
| <code>beta_estimate</code>        | Posterior estimates of the beta parameter.   |
| <code>theta_estimate</code>       | Posterior estimates of the theta parameter.  |
| <code>sigma_theta_estimate</code> | Posterior estimates of the standard deviation of theta.  |
| <code>z_estimate</code>           | Posterior estimates of the z parameter.  |
| <code>w_estimate</code>           | Posterior estimates of the w parameter.  |
| <code>beta</code>                 | Posterior samples of the beta parameter.   |
| <code>theta</code>                | Posterior samples of the theta parameter.  |
| <code>theta_sd</code>             | Posterior samples of the standard deviation of theta.  |
| <code>z</code>                    | Posterior samples of the z parameter, represented as a 3-dimensional matrix where the last axis denotes the dimension of the latent space. |
| <code>w</code>                    | Posterior samples of the w parameter, represented as a 3-dimensional matrix where the last axis denotes the dimension of the latent space. |
| <code>accept_beta</code>          | Acceptance ratio for the beta parameter.   |
| <code>accept_theta</code>         | Acceptance ratio for the theta parameter.  |
| <code>accept_z</code>             | Acceptance ratio for the z parameter.  |
| <code>accept_w</code>             | Acceptance ratio for the w parameter.  |
| <code>alpha_estimate</code>       | Posterior estimates of the alpha parameter.  |
| <code>alpha</code>                | Posterior estimates of the alpha parameter.  |
| <code>accept_alpha</code>         | Acceptance ratio for the alpha parameter.  |

**References**

Little, R. J., & Rubin, D. B. (2019). Statistical analysis with missing data (Vol. 793). John Wiley & Sons.

**Examples**

```
# generate example item response matrix
data      <- matrix(rbinom(500, size = 1, prob = 0.5),ncol=10,nrow=50)

# generate example missing indicator matrix
missing_mat <- matrix(rbinom(500, size = 1, prob = 0.2),ncol=10,nrow=50)
```

```
# make missing value with missing indicator matrix
data[missing_mat==1] <- 99

lsirm_result <- lsirm2pl_fixed_gamma_mcar(data)

# The code following can achieve the same result.
lsirm_result <- lsirm(data ~ lsirm2pl(spikenslab = FALSE, fixed_gamma = TRUE,
                                     missing_data = "mcar"))
```

lsirm2pl\_mar

*2PL LSIRM for missing at random data.*

### Description

[lsirm2pl\\_mar](#) is used to fit 2PL LSIRM in incomplete data assumed to be missing at random. [lsirm2pl\\_mar](#) factorizes item response matrix into column-wise item effect, row-wise respondent effect in a latent space, while considering the missing element under the assumption of missing at random. Unlike 1PL model, 2PL model assumes the item effect can vary according to respondent, allowing additional parameter multiplied with respondent effect. The resulting latent space provides an interaction map that represents interactions between respondents and items.

### Usage

```
lsirm2pl_mar(
  data,
  ndim = 2,
  niter = 15000,
  nburn = 2500,
  nthin = 5,
  nprint = 500,
  jump_beta = 0.4,
  jump_theta = 1,
  jump_alpha = 1,
  jump_gamma = 0.025,
  jump_z = 0.5,
  jump_w = 0.5,
  pr_mean_beta = 0,
  pr_sd_beta = 1,
  pr_mean_theta = 0,
  pr_mean_gamma = 0.5,
  pr_sd_gamma = 1,
  pr_mean_alpha = 0.5,
  pr_sd_alpha = 1,
  pr_a_theta = 0.001,
  pr_b_theta = 0.001,
  missing.val = 99,
```

```

    verbose = FALSE
)

```

### Arguments

|                            |   |
|----------------------------|---|
| <code>data</code>          | Matrix; a binary or continuous item response matrix for analysis. Each row represents a respondent, and each column contains responses to the corresponding item. |
| <code>ndim</code>          | Integer; the dimension of the latent space. Default is 2.   |
| <code>niter</code>         | Integer; the total number of MCMC iterations to run. Default is 15000.  |
| <code>nburn</code>         | Integer; the number of initial MCMC iterations to discard as burn-in. Default is 2500.  |
| <code>nthin</code>         | Integer; the number of MCMC iterations to thin. Default is 5.   |
| <code>nprint</code>        | Integer; the interval at which MCMC samples are displayed during execution. Default is 500.   |
| <code>jump_beta</code>     | Numeric; the jumping rule for the beta proposal density. Default is 0.4.  |
| <code>jump_theta</code>    | Numeric; the jumping rule for the theta proposal density. Default is 1.0.   |
| <code>jump_alpha</code>    | Numeric; the jumping rule for the alpha proposal density. Default is 1.0.   |
| <code>jump_gamma</code>    | Numeric; the jumping rule for the gamma proposal density. Default is 0.025.   |
| <code>jump_z</code>        | Numeric; the jumping rule for the z proposal density. Default is 0.5.   |
| <code>jump_w</code>        | Numeric; the jumping rule for the w proposal density. Default is 0.5.   |
| <code>pr_mean_beta</code>  | Numeric; the mean of the normal prior for beta. Default is 0.   |
| <code>pr_sd_beta</code>    | Numeric; the standard deviation of the normal prior for beta. Default is 1.0.   |
| <code>pr_mean_theta</code> | Numeric; the mean of the normal prior for theta. Default is 0.  |
| <code>pr_mean_gamma</code> | Numeric; mean of log normal prior for gamma. Default is 0.5.  |
| <code>pr_sd_gamma</code>   | Numeric; standard deviation of log normal prior for gamma. Default is 1.0.  |
| <code>pr_mean_alpha</code> | Numeric; the mean of the log normal prior for alpha. Default is 0.5.  |
| <code>pr_sd_alpha</code>   | Numeric; the standard deviation of the log normal prior for alpha. Default is 1.0.  |
| <code>pr_a_theta</code>    | Numeric; the shape parameter of the inverse gamma prior for the variance of theta. Default is 0.001.  |
| <code>pr_b_theta</code>    | Numeric; the scale parameter of the inverse gamma prior for the variance of theta. Default is 0.001.  |
| <code>missing.val</code>   | Numeric; A number to replace missing values. Default is 99.   |
| <code>verbose</code>       | Logical; If TRUE, MCMC samples are printed for each nprint. Default is FALSE.   |

## Details

lsirm2pl\_mar models the probability of correct response by respondent  $j$  to item  $i$  with item effect  $\beta_i$ , respondent effect  $\theta_j$  in the shared metric space, with  $\gamma$  represents the weight of the distance term. For 2pl model, the item effect is assumed to have additional discrimination parameter  $\alpha_i$  multiplied by  $\theta_j$ :

$$\text{logit}(P(Y_{j,i} = 1|\theta_j, \alpha_i, \beta_i, \gamma, z_j, w_i)) = \theta_j * \alpha_i + \beta_i - \gamma||z_j - w_i||$$

Under the assumption of missing at random, the model takes the missing element into consideration in the sampling procedure. For the details of missing at random assumption and data augmentation, see References.

## Value

lsirm2pl\_mar returns an object of list containing the following components:

|                      |  |
|----------------------|--|
| data                 | Data frame or matrix containing the variables in the model.  |
| missing.val          | A number to replace missing values.  |
| bic                  | Numeric value with the corresponding BIC.  |
| mcmc_inf             | Details about the number of MCMC iterations, burn-in periods, and thinning intervals.  |
| map_inf              | The log maximum a posteriori (MAP) value and the iteration number at which this MAP value occurs.  |
| beta_estimate        | Posterior estimates of the beta parameter.   |
| theta_estimate       | Posterior estimates of the theta parameter.  |
| sigma_theta_estimate | Posterior estimates of the standard deviation of theta.  |
| gamma_estimate       | posterior estimates of gamma parameter.  |
| z_estimate           | Posterior estimates of the z parameter.  |
| w_estimate           | Posterior estimates of the w parameter.  |
| imp_estimate         | Probability of imputating a missing value with 1.  |
| beta                 | Posterior samples of the beta parameter.   |
| theta                | Posterior samples of the theta parameter.  |
| gamma                | Posterior samples of the gamma parameter.  |
| theta_sd             | Posterior samples of the standard deviation of theta.  |
| z                    | Posterior samples of the z parameter, represented as a 3-dimensional matrix where the last axis denotes the dimension of the latent space. |
| w                    | Posterior samples of the w parameter, represented as a 3-dimensional matrix where the last axis denotes the dimension of the latent space. |
| imp                  | Imputation for missing Values using posterior samples.   |
| accept_beta          | Acceptance ratio for the beta parameter.   |
| accept_theta         | Acceptance ratio for the theta parameter.  |
| accept_z             | Acceptance ratio for the z parameter.  |

accept\_w            Acceptance ratio for the w parameter.  
 accept\_gamma      Acceptance ratio for the gamma parameter.  
 alpha\_estimate    Posterior estimates of the alpha parameter.  
 alpha              Posterior estimates of the alpha parameter.  
 accept\_alpha      Acceptance ratio for the alpha parameter.

## References

Little, R. J., & Rubin, D. B. (2019). Statistical analysis with missing data (Vol. 793). John Wiley & Sons.

## Examples

```
# generate example item response matrix
data <- matrix(rbinom(500, size = 1, prob = 0.5), ncol=10, nrow=50)

# generate example missing indicator matrix
missing_mat <- matrix(rbinom(500, size = 1, prob = 0.2), ncol=10, nrow=50)

# make missing value with missing indicator matrix
data[missing_mat==1] <- 99

lsirm_result <- lsirm2pl_mar(data)

# The code following can achieve the same result.
lsirm_result <- lsirm(data ~ lsirm2pl(spikenslab = FALSE, fixed_gamma = FALSE,
  missing_data = "mar"))
```

---

|                 |  |
|-----------------|--|
| lsirm2pl_mar_ss | <i>2PL LSIRM with model selection approach for missing at random data.</i> |
|-----------------|--|

---

## Description

[lsirm2pl\\_mar\\_ss](#) is used to fit 2PL LSIRM based on spike-and-slab priors in incomplete data assumed to be missing at random. [lsirm2pl\\_mar\\_ss](#) factorizes item response matrix into column-wise item effect, row-wise respondent effect in a latent space, while considering the missing element under the assumption of missing at random. Unlike 1PL model, 2PL model assumes the item effect can vary according to respondent, allowing additional parameter multiplied with respondent effect. The resulting latent space provides an interaction map that represents interactions between respondents and items.



**Usage**

```
lsirm2pl_mar_ss(
  data,
  ndim = 2,
  niter = 15000,
  nburn = 2500,
  nthin = 5,
  nprint = 500,
  jump_beta = 0.4,
  jump_theta = 1,
  jump_alpha = 1,
  jump_gamma = 1,
  jump_z = 0.5,
  jump_w = 0.5,
  pr_mean_beta = 0,
  pr_sd_beta = 1,
  pr_mean_theta = 0,
  pr_spike_mean = -3,
  pr_spike_sd = 1,
  pr_slab_mean = 0.5,
  pr_slab_sd = 1,
  pr_mean_alpha = 0.5,
  pr_sd_alpha = 1,
  pr_a_theta = 0.001,
  pr_b_theta = 0.001,
  pr_xi_a = 1,
  pr_xi_b = 1,
  missing.val = 99,
  verbose = FALSE
)
```

**Arguments**

|            |   |
|------------|---|
| data       | Matrix; a binary or continuous item response matrix for analysis. Each row represents a respondent, and each column contains responses to the corresponding item. |
| ndim       | Integer; the dimension of the latent space. Default is 2.   |
| niter      | Integer; the total number of MCMC iterations to run. Default is 15000.  |
| nburn      | Integer; the number of initial MCMC iterations to discard as burn-in. Default is 2500.  |
| nthin      | Integer; the number of MCMC iterations to thin. Default is 5.   |
| nprint     | Integer; the interval at which MCMC samples are displayed during execution. Default is 500.   |
| jump_beta  | Numeric; the jumping rule for the beta proposal density. Default is 0.4.  |
| jump_theta | Numeric; the jumping rule for the theta proposal density. Default is 1.0.   |
| jump_alpha | Numeric; the jumping rule for the alpha proposal density. Default is 1.0.   |

|               |  |
|---------------|--|
| jump_gamma    | Numeric; the jumping rule for the theta proposal density. Default is 1.0.                            |
| jump_z        | Numeric; the jumping rule for the z proposal density. Default is 0.5.                                |
| jump_w        | Numeric; the jumping rule for the w proposal density. Default is 0.5.                                |
| pr_mean_beta  | Numeric; the mean of the normal prior for beta. Default is 0.  |
| pr_sd_beta    | Numeric; the standard deviation of the normal prior for beta. Default is 1.0.                        |
| pr_mean_theta | Numeric; the mean of the normal prior for theta. Default is 0.                                       |
| pr_spike_mean | Numeric; the mean of spike prior for log gamma. Default is -3.                                       |
| pr_spike_sd   | Numeric; the standard deviation of spike prior for log gamma. Default is 1.                          |
| pr_slab_mean  | Numeric; the mean of spike prior for log gamma. Default is 0.5.                                      |
| pr_slab_sd    | Numeric; the standard deviation of spike prior for log gamma. Default is 1.                          |
| pr_mean_alpha | Numeric; the mean of the log normal prior for alpha. Default is 0.5.                                 |
| pr_sd_alpha   | Numeric; the standard deviation of the log normal prior for alpha. Default is 1.0.                   |
| pr_a_theta    | Numeric; the shape parameter of the inverse gamma prior for the variance of theta. Default is 0.001. |
| pr_b_theta    | Numeric; the scale parameter of the inverse gamma prior for the variance of theta. Default is 0.001. |
| pr_xi_a       | Numeric; the first shape parameter of beta prior for latent variable xi. Default is 1.               |
| pr_xi_b       | Numeric; the second shape parameter of beta prior for latent variable xi. Default is 1.              |
| missing.val   | Numeric; a number to replace missing values. Default is 99.  |
| verbose       | Logical; If TRUE, MCMC samples are printed for each nprint. Default is FALSE.                        |

## Details

lsirm2pl\_mar\_ss models the probability of correct response by respondent  $j$  to item  $i$  with item effect  $\beta_i$ , respondent effect  $\theta_j$  in the shared metric space, with  $\gamma$  represents the weight of the distance term. For 2pl model, the item effect is assumed to have additional discrimination parameter  $\alpha_i$  multiplied by  $\theta_j$ :

$$\text{logit}(P(Y_{j,i} = 1 | \theta_j, \alpha_i, \beta_i, \gamma, z_j, w_i)) = \theta_j * \alpha_i + \beta_i - \gamma ||z_j - w_i||$$

Under the assumption of missing at random, the model takes the missing element into consideration in the sampling procedure. For the details of missing at random assumption and data augmentation, see References. lsirm2pl\_mar\_ss model include model selection approach based on spike-and-slab priors for log gamma. For detail of spike-and-slab priors, see References.

## Value

lsirm2pl\_mar\_ss returns an object of list containing the following components:

data                      Data frame or matrix containing the variables in the model.

|                      |   |
|----------------------|---|
| missing.val          | A number to replace missing values.   |
| bic                  | Numeric value with the corresponding BIC.   |
| mcmc_inf             | Details about the number of MCMC iterations, burn-in periods, and thinning intervals.   |
| map_inf              | The log maximum a posteriori (MAP) value and the iteration number at which this MAP value occurs.   |
| beta_estimate        | Posterior estimates of the beta parameter.  |
| theta_estimate       | Posterior estimates of the theta parameter.   |
| sigma_theta_estimate | Posterior estimates of the standard deviation of theta.   |
| gamma_estimate       | posterior estimates of gamma parameter.   |
| z_estimate           | Posterior estimates of the z parameter.   |
| w_estimate           | Posterior estimates of the w parameter.   |
| beta                 | Posterior samples of the beta parameter.  |
| theta                | Posterior samples of the theta parameter.   |
| gamma                | Posterior samples of the gamma parameter.   |
| theta_sd             | Posterior samples of the standard deviation of theta.   |
| z                    | Posterior samples of the z parameter, represented as a 3-dimensional matrix where the last axis denotes the dimension of the latent space.  |
| w                    | Posterior samples of the w parameter, represented as a 3-dimensional matrix where the last axis denotes the dimension of the latent space.  |
| pi                   | Posterior samples of phi which is indicator of spike and slab prior. If phi is 1, log gamma follows the slab prior, otherwise follows the spike prior.                              |
| imp                  | Imputation for missing Values using posterior samples.  |
| accept_beta          | Acceptance ratio for the beta parameter.  |
| accept_theta         | Acceptance ratio for the theta parameter.   |
| accept_z             | Acceptance ratio for the z parameter.   |
| accept_w             | Acceptance ratio for the w parameter.   |
| accept_gamma         | Acceptance ratio for the gamma parameter.   |
| pi_estimate          | Posterior estimation of phi. inclusion probability of gamma. if estimation of phi is less than 0.5, choose Rasch model with gamma = 0, otherwise latent space model with gamma > 0. |
| imp_estimate         | Probability of imputating a missing value with 1.   |
| alpha_estimate       | Posterior estimates of the alpha parameter.   |
| alpha                | Posterior estimates of the alpha parameter.   |
| accept_alpha         | Acceptance ratio for the alpha parameter.   |

## References

Little, R. J., & Rubin, D. B. (2019). Statistical analysis with missing data (Vol. 793). John Wiley & Sons. Ishwaran, H., & Rao, J. S. (2005). Spike and slab variable selection: Frequentist and Bayesian strategies. *The Annals of Statistics*, 33(2), 730-773.

### Examples

```
# generate example item response matrix
data      <- matrix(rbinom(500, size = 1, prob = 0.5), ncol=10, nrow=50)

# generate example missing indicator matrix
missing_mat <- matrix(rbinom(500, size = 1, prob = 0.2), ncol=10, nrow=50)

# make missing value with missing indicator matrix
data[missing_mat==1] <- 99

lsirm_result <- lsirm2pl_mar_ss(data)

# The code following can achieve the same result.
lsirm_result <- lsirm(data ~ lsirm2pl(spikenslab = TRUE, fixed_gamma = FALSE,
                                     missing_data = "mar"))
```

---

lsirm2pl\_mcar

2PL LSIRM for missing completely at random data.

---

### Description

[lsirm2pl\\_mcar](#) is used to fit 2PL LSIRM in incomplete data assumed to be missing completely at random. [lsirm2pl\\_mcar](#) factorizes item response matrix into column-wise item effect, row-wise respondent effect in a latent space, while ignoring the missing element under the assumption of missing completely at random. Unlike 1PL model, 2PL model assumes the item effect can vary according to respondent, allowing additional parameter multiplied with respondent effect. The resulting latent space provides an interaction map that represents interactions between respondents and items.

### Usage

```
lsirm2pl_mcar(
  data,
  ndim = 2,
  niter = 15000,
  nburn = 2500,
  nthin = 5,
  nprint = 500,
  jump_beta = 0.4,
  jump_theta = 1,
  jump_alpha = 1,
  jump_gamma = 0.025,
  jump_z = 0.5,
  jump_w = 0.5,
  pr_mean_beta = 0,
  pr_sd_beta = 1,
  pr_mean_theta = 0,
```

```

pr_mean_gamma = 0.5,
pr_sd_gamma = 1,
pr_mean_alpha = 0.5,
pr_sd_alpha = 1,
pr_a_theta = 0.001,
pr_b_theta = 0.001,
missing.val = 99,
verbose = FALSE
)

```

### Arguments

|               |   |
|---------------|---|
| data          | Matrix; a binary or continuous item response matrix for analysis. Each row represents a respondent, and each column contains responses to the corresponding item. |
| ndim          | Integer; the dimension of the latent space. Default is 2.   |
| niter         | Integer; the total number of MCMC iterations to run. Default is 15000.  |
| nburn         | Integer; the number of initial MCMC iterations to discard as burn-in. Default is 2500.  |
| nthin         | Integer; the number of MCMC iterations to thin. Default is 5.   |
| nprint        | Integer; the interval at which MCMC samples are displayed during execution. Default is 500.   |
| jump_beta     | Numeric; the jumping rule for the beta proposal density. Default is 0.4.  |
| jump_theta    | Numeric; the jumping rule for the theta proposal density. Default is 1.0.   |
| jump_alpha    | Numeric; the jumping rule for the alpha proposal density. Default is 1.0.   |
| jump_gamma    | Numeric; the jumping rule for the gamma proposal density. Default is 0.025  |
| jump_z        | Numeric; the jumping rule for the z proposal density. Default is 0.5.   |
| jump_w        | Numeric; the jumping rule for the w proposal density. Default is 0.5.   |
| pr_mean_beta  | Numeric; the mean of the normal prior for beta. Default is 0.   |
| pr_sd_beta    | Numeric; the standard deviation of the normal prior for beta. Default is 1.0.   |
| pr_mean_theta | Numeric; the mean of the normal prior for theta. Default is 0.  |
| pr_mean_gamma | Numeric; mean of log normal prior for gamma. Default is 0.5.  |
| pr_sd_gamma   | Numeric; standard deviation of log normal prior for gamma. Default is 1.0.  |
| pr_mean_alpha | Numeric; the mean of the log normal prior for alpha. Default is 0.5.  |
| pr_sd_alpha   | Numeric; the standard deviation of the log normal prior for alpha. Default is 1.0.  |
| pr_a_theta    | Numeric; the shape parameter of the inverse gamma prior for the variance of theta. Default is 0.001.  |
| pr_b_theta    | Numeric; the scale parameter of the inverse gamma prior for the variance of theta. Default is 0.001.  |
| missing.val   | Numeric; A number to replace missing values. Default is 99.   |
| verbose       | Logical; If TRUE, MCMC samples are printed for each nprint. Default is FALSE.   |

## Details

lsirm2pl\_mcar models the probability of correct response by respondent  $j$  to item  $i$  with item effect  $\beta_i$ , respondent effect  $\theta_j$  in the shared metric space, with  $\gamma$  represents the weight of the distance term. For 2pl model, the the item effect is assumed to have additional discrimination parameter  $\alpha_i$  multiplied by  $\theta_j$ :

$$\text{logit}(P(Y_{j,i} = 1 | \theta_j, \alpha_i, \beta_i, \gamma, z_j, w_i)) = \theta_j * \alpha_i + \beta_i - \gamma ||z_j - w_i||$$

Under the assumption of missing completely at random, the model ignores the missing element in doing inference. For the details of missing completely at random assumption and data augmentation, see References.

## Value

lsirm2pl\_mar returns an object of list containing the following components:

|                      |  |
|----------------------|--|
| data                 | A data frame or matrix containing the variables used in the model.   |
| missing.val          | A number to replace missing values.  |
| bic                  | Numeric value with the corresponding BIC.  |
| mcmc_inf             | Details about the number of MCMC iterations, burn-in periods, and thinning intervals.  |
| map_inf              | The log maximum a posteriori (MAP) value and the iteration number at which this MAP value occurs.  |
| beta_estimate        | Posterior estimates of the beta parameter.   |
| theta_estimate       | Posterior estimates of the theta parameter.  |
| sigma_theta_estimate | Posterior estimates of the standard deviation of theta.  |
| gamma_estimate       | Posterior estimates of gamma parameter.  |
| z_estimate           | Posterior estimates of the z parameter.  |
| w_estimate           | Posterior estimates of the w parameter.  |
| beta                 | Posterior samples of the beta parameter.   |
| theta                | Posterior samples of the theta parameter.  |
| theta_sd             | Posterior samples of the standard deviation of theta.  |
| gamma                | Posterior samples of the gamma parameter.  |
| z                    | Posterior samples of the z parameter, represented as a 3-dimensional matrix where the last axis denotes the dimension of the latent space. |
| w                    | Posterior samples of the w parameter, represented as a 3-dimensional matrix where the last axis denotes the dimension of the latent space. |
| accept_beta          | Acceptance ratio for the beta parameter.   |
| accept_theta         | Acceptance ratio for the theta parameter.  |
| accept_z             | Acceptance ratio for the z parameter.  |
| accept_w             | Acceptance ratio for the w parameter.  |
| accept_gamma         | Acceptance ratio for the gamma parameter.  |
| alpha_estimate       | Posterior estimates of the alpha parameter.  |
| alpha                | Posterior estimates of the alpha parameter.  |
| accept_alpha         | Acceptance ratio for the alpha parameter.  |

## References

Little, R. J., & Rubin, D. B. (2019). Statistical analysis with missing data (Vol. 793). John Wiley & Sons.

## Examples

```
# generate example item response matrix
data      <- matrix(rbinom(500, size = 1, prob = 0.5), ncol=10, nrow=50)

# generate example missing indicator matrix
missing_mat  <- matrix(rbinom(500, size = 1, prob = 0.2), ncol=10, nrow=50)

# make missing value with missing indicator matrix
data[missing_mat==1] <- 99

lsirm_result <- lsirm2pl_mcar(data)

# The code following can achieve the same result.
lsirm_result <- lsirm(data ~ lsirm2pl(spikenslab = FALSE, fixed_gamma = FALSE,
                                     missing_data = "mcar"))
```

---

|                  |   |
|------------------|---|
| lsirm2pl_mcar_ss | <i>2PL LSIRM with model selection approach for missing completely at random data.</i> |
|------------------|---|

---

## Description

[lsirm2pl\\_mar\\_ss](#) is used to fit 2PL LSIRM based on spike-and-slab priors in incomplete data assumed to be missing completely at random. [lsirm2pl\\_mar\\_ss](#) factorizes item response matrix into column-wise item effect, row-wise respondent effect in a latent space, while ignoring the missing element under the assumption of missing completely at random. Unlike 1PL model, 2PL model assumes the item effect can vary according to respondent, allowing additional parameter multiplied with respondent effect. The resulting latent space provides an interaction map that represents interactions between respondents and items.

## Usage

```
lsirm2pl_mcar_ss(
  data,
  ndim = 2,
  niter = 15000,
  nburn = 2500,
  nthin = 5,
  nprint = 500,
  jump_beta = 0.4,
  jump_theta = 1,
  jump_alpha = 1,
```

```

jump_gamma = 1,
jump_z = 0.5,
jump_w = 0.5,
pr_mean_beta = 0,
pr_sd_beta = 1,
pr_mean_theta = 0,
pr_spike_mean = -3,
pr_spike_sd = 1,
pr_slab_mean = 0.5,
pr_slab_sd = 1,
pr_mean_alpha = 0.5,
pr_sd_alpha = 1,
pr_a_theta = 0.001,
pr_b_theta = 0.001,
pr_xi_a = 1,
pr_xi_b = 1,
missing.val = 99,
verbose = FALSE
)

```

### Arguments

|               |   |
|---------------|---|
| data          | Matrix; a binary or continuous item response matrix for analysis. Each row represents a respondent, and each column contains responses to the corresponding item. |
| ndim          | Integer; the dimension of the latent space. Default is 2.   |
| niter         | Integer; the total number of MCMC iterations to run. Default is 15000.  |
| nburn         | Integer; the number of initial MCMC iterations to discard as burn-in. Default is 2500.  |
| nthin         | Integer; the number of MCMC iterations to thin. Default is 5.   |
| nprint        | Integer; the interval at which MCMC samples are displayed during execution. Default is 500.   |
| jump_beta     | Numeric; the jumping rule for the beta proposal density. Default is 0.4.  |
| jump_theta    | Numeric; the jumping rule for the theta proposal density. Default is 1.0.   |
| jump_alpha    | Numeric; the jumping rule for the alpha proposal density. Default is 1.0.   |
| jump_gamma    | Numeric; the jumping rule for the gamma proposal density. Default is 1.0.   |
| jump_z        | Numeric; the jumping rule for the z proposal density. Default is 0.5.   |
| jump_w        | Numeric; the jumping rule for the w proposal density. Default is 0.5.   |
| pr_mean_beta  | Numeric; the mean of the normal prior for beta. Default is 0.   |
| pr_sd_beta    | Numeric; the standard deviation of the normal prior for beta. Default is 1.0.   |
| pr_mean_theta | Numeric; the mean of the normal prior for theta. Default is 0.  |
| pr_spike_mean | Numeric; the mean of spike prior for log gamma. Default is -3.  |
| pr_spike_sd   | Numeric; the standard deviation of spike prior for log gamma. Default is 1.   |
| pr_slab_mean  | Numeric; the mean of spike prior for log gamma. Default is 0.5.   |



|               |  |
|---------------|--|
| pr_slab_sd    | Numeric; the standard deviation of spike prior for log gamma. Default is 1.                          |
| pr_mean_alpha | Numeric; the mean of the log normal prior for alpha. Default is 0.5.                                 |
| pr_sd_alpha   | Numeric; the standard deviation of the log normal prior for alpha. Default is 1.0.                   |
| pr_a_theta    | Numeric; the shape parameter of the inverse gamma prior for the variance of theta. Default is 0.001. |
| pr_b_theta    | Numeric; the scale parameter of the inverse gamma prior for the variance of theta. Default is 0.001. |
| pr_xi_a       | Numeric; the first shape parameter of beta prior for latent variable xi. Default is 1.               |
| pr_xi_b       | Numeric; the second shape parameter of beta prior for latent variable xi. Default is 1.              |
| missing.val   | Numeric; a number to replace missing values. Default is 99.  |
| verbose       | Logical; If TRUE, MCMC samples are printed for each nprint. Default is FALSE.                        |

## Details

lsirm2pl\_mcar\_ss models the probability of correct response by respondent  $j$  to item  $i$  with item effect  $\beta_i$ , respondent effect  $\theta_j$  in the shared metric space, with  $\gamma$  represents the weight of the distance term. For 2pl model, the item effect is assumed to have additional discrimination parameter  $\alpha_i$  multiplied by  $\theta_j$ :

$$\text{logit}(P(Y_{j,i} = 1 | \theta_j, \alpha_i, \beta_i, \gamma, z_j, w_i)) = \theta_j * \alpha_i + \beta_i - \gamma ||z_j - w_i||$$

Under the assumption of missing at random, the model takes the missing element into consideration in the sampling procedure. For the details of missing at random assumption and data augmentation, see References. lsirm2pl\_mcar\_ss model include model selection approach based on spike-and-slab priors for log gamma. For detail of spike-and-slab priors, see References.

## Value

lsirm2pl\_mar\_ss returns an object of list containing the following components:

|                      |   |
|----------------------|---|
| data                 | Data frame or matrix containing the variables in the model.                                       |
| missing.val          | A number to replace missing values.   |
| bic                  | Numeric value with the corresponding BIC.   |
| mcmc_inf             | Details about the number of MCMC iterations, burn-in periods, and thinning intervals.             |
| map_inf              | The log maximum a posteriori (MAP) value and the iteration number at which this MAP value occurs. |
| beta_estimate        | Posterior estimates of the beta parameter.  |
| theta_estimate       | Posterior estimates of the theta parameter.   |
| sigma_theta_estimate | Posterior estimates of the standard deviation of theta.   |



---

lsirm2pl\_normal\_fixed\_gamma

2PL LSIRM fixing gamma to 1 with normal likelihood

---

## Description

[lsirm2pl\\_normal\\_fixed\\_gamma](#) is used to fit 2PL LSIRM with gamma fixed to 1 for continuous variable. [lsirm2pl\\_normal\\_fixed\\_gamma](#) factorizes item response matrix into column-wise item effect, row-wise respondent effect and further embeds interaction effect in a latent space. Unlike 1PL model, 2PL model assumes the item effect can vary according to respondent, allowing additional parameter multiplied with respondent effect. The resulting latent space provides an interaction map that represents interactions between respondents and items.

## Usage

```
lsirm2pl_normal_fixed_gamma(
  data,
  ndim = 2,
  niter = 15000,
  nburn = 2500,
  nthin = 5,
  nprint = 500,
  jump_beta = 0.4,
  jump_theta = 1,
  jump_alpha = 1,
  jump_z = 0.5,
  jump_w = 0.5,
  pr_mean_beta = 0,
  pr_sd_beta = 1,
  pr_mean_theta = 0,
  pr_mean_alpha = 0.5,
  pr_sd_alpha = 1,
  pr_a_theta = 0.001,
  pr_b_theta = 0.001,
  pr_a_eps = 0.001,
  pr_b_eps = 0.001,
  verbose = FALSE
)
```

## Arguments

|       |   |
|-------|---|
| data  | Matrix; a binary or continuous item response matrix for analysis. Each row represents a respondent, and each column contains responses to the corresponding item. |
| ndim  | Integer; the dimension of the latent space. Default is 2.   |
| niter | Integer; the total number of MCMC iterations to run. Default is 15000.  |

|               |  |
|---------------|--|
| nburn         | Integer; the number of initial MCMC iterations to discard as burn-in. Default is 2500.                 |
| nthin         | Integer; the number of MCMC iterations to thin. Default is 5.  |
| nprint        | Integer; the interval at which MCMC samples are displayed during execution. Default is 500.            |
| jump_beta     | Numeric; the jumping rule for the beta proposal density. Default is 0.4.                               |
| jump_theta    | Numeric; the jumping rule for the theta proposal density. Default is 1.0.                              |
| jump_alpha    | Numeric; the jumping rule for the alpha proposal density. Default is 1.0.                              |
| jump_z        | Numeric; the jumping rule for the z proposal density. Default is 0.5.                                  |
| jump_w        | Numeric; the jumping rule for the w proposal density. Default is 0.5.                                  |
| pr_mean_beta  | Numeric; the mean of the normal prior for beta. Default is 0.  |
| pr_sd_beta    | Numeric; the standard deviation of the normal prior for beta. Default is 1.0.                          |
| pr_mean_theta | Numeric; the mean of the normal prior for theta. Default is 0.   |
| pr_mean_alpha | Numeric; the mean of the log normal prior for alpha. Default is 0.5.                                   |
| pr_sd_alpha   | Numeric; the standard deviation of the log normal prior for alpha. Default is 1.0.                     |
| pr_a_theta    | Numeric; the shape parameter of the inverse gamma prior for the variance of theta. Default is 0.001.   |
| pr_b_theta    | Numeric; the scale parameter of the inverse gamma prior for the variance of theta. Default is 0.001.   |
| pr_a_eps      | Numeric; the shape parameter of inverse gamma prior for variance of data likelihood. Default is 0.001. |
| pr_b_eps      | Numeric; the scale parameter of inverse gamma prior for variance of data likelihood. Default is 0.001. |
| verbose       | Logical; If TRUE, MCMC samples are printed for each nprint. Default is FALSE.                          |

## Details

`lsirm2pl_normal_fixed_gamma` models the continuous value of response by respondent  $j$  to item  $i$  with item effect  $\beta_i$ , respondent effect  $\theta_j$  and the distance between latent position  $w_i$  of item  $i$  and latent position  $z_j$  of respondent  $j$  in the shared metric space. For 2pl model, the the item effect is assumed to have additional discrimination parameter  $\alpha_i$  multiplied by  $\theta_j$ :

$$Y_{j,i} = \theta_j + \beta_i - \gamma ||z_j - w_i|| + e_{j,i}$$

where the error  $e_{j,i} \sim N(0, \sigma^2)$

## Value

`lsirm2pl_normal_fixed_gamma` returns an object of list containing the following components:

|      |  |
|------|--|
| data | A data frame or matrix containing the variables used in the model.     |
| bic  | A numeric value representing the Bayesian Information Criterion (BIC). |

|                      |  |
|----------------------|--|
| mcmc_inf             | Details about the number of MCMC iterations, burn-in periods, and thinning intervals.  |
| map_inf              | The log maximum a posteriori (MAP) value and the iteration number at which this MAP value occurs.  |
| beta_estimate        | Posterior estimates of the beta parameter.   |
| theta_estimate       | Posterior estimates of the theta parameter.  |
| sigma_theta_estimate | Posterior estimates of the standard deviation of theta.  |
| z_estimate           | Posterior estimates of the z parameter.  |
| w_estimate           | Posterior estimates of the w parameter.  |
| beta                 | Posterior samples of the beta parameter.   |
| theta                | Posterior samples of the theta parameter.  |
| theta_sd             | Posterior samples of the standard deviation of theta.  |
| z                    | Posterior samples of the z parameter, represented as a 3-dimensional matrix where the last axis denotes the dimension of the latent space. |
| w                    | Posterior samples of the w parameter, represented as a 3-dimensional matrix where the last axis denotes the dimension of the latent space. |
| accept_beta          | Acceptance ratio for the beta parameter.   |
| accept_theta         | Acceptance ratio for the theta parameter.  |
| accept_z             | Acceptance ratio for the z parameter.  |
| accept_w             | Acceptance ratio for the w parameter.  |
| sigma_estimate       | Posterior estimates of the standard deviation.   |
| sigma                | Posterior samples of the standard deviation.   |
| alpha_estimate       | Posterior estimates of the alpha parameter.  |
| alpha                | Posterior estimates of the alpha parameter.  |
| accept_alpha         | Acceptance ratio for the alpha parameter.  |

## Examples

```
# generate example (continuous) item response matrix
data <- matrix(rnorm(500, mean = 0, sd = 1), ncol=10, nrow=50)

lsrm_result <- lsirm2pl_normal_fixed_gamma(data)

# The code following can achieve the same result.
lsirm_result <- lsirm(data ~ lsirm2pl(spikenslab = FALSE, fixed_gamma = TRUE))
```

---

```
lsirm2pl_normal_fixed_gamma_mar
```

*2PL LSIRM fixing gamma to 1 with normal likelihood for missing at random data.*

---

## Description

[lsirm2pl\\_normal\\_fixed\\_gamma\\_mar](#) is used to fit 2PL LSIRM with gamma fixed to 1 for continuous variable in incomplete data assumed to be missing at random.

[lsirm2pl\\_normal\\_fixed\\_gamma\\_mar](#) factorizes item response matrix into column-wise item effect, row-wise respondent effect and further embeds interaction effect in a latent space, while considering the missing element under the assumption of missing at random. Unlike 1PL model, 2PL model assumes the item effect can vary according to respondent, allowing additional parameter multiplied with respondent effect. The resulting latent space provides an interaction map that represents interactions between respondents and items.

## Usage

```
lsirm2pl_normal_fixed_gamma_mar(
  data,
  ndim = 2,
  niter = 15000,
  nburn = 2500,
  nthin = 5,
  nprint = 500,
  jump_beta = 0.4,
  jump_theta = 1,
  jump_alpha = 1,
  jump_z = 0.5,
  jump_w = 0.5,
  pr_mean_beta = 0,
  pr_sd_beta = 1,
  pr_mean_theta = 0,
  pr_mean_alpha = 0.5,
  pr_sd_alpha = 1,
  pr_a_theta = 0.001,
  pr_b_theta = 0.001,
  pr_a_eps = 0.001,
  pr_b_eps = 0.001,
  missing.val = 99,
  verbose = FALSE
)
```

## Arguments

|      |   |
|------|---|
| data | Matrix; a binary or continuous item response matrix for analysis. Each row represents a respondent, and each column contains responses to the corresponding |
|------|---|

|               |  |
|---------------|--|
|               | item.  |
| ndim          | Integer; the dimension of the latent space. Default is 2.  |
| niter         | Integer; the total number of MCMC iterations to run. Default is 15000.                                 |
| nburn         | Integer; the number of initial MCMC iterations to discard as burn-in. Default is 2500.                 |
| nthin         | Integer; the number of MCMC iterations to thin. Default is 5.  |
| nprint        | Integer; the interval at which MCMC samples are displayed during execution. Default is 500.            |
| jump_beta     | Numeric; the jumping rule for the beta proposal density. Default is 0.4.                               |
| jump_theta    | Numeric; the jumping rule for the theta proposal density. Default is 1.0.                              |
| jump_alpha    | Numeric; the jumping rule for the alpha proposal density. Default is 1.0.                              |
| jump_z        | Numeric; the jumping rule for the z proposal density. Default is 0.5.                                  |
| jump_w        | Numeric; the jumping rule for the w proposal density. Default is 0.5.                                  |
| pr_mean_beta  | Numeric; the mean of the normal prior for beta. Default is 0.  |
| pr_sd_beta    | Numeric; the standard deviation of the normal prior for beta. Default is 1.0.                          |
| pr_mean_theta | Numeric; the mean of the normal prior for theta. Default is 0.   |
| pr_mean_alpha | Numeric; the mean of the log normal prior for alpha. Default is 0.5.                                   |
| pr_sd_alpha   | Numeric; the standard deviation of the log normal prior for alpha. Default is 1.0.                     |
| pr_a_theta    | Numeric; the shape parameter of the inverse gamma prior for the variance of theta. Default is 0.001.   |
| pr_b_theta    | Numeric; the scale parameter of the inverse gamma prior for the variance of theta. Default is 0.001.   |
| pr_a_eps      | Numeric; the shape parameter of inverse gamma prior for variance of data likelihood. Default is 0.001. |
| pr_b_eps      | Numeric; the scale parameter of inverse gamma prior for variance of data likelihood. Default is 0.001. |
| missing.val   | Numeric; a number to replace missing values. Default is 99.  |
| verbose       | Logical; If TRUE, MCMC samples are printed for each nprint. Default is FALSE.                          |

## Details

lsirm2pl\_normal\_fixed\_gamma\_mar models the continuous value of response by respondent  $j$  to item  $i$  with item effect  $\beta_i$ , respondent effect  $\theta_j$  and the distance between latent position  $w_i$  of item  $i$  and latent position  $z_j$  of respondent  $j$  in the shared metric space. For 2pl model, the item effect is assumed to have additional discrimination parameter  $\alpha_i$  multiplied by  $\theta_j$ :

$$Y_{j,i} = \theta_j + \beta_i - \gamma ||z_j - w_i|| + e_{j,i}$$

where the error  $e_{j,i} \sim N(0, \sigma^2)$ . Under the assumption of missing at random, the model takes the missing element into consideration in the sampling procedure. For the details of missing at random assumption and data augmentation, see References.

**Value**

`lsirm2pl_normal_fixed_gamma_mar` returns an object of list containing the following components:

|                                   |  |
|-----------------------------------|--|
| <code>data</code>                 | Data frame or matrix containing the variables in the model.  |
| <code>missing.val</code>          | A number to replace missing values.  |
| <code>bic</code>                  | Numeric value with the corresponding BIC.  |
| <code>mcmc_inf</code>             | Details about the number of MCMC iterations, burn-in periods, and thinning intervals.  |
| <code>map_inf</code>              | The log maximum a posteriori (MAP) value and the iteration number at which this MAP value occurs.  |
| <code>beta_estimate</code>        | Posterior estimates of the beta parameter.   |
| <code>theta_estimate</code>       | Posterior estimates of the theta parameter.  |
| <code>sigma_theta_estimate</code> | Posterior estimates of the standard deviation of theta.  |
| <code>z_estimate</code>           | Posterior estimates of the z parameter.  |
| <code>w_estimate</code>           | Posterior estimates of the w parameter.  |
| <code>imp_estimate</code>         | Probability of imputating a missing value with 1.  |
| <code>beta</code>                 | Posterior samples of the beta parameter.   |
| <code>theta</code>                | Posterior samples of the theta parameter.  |
| <code>theta_sd</code>             | Posterior samples of the standard deviation of theta.  |
| <code>z</code>                    | Posterior samples of the z parameter, represented as a 3-dimensional matrix where the last axis denotes the dimension of the latent space. |
| <code>w</code>                    | Posterior samples of the w parameter, represented as a 3-dimensional matrix where the last axis denotes the dimension of the latent space. |
| <code>imp</code>                  | Imputation for missing Values using posterior samples.   |
| <code>accept_beta</code>          | Acceptance ratio for the beta parameter.   |
| <code>accept_theta</code>         | Acceptance ratio for the theta parameter.  |
| <code>accept_z</code>             | Acceptance ratio for the z parameter.  |
| <code>accept_w</code>             | Acceptance ratio for the w parameter.  |
| <code>sigma_estimate</code>       | Posterior estimates of the standard deviation.   |
| <code>sigma</code>                | Posterior samples of the standard deviation.   |
| <code>alpha_estimate</code>       | Posterior estimates of the alpha parameter.  |
| <code>alpha</code>                | Posterior estimates of the alpha parameter.  |
| <code>accept_alpha</code>         | Acceptance ratio for the alpha parameter.  |



## Examples

```
# generate example (continuous) item response matrix
data      <- matrix(rnorm(500, mean = 0, sd = 1), ncol=10, nrow=50)

# generate example missing indicator matrix
missing_mat  <- matrix(rbinom(500, size = 1, prob = 0.2), ncol=10, nrow=50)

# make missing value with missing indicator matrix
data[missing_mat==1] <- 99

lsirm_result <- lsirm2pl_normal_fixed_gamma_mar(data)

# The code following can achieve the same result.
lsirm_result <- lsirm(data ~ lsirm2pl(spikenslab = FALSE, fixed_gamma = TRUE,
                                     missing_data = "mar"))
```

---

```
lsirm2pl_normal_fixed_gamma_mcar
```

*2PL LSIRM fixing gamma to 1 with normal likelihood for missing completely at random data.*

---

## Description

[lsirm2pl\\_normal\\_fixed\\_gamma\\_mcar](#) is used to fit 2PL LSIRM with gamma fixed to 1 for continuous variable in incomplete data assumed to be missing completely at random.

[lsirm2pl\\_normal\\_fixed\\_gamma\\_mcar](#) factorizes item response matrix into column-wise item effect, row-wise respondent effect and further embeds interaction effect in a latent space, while ignoring the missing element under the assumption of missing completely at random. Unlike 1PL model, 2PL model assumes the item effect can vary according to respondent, allowing additional parameter multiplied with respondent effect. The resulting latent space provides an interaction map that represents interactions between respondents and items.

## Usage

```
lsirm2pl_normal_fixed_gamma_mcar(
  data,
  ndim = 2,
  niter = 15000,
  nburn = 2500,
  nthin = 5,
  nprint = 500,
  jump_beta = 0.4,
  jump_theta = 1,
  jump_alpha = 1,
  jump_z = 0.5,
  jump_w = 0.5,
```

```

pr_mean_beta = 0,
pr_sd_beta = 1,
pr_mean_theta = 0,
pr_mean_alpha = 0.5,
pr_sd_alpha = 1,
pr_a_theta = 0.001,
pr_b_theta = 0.001,
pr_a_eps = 0.001,
pr_b_eps = 0.001,
missing.val = 99,
verbose = FALSE
)

```

### Arguments

|                            |   |
|----------------------------|---|
| <code>data</code>          | Matrix; a binary or continuous item response matrix for analysis. Each row represents a respondent, and each column contains responses to the corresponding item. |
| <code>ndim</code>          | Integer; the dimension of the latent space. Default is 2.   |
| <code>niter</code>         | Integer; the total number of MCMC iterations to run. Default is 15000.  |
| <code>nburn</code>         | Integer; the number of initial MCMC iterations to discard as burn-in. Default is 2500.  |
| <code>nthin</code>         | Integer; the number of MCMC iterations to thin. Default is 5.   |
| <code>nprint</code>        | Integer; the interval at which MCMC samples are displayed during execution. Default is 500.   |
| <code>jump_beta</code>     | Numeric; the jumping rule for the beta proposal density. Default is 0.4.  |
| <code>jump_theta</code>    | Numeric; the jumping rule for the theta proposal density. Default is 1.0.   |
| <code>jump_alpha</code>    | Numeric; the jumping rule for the alpha proposal density. Default is 1.0.   |
| <code>jump_z</code>        | Numeric; the jumping rule for the z proposal density. Default is 0.5.   |
| <code>jump_w</code>        | Numeric; the jumping rule for the w proposal density. Default is 0.5.   |
| <code>pr_mean_beta</code>  | Numeric; the mean of the normal prior for beta. Default is 0.   |
| <code>pr_sd_beta</code>    | Numeric; the standard deviation of the normal prior for beta. Default is 1.0.   |
| <code>pr_mean_theta</code> | Numeric; the mean of the normal prior for theta. Default is 0.  |
| <code>pr_mean_alpha</code> | Numeric; the mean of the log normal prior for alpha. Default is 0.5.  |
| <code>pr_sd_alpha</code>   | Numeric; the standard deviation of the log normal prior for alpha. Default is 1.0.  |
| <code>pr_a_theta</code>    | Numeric; the shape parameter of the inverse gamma prior for the variance of theta. Default is 0.001.  |
| <code>pr_b_theta</code>    | Numeric; the scale parameter of the inverse gamma prior for the variance of theta. Default is 0.001.  |
| <code>pr_a_eps</code>      | Numeric; the shape parameter of inverse gamma prior for variance of data likelihood. Default is 0.001.  |

|             |  |
|-------------|--|
| pr_b_eps    | Numeric; the scale parameter of inverse gamma prior for variance of data likelihood. Default is 0.001. |
| missing.val | Numeric; a number to replace missing values. Default is 99.  |
| verbose     | Logical; If TRUE, MCMC samples are printed for each nprint. Default is FALSE.                          |

## Details

lsirm2pl\_normal\_fixed\_gamma\_mcar models the continuous value of response by respondent  $j$  to item  $i$  with item effect  $\beta_i$ , respondent effect  $\theta_j$  and the distance between latent position  $w_i$  of item  $i$  and latent position  $z_j$  of respondent  $j$  in the shared metric space. For 2pl model, the item effect is assumed to have additional discrimination parameter  $\alpha_i$  multiplied by  $\theta_j$ :

$$Y_{j,i} = \theta_j + \beta_i - \gamma ||z_j - w_i|| + e_{j,i}$$

where the error  $e_{j,i} \sim N(0, \sigma^2)$ . Under the assumption of missing completely at random, the model ignores the missing element in doing inference. For the details of missing completely at random assumption and data augmentation, see References.

## Value

lsirm2pl\_normal\_fixed\_gamma\_mcar returns an object of list containing the following components:

|                      |  |
|----------------------|--|
| data                 | Data frame or matrix containing the variables in the model.  |
| missing.val          | A number to replace missing values.  |
| bic                  | Numeric value with the corresponding BIC.  |
| mcmc_inf             | Details about the number of MCMC iterations, burn-in periods, and thinning intervals.  |
| map_inf              | The log maximum a posteriori (MAP) value and the iteration number at which this MAP value occurs.  |
| beta_estimate        | Posterior estimates of the beta parameter.   |
| theta_estimate       | Posterior estimates of the theta parameter.  |
| sigma_theta_estimate | Posterior estimates of the standard deviation of theta.  |
| z_estimate           | Posterior estimates of the z parameter.  |
| w_estimate           | Posterior estimates of the w parameter.  |
| beta                 | Posterior samples of the beta parameter.   |
| theta                | Posterior samples of the theta parameter.  |
| theta_sd             | Posterior samples of the standard deviation of theta.  |
| z                    | Posterior samples of the z parameter, represented as a 3-dimensional matrix where the last axis denotes the dimension of the latent space. |
| w                    | Posterior samples of the w parameter, represented as a 3-dimensional matrix where the last axis denotes the dimension of the latent space. |
| accept_beta          | Acceptance ratio for the beta parameter.   |

accept\_theta    Acceptance ratio for the theta parameter.  
 accept\_z        Acceptance ratio for the z parameter.  
 accept\_w        Acceptance ratio for the w parameter.  
 sigma\_estimate   Posterior estimates of the standard deviation.  
 sigma           Posterior samples of the standard deviation.  
 alpha\_estimate   Posterior estimates of the alpha parameter.  
 alpha            Posterior estimates of the alpha parameter.  
 accept\_alpha    Acceptance ratio for the alpha parameter.

### Examples

```

# generate example (continuous) item response matrix
data      <- matrix(rnorm(500, mean = 0, sd = 1),ncol=10,nrow=50)

# generate example missing indicator matrix
missing_mat  <- matrix(rbinom(500, size = 1, prob = 0.2),ncol=10,nrow=50)

# make missing value with missing indicator matrix
data[missing_mat==1] <- 99

lsirm_result <- lsirm2pl_normal_fixed_gamma_mcar(data)

# The code following can achieve the same result.
lsirm_result <- lsirm(data ~ lsirm2pl(spikenslab = FALSE, fixed_gamma = TRUE,
                                     missing_data = "mcar"))
  
```

---

|                     |  |
|---------------------|--|
| lsirm2pl_normal_mar | 2PL LSIRM with normal likelihood and missing at random data. |
|---------------------|--|

---

### Description

[lsirm2pl\\_normal\\_mar](#) is used to fit 2PL LSIRM for continuous variable in incomplete data assumed to be missing at random. [lsirm2pl\\_normal\\_mar](#) factorizes item response matrix into column-wise item effect, row-wise respondent effect and further embeds interaction effect in a latent space, while considering the missing element under the assumption of missing at random. Unlike IPL model, 2PL model assumes the item effect can vary according to respondent, allowing additional parameter multiplied with respondent effect. The resulting latent space provides an interaction map that represents interactions between respondents and items.

### Usage

```

lsirm2pl_normal_mar(
  data,
  ndim = 2,
  niter = 15000,

```

```

nburn = 2500,
nthin = 5,
nprint = 500,
jump_beta = 0.4,
jump_theta = 1,
jump_alpha = 1,
jump_gamma = 1,
jump_z = 0.5,
jump_w = 0.5,
pr_mean_beta = 0,
pr_sd_beta = 1,
pr_mean_theta = 0,
pr_mean_gamma = 0.5,
pr_sd_gamma = 1,
pr_mean_alpha = 0.5,
pr_sd_alpha = 1,
pr_a_theta = 0.001,
pr_b_theta = 0.001,
pr_a_eps = 0.001,
pr_b_eps = 0.001,
missing.val = 99,
verbose = FALSE
)

```

### Arguments

|               |   |
|---------------|---|
| data          | Matrix; a binary or continuous item response matrix for analysis. Each row represents a respondent, and each column contains responses to the corresponding item. |
| ndim          | Integer; the dimension of the latent space. Default is 2.   |
| niter         | Integer; the total number of MCMC iterations to run. Default is 15000.  |
| nburn         | Integer; the number of initial MCMC iterations to discard as burn-in. Default is 2500.  |
| nthin         | Integer; the number of MCMC iterations to thin. Default is 5.   |
| nprint        | Integer; the interval at which MCMC samples are displayed during execution. Default is 500.   |
| jump_beta     | Numeric; the jumping rule for the beta proposal density. Default is 0.4.  |
| jump_theta    | Numeric; the jumping rule for the theta proposal density. Default is 1.0.   |
| jump_alpha    | Numeric; the jumping rule for the alpha proposal density. Default is 1.0.   |
| jump_gamma    | Numeric; the jumping rule for the gamma proposal density. Default is 0.025  |
| jump_z        | Numeric; the jumping rule for the z proposal density. Default is 0.5.   |
| jump_w        | Numeric; the jumping rule for the w proposal density. Default is 0.5.   |
| pr_mean_beta  | Numeric; the mean of the normal prior for beta. Default is 0.   |
| pr_sd_beta    | Numeric; the standard deviation of the normal prior for beta. Default is 1.0.   |
| pr_mean_theta | Numeric; the mean of the normal prior for theta. Default is 0.  |

|               |  |
|---------------|--|
| pr_mean_gamma | Numeric; mean of log normal prior for gamma. Default is 0.5.   |
| pr_sd_gamma   | Numeric; standard deviation of log normal prior for gamma. Default is 1.0.                             |
| pr_mean_alpha | Numeric; the mean of the log normal prior for alpha. Default is 0.5.                                   |
| pr_sd_alpha   | Numeric; the standard deviation of the log normal prior for alpha. Default is 1.0.                     |
| pr_a_theta    | Numeric; the shape parameter of the inverse gamma prior for the variance of theta. Default is 0.001.   |
| pr_b_theta    | Numeric; the scale parameter of the inverse gamma prior for the variance of theta. Default is 0.001.   |
| pr_a_eps      | Numeric; the shape parameter of inverse gamma prior for variance of data likelihood. Default is 0.001. |
| pr_b_eps      | Numeric; the scale parameter of inverse gamma prior for variance of data likelihood. Default is 0.001. |
| missing.val   | Numeric; a number to replace missing values. Default is 99.  |
| verbose       | Logical; If TRUE, MCMC samples are printed for each nprint. Default is FALSE.                          |

### Details

lsirm2pl\_normal\_mar models the continuous value of response by respondent  $j$  to item  $i$  with item effect  $\beta_i$ , respondent effect  $\theta_j$  and the distance between latent position  $w_i$  of item  $i$  and latent position  $z_j$  of respondent  $j$  in the shared metric space, with  $\gamma$  represents the weight of the distance term. For 2pl model, the item effect is assumed to have additional discrimination parameter  $\alpha_i$  multiplied by  $\theta_j$ :

$$Y_{j,i} = \theta_j + \beta_i - \gamma ||z_j - w_i|| + e_{j,i}$$

where the error  $e_{j,i} \sim N(0, \sigma^2)$  Under the assumption of missing at random, the model takes the missing element into consideration in the sampling procedure. For the details of missing at random assumption and data augmentation, see References.

### Value

lsirm2pl\_normal\_mar returns an object of list containing the following components:

|                      |   |
|----------------------|---|
| data                 | Data frame or matrix containing the variables in the model.                                       |
| missing.val          | A number to replace missing values.   |
| bic                  | Numeric value with the corresponding BIC.   |
| mcmc_inf             | Details about the number of MCMC iterations, burn-in periods, and thinning intervals.             |
| map_inf              | The log maximum a posteriori (MAP) value and the iteration number at which this MAP value occurs. |
| beta_estimate        | Posterior estimates of the beta parameter.  |
| theta_estimate       | Posterior estimates of the theta parameter.   |
| sigma_theta_estimate | Posterior estimates of the standard deviation of theta.   |



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lsirm2pl\_normal\_mar\_ss

*2pl LSIRM with normal likelihood and model selection approach for missing at random data.*

---

## Description

[lsirm2pl\\_normal\\_mar\\_ss](#) is used to fit 2pl LSIRM with model selection approach based on spike-and-slab priors for continuous variable in incomplete data assumed to be missing at random. [lsirm2pl\\_normal\\_mar\\_ss](#) factorizes item response matrix into column-wise item effect, row-wise respondent effect and further embeds interaction effect in a latent space, while considering the missing element under the assumption of missing at random. Unlike 1pl model, 2pl model assumes the item effect can vary according to respondent, allowing additional parameter multiplied with respondent effect. The resulting latent space provides an interaction map that represents interactions between respondents and items.

## Usage

```
lsirm2pl_normal_mar_ss(
  data,
  ndim = 2,
  niter = 15000,
  nburn = 2500,
  nthin = 5,
  nprint = 500,
  jump_beta = 0.4,
  jump_theta = 1,
  jump_alpha = 1,
  jump_gamma = 1,
  jump_z = 0.5,
  jump_w = 0.5,
  pr_mean_beta = 0,
  pr_sd_beta = 1,
  pr_mean_theta = 0,
  pr_spike_mean = -3,
  pr_spike_sd = 1,
  pr_slab_mean = 0.5,
  pr_slab_sd = 1,
  pr_mean_alpha = 0.5,
  pr_sd_alpha = 1,
  pr_a_eps = 0.001,
  pr_b_eps = 0.001,
  pr_a_theta = 0.001,
  pr_b_theta = 0.001,
  pr_xi_a = 0.001,
  pr_xi_b = 0.001,
  missing.val = 99,
```



```

    verbose = FALSE
)

```

### Arguments

|               |   |
|---------------|---|
| data          | Matrix; a binary or continuous item response matrix for analysis. Each row represents a respondent, and each column contains responses to the corresponding item. |
| ndim          | Integer; the dimension of the latent space. Default is 2.   |
| niter         | Integer; the total number of MCMC iterations to run. Default is 15000.  |
| nburn         | Integer; the number of initial MCMC iterations to discard as burn-in. Default is 2500.  |
| nthin         | Integer; the number of MCMC iterations to thin. Default is 5.   |
| nprint        | Integer; the interval at which MCMC samples are displayed during execution. Default is 500.   |
| jump_beta     | Numeric; the jumping rule for the beta proposal density. Default is 0.4.  |
| jump_theta    | Numeric; the jumping rule for the theta proposal density. Default is 1.0.   |
| jump_alpha    | Numeric; the jumping rule for the alpha proposal density. Default is 1.0.   |
| jump_gamma    | Numeric; the jumping rule for the gamma proposal density. Default is 1.0.   |
| jump_z        | Numeric; the jumping rule for the z proposal density. Default is 0.5.   |
| jump_w        | Numeric; the jumping rule for the w proposal density. Default is 0.5.   |
| pr_mean_beta  | Numeric; the mean of the normal prior for beta. Default is 0.   |
| pr_sd_beta    | Numeric; the standard deviation of the normal prior for beta. Default is 1.0.   |
| pr_mean_theta | Numeric; the mean of the normal prior for theta. Default is 0.  |
| pr_spike_mean | Numeric; the mean of spike prior for log gamma. Default is -3.  |
| pr_spike_sd   | Numeric; the standard deviation of spike prior for log gamma. Default is 1.   |
| pr_slab_mean  | Numeric; the mean of spike prior for log gamma. Default is 0.5.   |
| pr_slab_sd    | Numeric; the standard deviation of spike prior for log gamma. Default is 1.   |
| pr_mean_alpha | Numeric; the mean of the log normal prior for alpha. Default is 0.5.  |
| pr_sd_alpha   | Numeric; the standard deviation of the log normal prior for alpha. Default is 1.0.  |
| pr_a_eps      | Numeric; the shape parameter of inverse gamma prior for variance of data likelihood. Default is 0.001.  |
| pr_b_eps      | Numeric; the scale parameter of inverse gamma prior for variance of data likelihood. Default is 0.001.  |
| pr_a_theta    | Numeric; the shape parameter of the inverse gamma prior for the variance of theta. Default is 0.001.  |
| pr_b_theta    | Numeric; the scale parameter of the inverse gamma prior for the variance of theta. Default is 0.001.  |
| pr_xi_a       | Numeric; the first shape parameter of beta prior for latent variable xi. Default is 1.  |

|             |   |
|-------------|---|
| pr_xi_b     | Numeric; the second shape parameter of beta prior for latent variable xi. Default is 1. |
| missing.val | Numeric; a number to replace missing values. Default is 99.                             |
| verbose     | Logical; If TRUE, MCMC samples are printed for each nprint. Default is FALSE.           |

### Details

lsirm2pl\_normal\_mar\_ss models the continuous value of response by respondent  $j$  to item  $i$  with item effect  $\beta_i$ , respondent effect  $\theta_j$  and the distance between latent position  $w_i$  of item  $i$  and latent position  $z_j$  of respondent  $j$  in the shared metric space, with  $\gamma$  represents the weight of the distance term. For 2pl model, the item effect is assumed to have additional discrimination parameter  $\alpha_i$  multiplied by  $\theta_j$ :

$$Y_{j,i} = \theta_j + \beta_i - \gamma ||z_j - w_i|| + e_{j,i}$$

where the error  $e_{j,i} \sim N(0, \sigma^2)$ . Under the assumption of missing at random, the model takes the missing element into consideration in the sampling procedure. For the details of missing at random assumption and data augmentation, see References. lsirm2pl\_normal\_mcar\_ss model include model selection approach based on spike-and-slab priors for log gamma. For detail of spike-and-slab priors, see References.

### Value

lsirm2pl\_normal\_mar\_ss returns an object of list containing the following components:

|                      |  |
|----------------------|--|
| data                 | Data frame or matrix containing the variables in the model.  |
| missing.val          | A number to replace missing values.  |
| bic                  | Numeric value with the corresponding BIC.  |
| mcmc_inf             | Details about the number of MCMC iterations, burn-in periods, and thinning intervals.  |
| map_inf              | The log maximum a posteriori (MAP) value and the iteration number at which this MAP value occurs.  |
| beta_estimate        | Posterior estimates of the beta parameter.   |
| theta_estimate       | Posterior estimates of the theta parameter.  |
| sigma_theta_estimate | Posterior estimates of the standard deviation of theta.  |
| gamma_estimate       | posterior estimates of gamma parameter.  |
| z_estimate           | Posterior estimates of the z parameter.  |
| w_estimate           | Posterior estimates of the w parameter.  |
| beta                 | Posterior samples of the beta parameter.   |
| theta                | Posterior samples of the theta parameter.  |
| gamma                | Posterior samples of the gamma parameter.  |
| theta_sd             | Posterior samples of the standard deviation of theta.  |
| z                    | Posterior samples of the z parameter, represented as a 3-dimensional matrix where the last axis denotes the dimension of the latent space. |



---

|                      |  |
|----------------------|--|
| lsirm2pl_normal_mcar | <i>2PL LSIRM with normal likelihood and missing completely at random data.</i> |
|----------------------|--|

---

## Description

[lsirm2pl\\_normal\\_mcar](#) is used to fit 2PL LSIRM for continuous variable in incomplete data assumed to be missing completely at random. [lsirm2pl\\_normal\\_mcar](#) factorizes item response matrix into column-wise item effect, row-wise respondent effect and further embeds interaction effect in a latent space, while ignoring the missing element under the assumption of missing completely at random. Unlike 1PL model, 2PL model assumes the item effect can vary according to respondent, allowing additional parameter multiplied with respondent effect. The resulting latent space provides an interaction map that represents interactions between respondents and items.

## Usage

```
lsirm2pl_normal_mcar(
  data,
  ndim = 2,
  niter = 15000,
  nburn = 2500,
  nthin = 5,
  nprint = 500,
  jump_beta = 0.4,
  jump_theta = 1,
  jump_alpha = 1,
  jump_gamma = 1,
  jump_z = 0.5,
  jump_w = 0.5,
  pr_mean_beta = 0,
  pr_sd_beta = 1,
  pr_mean_theta = 0,
  pr_mean_gamma = 0.5,
  pr_sd_gamma = 1,
  pr_mean_alpha = 0.5,
  pr_sd_alpha = 1,
  pr_a_theta = 0.001,
  pr_b_theta = 0.001,
  pr_a_eps = 0.001,
  pr_b_eps = 0.001,
  missing.val = 99,
  verbose = FALSE
)
```

## Arguments

|      |   |
|------|---|
| data | Matrix; a binary or continuous item response matrix for analysis. Each row represents a respondent, and each column contains responses to the corresponding |
|------|---|

|               |  |
|---------------|--|
|               | item.  |
| ndim          | Integer; the dimension of the latent space. Default is 2.  |
| niter         | Integer; the total number of MCMC iterations to run. Default is 15000.                                 |
| nburn         | Integer; the number of initial MCMC iterations to discard as burn-in. Default is 2500.                 |
| nthin         | Integer; the number of MCMC iterations to thin. Default is 5.  |
| nprint        | Integer; the interval at which MCMC samples are displayed during execution. Default is 500.            |
| jump_beta     | Numeric; the jumping rule for the beta proposal density. Default is 0.4.                               |
| jump_theta    | Numeric; the jumping rule for the theta proposal density. Default is 1.0.                              |
| jump_alpha    | Numeric; the jumping rule for the alpha proposal density. Default is 1.0.                              |
| jump_gamma    | Numeric; the jumping rule for the gamma proposal density. Default is 0.025                             |
| jump_z        | Numeric; the jumping rule for the z proposal density. Default is 0.5.                                  |
| jump_w        | Numeric; the jumping rule for the w proposal density. Default is 0.5.                                  |
| pr_mean_beta  | Numeric; the mean of the normal prior for beta. Default is 0.  |
| pr_sd_beta    | Numeric; the standard deviation of the normal prior for beta. Default is 1.0.                          |
| pr_mean_theta | Numeric; the mean of the normal prior for theta. Default is 0.   |
| pr_mean_gamma | Numeric; mean of log normal prior for gamma. Default is 0.5.   |
| pr_sd_gamma   | Numeric; standard deviation of log normal prior for gamma. Default is 1.0.                             |
| pr_mean_alpha | Numeric; the mean of the log normal prior for alpha. Default is 0.5.                                   |
| pr_sd_alpha   | Numeric; the standard deviation of the log normal prior for alpha. Default is 1.0.                     |
| pr_a_theta    | Numeric; the shape parameter of the inverse gamma prior for the variance of theta. Default is 0.001.   |
| pr_b_theta    | Numeric; the scale parameter of the inverse gamma prior for the variance of theta. Default is 0.001.   |
| pr_a_eps      | Numeric; the shape parameter of inverse gamma prior for variance of data likelihood. Default is 0.001. |
| pr_b_eps      | Numeric; the scale parameter of inverse gamma prior for variance of data likelihood. Default is 0.001. |
| missing.val   | Numeric; a number to replace missing values. Default is 99.  |
| verbose       | Logical; If TRUE, MCMC samples are printed for each nprint. Default is FALSE.                          |

## Details

lsirm2pl\_normal\_mcar models the continuous value of response by respondent  $j$  to item  $i$  with item effect  $\beta_i$ , respondent effect  $\theta_j$  and the distance between latent position  $w_i$  of item  $i$  and latent position  $z_j$  of respondent  $j$  in the shared metric space, with  $\gamma$  represents the weight of the distance term. For 2pl model, the item effect is assumed to have additional discrimination parameter  $\alpha_i$  multiplied by  $\theta_j$ :

$$Y_{j,i} = \theta_j + \beta_i - \gamma ||z_j - w_i|| + e_{j,i}$$

where the error  $e_{j,i} \sim N(0, \sigma^2)$ . Under the assumption of missing completely at random, the model ignores the missing element in doing inference. For the details of missing completely at random assumption and data augmentation, see References.

### Value

lsirm2pl\_normal\_mcar returns an object of list containing the following components:

|                      |  |
|----------------------|--|
| data                 | A data frame or matrix containing the variables used in the model.   |
| missing.val          | A number to replace missing values.  |
| bic                  | Numeric value with the corresponding BIC.  |
| mcmc_inf             | Details about the number of MCMC iterations, burn-in periods, and thinning intervals.  |
| map_inf              | The log maximum a posteriori (MAP) value and the iteration number at which this MAP value occurs.  |
| beta_estimate        | Posterior estimates of the beta parameter.   |
| theta_estimate       | Posterior estimates of the theta parameter.  |
| sigma_theta_estimate | Posterior estimates of the standard deviation of theta.  |
| gamma_estimate       | Posterior estimates of gamma parameter.  |
| z_estimate           | Posterior estimates of the z parameter.  |
| w_estimate           | Posterior estimates of the w parameter.  |
| beta                 | Posterior samples of the beta parameter.   |
| theta                | Posterior samples of the theta parameter.  |
| theta_sd             | Posterior samples of the standard deviation of theta.  |
| gamma                | Posterior samples of the gamma parameter.  |
| z                    | Posterior samples of the z parameter, represented as a 3-dimensional matrix where the last axis denotes the dimension of the latent space. |
| w                    | Posterior samples of the w parameter, represented as a 3-dimensional matrix where the last axis denotes the dimension of the latent space. |
| accept_beta          | Acceptance ratio for the beta parameter.   |
| accept_theta         | Acceptance ratio for the theta parameter.  |
| accept_z             | Acceptance ratio for the z parameter.  |
| accept_w             | Acceptance ratio for the w parameter.  |
| accept_gamma         | Acceptance ratio for the gamma parameter.  |
| sigma_estimate       | Posterior estimates of the standard deviation.   |
| sigma                | Posterior samples of the standard deviation.   |
| alpha_estimate       | Posterior estimates of the alpha parameter.  |
| alpha                | Posterior estimates of the alpha parameter.  |
| accept_alpha         | Acceptance ratio for the alpha parameter.  |

## References

Little, R. J., & Rubin, D. B. (2019). Statistical analysis with missing data (Vol. 793). John Wiley & Sons.

## Examples

```
# generate example (continuous) item response matrix
data      <- matrix(rnorm(500, mean = 0, sd = 1), ncol=10, nrow=50)

# generate example missing indicator matrix
missing_mat <- matrix(rbinom(500, size = 1, prob = 0.2), ncol=10, nrow=50)

# make missing value with missing indicator matrix
data[missing_mat==1] <- 99

lsirm_result <- lsirm2pl_normal_mcar(data)

# The code following can achieve the same result.
lsirm_result <- lsirm(data ~ lsirm2pl(spikenslab = FALSE, fixed_gamma = FALSE,
                                     missing_data = "mcar"))
```

---

```
lsirm2pl_normal_mcar_ss
```

*2PL LSIRM with normal likelihood and model selection approach for missing completely at random data.*

---

## Description

[lsirm2pl\\_normal\\_mcar\\_ss](#) is used to fit 2PL LSIRM with model selection approach based on spike-and-slab priors for continuous variable in incomplete data assumed to be missing completely at random. [lsirm2pl\\_normal\\_mcar\\_ss](#) factorizes item response matrix into column-wise item effect, row-wise respondent effect and further embeds interaction effect in a latent space, while ignoring the missing element under the assumption of missing completely at random. Unlike 1PL model, 2PL model assumes the item effect can vary according to respondent, allowing additional parameter multiplied with respondent effect. The resulting latent space provides an interaction map that represents interactions between respondents and items.

## Usage

```
lsirm2pl_normal_mcar_ss(
  data,
  ndim = 2,
  niter = 15000,
  nburn = 2500,
  nthin = 5,
  nprint = 500,
  jump_beta = 0.4,
```

```

jump_theta = 1,
jump_alpha = 1,
jump_gamma = 1,
jump_z = 0.5,
jump_w = 0.5,
pr_mean_beta = 0,
pr_sd_beta = 1,
pr_mean_theta = 0,
pr_spike_mean = -3,
pr_spike_sd = 1,
pr_slab_mean = 0.5,
pr_slab_sd = 1,
pr_mean_alpha = 0.5,
pr_sd_alpha = 1,
pr_a_eps = 0.001,
pr_b_eps = 0.001,
pr_a_theta = 0.001,
pr_b_theta = 0.001,
pr_xi_a = 0.001,
pr_xi_b = 0.001,
missing.val = 99,
verbose = FALSE
)

```

### Arguments

|               |   |
|---------------|---|
| data          | Matrix; a binary or continuous item response matrix for analysis. Each row represents a respondent, and each column contains responses to the corresponding item. |
| ndim          | Integer; the dimension of the latent space. Default is 2.   |
| niter         | Integer; the total number of MCMC iterations to run. Default is 15000.  |
| nburn         | Integer; the number of initial MCMC iterations to discard as burn-in. Default is 2500.  |
| nthin         | Integer; the number of MCMC iterations to thin. Default is 5.   |
| nprint        | Integer; the interval at which MCMC samples are displayed during execution. Default is 500.   |
| jump_beta     | Numeric; the jumping rule for the beta proposal density. Default is 0.4.  |
| jump_theta    | Numeric; the jumping rule for the theta proposal density. Default is 1.0.   |
| jump_alpha    | Numeric; the jumping rule for the alpha proposal density. Default is 1.0.   |
| jump_gamma    | Numeric; the jumping rule for the gamma proposal density. Default is 1.0.   |
| jump_z        | Numeric; the jumping rule for the z proposal density. Default is 0.5.   |
| jump_w        | Numeric; the jumping rule for the w proposal density. Default is 0.5.   |
| pr_mean_beta  | Numeric; the mean of the normal prior for beta. Default is 0.   |
| pr_sd_beta    | Numeric; the standard deviation of the normal prior for beta. Default is 1.0.   |
| pr_mean_theta | Numeric; the mean of the normal prior for theta. Default is 0.  |



|               |  |
|---------------|--|
| pr_spike_mean | Numeric; the mean of spike prior for log gamma. Default is -3.   |
| pr_spike_sd   | Numeric; the standard deviation of spike prior for log gamma. Default is 1.                            |
| pr_slab_mean  | Numeric; the mean of spike prior for log gamma. Default is 0.5.  |
| pr_slab_sd    | Numeric; the standard deviation of spike prior for log gamma. Default is 1.                            |
| pr_mean_alpha | Numeric; the mean of the log normal prior for alpha. Default is 0.5.                                   |
| pr_sd_alpha   | Numeric; the standard deviation of the log normal prior for alpha. Default is 1.0.                     |
| pr_a_eps      | Numeric; the shape parameter of inverse gamma prior for variance of data likelihood. Default is 0.001. |
| pr_b_eps      | Numeric; the scale parameter of inverse gamma prior for variance of data likelihood. Default is 0.001. |
| pr_a_theta    | Numeric; the shape parameter of the inverse gamma prior for the variance of theta. Default is 0.001.   |
| pr_b_theta    | Numeric; the scale parameter of the inverse gamma prior for the variance of theta. Default is 0.001.   |
| pr_xi_a       | Numeric; the first shape parameter of beta prior for latent variable xi. Default is 1.                 |
| pr_xi_b       | Numeric; the second shape parameter of beta prior for latent variable xi. Default is 1.                |
| missing.val   | Numeric; a number to replace missing values. Default is 99.  |
| verbose       | Logical; If TRUE, MCMC samples are printed for each nprint. Default is FALSE.                          |

## Details

lsirm2pl\_normal\_mcar\_ss models the continuous value of response by respondent  $j$  to item  $i$  with item effect  $\beta_i$ , respondent effect  $\theta_j$  and the distance between latent position  $w_i$  of item  $i$  and latent position  $z_j$  of respondent  $j$  in the shared metric space, with  $\gamma$  represents the weight of the distance term. For 2pl model, the item effect is assumed to have additional discrimination parameter  $\alpha_i$  multiplied by  $\theta_j$ :

$$Y_{j,i} = \theta_j + \beta_i - \gamma ||z_j - w_i|| + e_{j,i}$$

where the error  $e_{j,i} \sim N(0, \sigma^2)$ . Under the assumption of missing completely at random, the model ignores the missing element in doing inference. For the details of missing completely at random assumption and data augmentation, see References. lsirm2pl\_normal\_mcar\_ss model include model selection approach based on spike-and-slab priors for log gamma. For detail of spike-and-slab priors, see References.

## Value

lsirm2pl\_normal\_mcar\_ss returns an object of list containing the following components:

|             |   |
|-------------|---|
| data        | Data frame or matrix containing the variables in the model. |
| missing.val | A number to replace missing values.                         |
| bic         | Numeric value with the corresponding BIC.                   |

|                      |  |
|----------------------|--|
| mcmc_inf             | Details about the number of MCMC iterations, burn-in periods, and thinning intervals.  |
| map_inf              | The log maximum a posteriori (MAP) value and the iteration number at which this MAP value occurs.  |
| beta_estimate        | Posterior estimates of the beta parameter.   |
| theta_estimate       | Posterior estimates of the theta parameter.  |
| sigma_theta_estimate | Posterior estimates of the standard deviation of theta.  |
| gamma_estimate       | posterior estimates of gamma parameter.  |
| z_estimate           | Posterior estimates of the z parameter.  |
| w_estimate           | Posterior estimates of the w parameter.  |
| beta                 | Posterior samples of the beta parameter.   |
| theta                | Posterior samples of the theta parameter.  |
| gamma                | Posterior samples of the gamma parameter.  |
| theta_sd             | Posterior samples of the standard deviation of theta.  |
| z                    | Posterior samples of the z parameter, represented as a 3-dimensional matrix where the last axis denotes the dimension of the latent space.             |
| w                    | Posterior samples of the w parameter, represented as a 3-dimensional matrix where the last axis denotes the dimension of the latent space.             |
| pi                   | Posterior samples of phi which is indicator of spike and slab prior. If phi is 1, log gamma follows the slab prior, otherwise follows the spike prior. |
| accept_beta          | Acceptance ratio for the beta parameter.   |
| accept_theta         | Acceptance ratio for the theta parameter.  |
| accept_z             | Acceptance ratio for the z parameter.  |
| accept_w             | Acceptance ratio for the w parameter.  |
| accept_gamma         | Acceptance ratio for the gamma parameter.  |
| sigma_estimate       | Posterior estimates of the standard deviation.   |
| sigma                | Posterior samples of the standard deviation.   |
| alpha_estimate       | Posterior estimates of the alpha parameter.  |
| alpha                | Posterior estimates of the alpha parameter.  |
| accept_alpha         | Acceptance ratio for the alpha parameter.  |

## References

Little, R. J., & Rubin, D. B. (2019). Statistical analysis with missing data (Vol. 793). John Wiley & Sons. Ishwaran, H., & Rao, J. S. (2005). Spike and slab variable selection: Frequentist and Bayesian strategies. *The Annals of Statistics*, 33(2), 730-773.

### Examples

```
# generate example (continuous) item response matrix
data      <- matrix(rnorm(500, mean = 0, sd = 1),ncol=10,nrow=50)

# generate example missing indicator matrix
missing_mat  <- matrix(rbinom(500, size = 1, prob = 0.2),ncol=10,nrow=50)

# make missing value with missing indicator matrix
data[missing_mat==1] <- 99

lsirm_result <- lsirm2pl_normal_mcar_ss(data)

# The code following can achieve the same result.
lsirm_result <- lsirm(data ~ lsirm2pl(spikenslab = TRUE, fixed_gamma = FALSE,
                                     missing_data = "mcar"))
```

---

|                   |   |
|-------------------|---|
| lsirm2pl_normal_o | <i>2PL LSIRM with normal likelihood</i> |
|-------------------|---|

---

### Description

[lsirm2pl\\_normal\\_o](#) is used to fit 2PL LSIRM for continuous variable. [lsirm2pl\\_normal\\_o](#) factorizes item response matrix into column-wise item effect, row-wise respondent effect and further embeds interaction effect in a latent space. Unlike 1PL model, 2PL model assumes the item effect can vary according to respondent, allowing additional parameter multiplied with respondent effect. The resulting latent space provides an interaction map that represents interactions between respondents and items.

### Usage

```
lsirm2pl_normal_o(
  data,
  ndim = 2,
  niter = 15000,
  nburn = 2500,
  nthin = 5,
  nprint = 500,
  jump_beta = 0.4,
  jump_theta = 1,
  jump_alpha = 1,
  jump_gamma = 0.025,
  jump_z = 0.5,
  jump_w = 0.5,
  pr_mean_beta = 0,
  pr_sd_beta = 1,
  pr_mean_theta = 0,
  pr_mean_gamma = 0.5,
```

```

pr_sd_gamma = 1,
pr_mean_alpha = 0.5,
pr_sd_alpha = 1,
pr_a_theta = 0.001,
pr_b_theta = 0.001,
pr_a_eps = 0.001,
pr_b_eps = 0.001,
verbose = FALSE
)

```

### Arguments

|               |   |
|---------------|---|
| data          | Matrix; a binary or continuous item response matrix for analysis. Each row represents a respondent, and each column contains responses to the corresponding item. |
| ndim          | Integer; the dimension of the latent space. Default is 2.   |
| niter         | Integer; the total number of MCMC iterations to run. Default is 15000.  |
| nburn         | Integer; the number of initial MCMC iterations to discard as burn-in. Default is 2500.  |
| nthin         | Integer; the number of MCMC iterations to thin. Default is 5.   |
| nprint        | Integer; the interval at which MCMC samples are displayed during execution. Default is 500.   |
| jump_beta     | Numeric; the jumping rule for the beta proposal density. Default is 0.4.  |
| jump_theta    | Numeric; the jumping rule for the theta proposal density. Default is 1.0.   |
| jump_alpha    | Numeric; the jumping rule for the alpha proposal density. Default is 1.0.   |
| jump_gamma    | Numeric; the jumping rule for the gamma proposal density. Default is 0.025  |
| jump_z        | Numeric; the jumping rule for the z proposal density. Default is 0.5.   |
| jump_w        | Numeric; the jumping rule for the w proposal density. Default is 0.5.   |
| pr_mean_beta  | Numeric; the mean of the normal prior for beta. Default is 0.   |
| pr_sd_beta    | Numeric; the standard deviation of the normal prior for beta. Default is 1.0.   |
| pr_mean_theta | Numeric; the mean of the normal prior for theta. Default is 0.  |
| pr_mean_gamma | Numeric; mean of log normal prior for gamma. Default is 0.5.  |
| pr_sd_gamma   | Numeric; standard deviation of log normal prior for gamma. Default is 1.0.  |
| pr_mean_alpha | Numeric; the mean of the log normal prior for alpha. Default is 0.5.  |
| pr_sd_alpha   | Numeric; the standard deviation of the log normal prior for alpha. Default is 1.0.  |
| pr_a_theta    | Numeric; the shape parameter of the inverse gamma prior for the variance of theta. Default is 0.001.  |
| pr_b_theta    | Numeric; the scale parameter of the inverse gamma prior for the variance of theta. Default is 0.001.  |
| pr_a_eps      | Numeric; the shape parameter of inverse gamma prior for variance of data likelihood. Default is 0.001.  |

|          |  |
|----------|--|
| pr_b_eps | Numeric; the scale parameter of inverse gamma prior for variance of data likelihood. Default is 0.001. |
| verbose  | Logical; If TRUE, MCMC samples are printed for each nprint. Default is FALSE.                          |

### Details

lsirm2pl\_normal\_o models the continuous value of response by respondent  $j$  to item  $i$  with item effect  $\beta_i$ , respondent effect  $\theta_j$  and the distance between latent position  $w_i$  of item  $i$  and latent position  $z_j$  of respondent  $j$  in the shared metric space, with  $\gamma$  represents the weight of the distance term. For 2pl model, the the item effect is assumed to have additional discrimination parameter  $\alpha_i$  multiplied by  $\theta_j$ :

$$Y_{j,i} = \theta_j + \beta_i - \gamma ||z_j - w_i|| + e_{j,i}$$

where the error  $e_{j,i} \sim N(0, \sigma^2)$

### Value

lsirm2pl\_normal\_o returns an object of list containing the following components:

|                      |  |
|----------------------|--|
| data                 | Data frame or matrix containing the variables used in the model.   |
| bic                  | A numeric value representing the Bayesian Information Criterion (BIC).   |
| mcmc_inf             | Details about the number of MCMC iterations, burn-in periods, and thinning intervals.  |
| map_inf              | The log maximum a posteriori (MAP) value and the iteration number at which this MAP value occurs.  |
| beta_estimate        | Posterior estimates of the beta parameter.   |
| theta_estimate       | Posterior estimates of the theta parameter.  |
| sigma_theta_estimate | Posterior estimates of the standard deviation of theta.  |
| gamma_estimate       | Posterior estimates of gamma parameter.  |
| z_estimate           | Posterior estimates of the z parameter.  |
| w_estimate           | Posterior estimates of the w parameter.  |
| beta                 | Posterior samples of the beta parameter.   |
| theta                | Posterior samples of the theta parameter.  |
| theta_sd             | Posterior samples of the standard deviation of theta.  |
| gamma                | Posterior samples of the gamma parameter.  |
| z                    | Posterior samples of the z parameter, represented as a 3-dimensional matrix where the last axis denotes the dimension of the latent space. |
| w                    | Posterior samples of the w parameter, represented as a 3-dimensional matrix where the last axis denotes the dimension of the latent space. |
| accept_beta          | Acceptance ratio for the beta parameter.   |
| accept_theta         | Acceptance ratio for the theta parameter.  |
| accept_z             | Acceptance ratio for the z parameter.  |

|                |  |
|----------------|--|
| accept_w       | Acceptance ratio for the w parameter.          |
| accept_gamma   | Acceptance ratio for the gamma parameter.      |
| sigma_estimate | Posterior estimates of the standard deviation. |
| sigma          | Posterior samples of the standard deviation.   |
| alpha_estimate | Posterior estimates of the alpha parameter.    |
| alpha          | Posterior estimates of the alpha parameter.    |
| accept_alpha   | Acceptance ratio for the alpha parameter.      |

### Examples

```
# generate example (continuous) item response matrix
data <- matrix(rnorm(500, mean = 0, sd = 1), ncol=10, nrow=50)
lsirm_result <- lsirm2pl_normal_o(data)

# The code following can achieve the same result.
lsirm_result <- lsirm(data ~ lsirm2pl(spikenslab = FALSE, fixed_gamma = FALSE))
```

---

|                    |   |
|--------------------|---|
| lsirm2pl_normal_ss | <i>2PL LSIRM with normal likelihood and model selection approach.</i> |
|--------------------|---|

---

### Description

[lsirm2pl\\_normal\\_ss](#) is used to fit 2PL LSIRM for continuous variable with model selection approach. [lsirm2pl\\_normal\\_ss](#) factorizes item response matrix into column-wise item effect, row-wise respondent effect and further embeds interaction effect in a latent space. Unlike 1PL model, 2PL model assumes the item effect can vary according to respondent, allowing additional parameter multiplied with respondent effect. The resulting latent space provides an interaction map that represents interactions between respondents and items.

### Usage

```
lsirm2pl_normal_ss(
  data,
  ndim = 2,
  niter = 15000,
  nburn = 2500,
  nthin = 5,
  nprint = 500,
  jump_beta = 0.4,
  jump_theta = 1,
  jump_alpha = 1,
  jump_gamma = 1,
  jump_z = 0.5,
  jump_w = 0.5,
  pr_mean_beta = 0,
```

```

pr_sd_beta = 1,
pr_mean_theta = 0,
pr_spike_mean = -3,
pr_spike_sd = 1,
pr_slab_mean = 0.5,
pr_slab_sd = 1,
pr_mean_alpha = 0.5,
pr_sd_alpha = 1,
pr_a_eps = 0.001,
pr_b_eps = 0.001,
pr_a_theta = 0.001,
pr_b_theta = 0.001,
pr_xi_a = 0.001,
pr_xi_b = 0.001,
verbose = FALSE
)

```

### Arguments

|               |   |
|---------------|---|
| data          | Matrix; a binary or continuous item response matrix for analysis. Each row represents a respondent, and each column contains responses to the corresponding item. |
| ndim          | Integer; the dimension of the latent space. Default is 2.   |
| niter         | Integer; the total number of MCMC iterations to run. Default is 15000.  |
| nburn         | Integer; the number of initial MCMC iterations to discard as burn-in. Default is 2500.  |
| nthin         | Integer; the number of MCMC iterations to thin. Default is 5.   |
| nprint        | Integer; the interval at which MCMC samples are displayed during execution. Default is 500.   |
| jump_beta     | Numeric; the jumping rule for the beta proposal density. Default is 0.4.  |
| jump_theta    | Numeric; the jumping rule for the theta proposal density. Default is 1.0.   |
| jump_alpha    | Numeric; the jumping rule for the alpha proposal density. Default is 1.0.   |
| jump_gamma    | Numeric; the jumping rule for the theta proposal density. Default is 1.0.   |
| jump_z        | Numeric; the jumping rule for the z proposal density. Default is 0.5.   |
| jump_w        | Numeric; the jumping rule for the w proposal density. Default is 0.5.   |
| pr_mean_beta  | Numeric; the mean of the normal prior for beta. Default is 0.   |
| pr_sd_beta    | Numeric; the standard deviation of the normal prior for beta. Default is 1.0.   |
| pr_mean_theta | Numeric; the mean of the normal prior for theta. Default is 0.  |
| pr_spike_mean | Numeric; mean of spike prior for log gamma default value is -3.   |
| pr_spike_sd   | Numeric; standard deviation of spike prior for log gamma default value is 1.  |
| pr_slab_mean  | Numeric; mean of spike prior for log gamma default value is 0.5.  |
| pr_slab_sd    | Numeric; standard deviation of spike prior for log gamma default value is 1.  |
| pr_mean_alpha | Numeric; the mean of the log normal prior for alpha. Default is 0.5.  |

|             |  |
|-------------|--|
| pr_sd_alpha | Numeric; the standard deviation of the log normal prior for alpha. Default is 1.0.                   |
| pr_a_eps    | Numeric; shape parameter of inverse gamma prior for variance of data likelihood. Default is 0.001.   |
| pr_b_eps    | Numeric; scale parameter of inverse gamma prior for variance of data likelihood. Default is 0.001.   |
| pr_a_theta  | Numeric; the shape parameter of the inverse gamma prior for the variance of theta. Default is 0.001. |
| pr_b_theta  | Numeric; the scale parameter of the inverse gamma prior for the variance of theta. Default is 0.001. |
| pr_xi_a     | Numeric; first shape parameter of beta prior for latent variable xi. Default is 1.                   |
| pr_xi_b     | Numeric; second shape parameter of beta prior for latent variable xi. Default is 1.                  |
| verbose     | Logical; If TRUE, MCMC samples are printed for each nprint. Default is FALSE.                        |

### Details

lsirm2pl\_normal\_ss models the continuous value of response by respondent  $j$  to item  $i$  with item effect  $\beta_i$ , respondent effect  $\theta_j$  and the distance between latent position  $w_i$  of item  $i$  and latent position  $z_j$  of respondent  $j$  in the shared metric space, with  $\gamma$  represents the weight of the distance term. For 2pl model, the item effect is assumed to have additional discrimination parameter  $\alpha_i$  multiplied by  $\theta_j$ :

$$Y_{j,i} = \theta_j + \beta_i - \gamma ||z_j - w_i|| + e_{j,i}$$

where the error  $e_{j,i} \sim N(0, \sigma^2)$ . lsirm2pl\_normal\_ss model include model selection approach based on spike-and-slab priors for log gamma. For detail of spike-and-slab priors, see References.

### Value

lsirm2pl\_normal\_ss returns an object of list containing the following components:

|                      |   |
|----------------------|---|
| data                 | Data frame or matrix containing the variables in the model.                               |
| bic                  | Numeric value with the corresponding BIC.   |
| mcmc_inf             | number of mcmc iteration, burn-in periods, and thinning intervals.                        |
| map_inf              | value of log maximum a posterior and iteration number which have log maximum a posterior. |
| beta_estimate        | posterior estimation of beta.   |
| theta_estimate       | posterior estimation of theta.  |
| sigma_theta_estimate | posterior estimation of standard deviation of theta.                                      |
| sigma_estimate       | posterior estimation of standard deviation.   |
| gamma_estimate       | posterior estimation of gamma.  |
| z_estimate           | posterior estimation of z.  |
| w_estimate           | posterior estimation of w.  |



|                |   |
|----------------|---|
| pi_estimate    | posterior estimation of phi. inclusion probability of gamma. if estimation of phi is less than 0.5, choose Rasch model with gamma = 0, otherwise latent space model with gamma > 0. |
| beta           | posterior samples of beta.  |
| theta          | posterior samples of theta.   |
| theta_sd       | posterior samples of standard deviation of theta.   |
| sigma          | posterior samples of standard deviation.  |
| gamma          | posterior samples of gamma.   |
| z              | posterior samples of z. The output is 3-dimensional matrix with last axis represent the dimension of latent space.  |
| w              | posterior samples of w. The output is 3-dimensional matrix with last axis represent the dimension of latent space.  |
| pi             | posterior samples of phi which is indicator of spike and slab prior. If phi is 1, log gamma follows the slab prior, otherwise follows the spike prior.                              |
| accept_beta    | accept ratio of beta.   |
| accept_theta   | accept ratio of theta.  |
| accept_w       | accept ratio of w.  |
| accept_z       | accept ratio of z.  |
| accept_gamma   | accept ratio of gamma.  |
| alpha_estimate | Posterior estimates of the alpha parameter.   |
| alpha          | Posterior estimates of the alpha parameter.   |
| accept_alpha   | Acceptance ratio for the alpha parameter.   |

## References

Ishwaran, H., & Rao, J. S. (2005). Spike and slab variable selection: frequentist and Bayesian strategies. *The Annals of Statistics*, 33(2), 730-773.

## Examples

```
# generate example (continuous) item response matrix
data <- matrix(rnorm(500, mean = 0, sd = 1), ncol=10, nrow=50)

lsirm_result <- lsirm2pl_normal_ss(data)

# The code following can achieve the same result.
lsirm_result <- lsirm(data ~ lsirm2pl(spikenslab = TRUE, fixed_gamma = FALSE))
```

lsirm2pl\_o

*2PL LSIRM.***Description**

`lsirm2pl_o` is used to fit 2PL LSIRM. `lsirm2pl_o` factorizes item response matrix into column-wise item effect, row-wise respondent effect and further embeds interaction effect in a latent space. Unlike 1PL model, 2PL model assumes the item effect can vary according to respondent, allowing additional parameter multiplied with respondent effect. The resulting latent space provides an interaction map that represents interactions between respondents and items.

**Usage**

```
lsirm2pl_o(
  data,
  ndim = 2,
  niter = 15000,
  nburn = 2500,
  nthin = 5,
  nprint = 500,
  jump_beta = 0.4,
  jump_theta = 1,
  jump_alpha = 1,
  jump_gamma = 0.025,
  jump_z = 0.5,
  jump_w = 0.5,
  pr_mean_beta = 0,
  pr_sd_beta = 1,
  pr_mean_theta = 0,
  pr_mean_gamma = 0.5,
  pr_sd_gamma = 1,
  pr_mean_alpha = 0.5,
  pr_sd_alpha = 1,
  pr_a_theta = 0.001,
  pr_b_theta = 0.001,
  verbose = FALSE
)
```

**Arguments**

|                    |   |
|--------------------|---|
| <code>data</code>  | Matrix; a binary or continuous item response matrix for analysis. Each row represents a respondent, and each column contains responses to the corresponding item. |
| <code>ndim</code>  | Integer; the dimension of the latent space. Default is 2.   |
| <code>niter</code> | Integer; the total number of MCMC iterations to run. Default is 15000.  |

|               |  |
|---------------|--|
| nburn         | Integer; the number of initial MCMC iterations to discard as burn-in. Default is 2500.               |
| nthin         | Integer; the number of MCMC iterations to thin. Default is 5.  |
| nprint        | Integer; the interval at which MCMC samples are displayed during execution. Default is 500.          |
| jump_beta     | Numeric; the jumping rule for the beta proposal density. Default is 0.4.                             |
| jump_theta    | Numeric; the jumping rule for the theta proposal density. Default is 1.0.                            |
| jump_alpha    | Numeric; the jumping rule for the alpha proposal density. Default is 1.0.                            |
| jump_gamma    | Numeric; the jumping rule for the gamma proposal density. Default is 0.025.                          |
| jump_z        | Numeric; the jumping rule for the z proposal density. Default is 0.5.                                |
| jump_w        | Numeric; the jumping rule for the w proposal density. Default is 0.5.                                |
| pr_mean_beta  | Numeric; the mean of the normal prior for beta. Default is 0.  |
| pr_sd_beta    | Numeric; the standard deviation of the normal prior for beta. Default is 1.0.                        |
| pr_mean_theta | Numeric; the mean of the normal prior for theta. Default is 0.                                       |
| pr_mean_gamma | Numeric; mean of log normal prior for gamma. Default is 0.5.   |
| pr_sd_gamma   | Numeric; standard deviation of log normal prior for gamma. Default is 1.0.                           |
| pr_mean_alpha | Numeric; the mean of the log normal prior for alpha. Default is 0.5.                                 |
| pr_sd_alpha   | Numeric; the standard deviation of the log normal prior for alpha. Default is 1.0.                   |
| pr_a_theta    | Numeric; the shape parameter of the inverse gamma prior for the variance of theta. Default is 0.001. |
| pr_b_theta    | Numeric; the scale parameter of the inverse gamma prior for the variance of theta. Default is 0.001. |
| verbose       | Logical; If TRUE, MCMC samples are printed for each nprint. Default is FALSE.                        |

## Details

lsirm2pl\_o models the probability of correct response by respondent  $j$  to item  $i$  with item effect  $\beta_i$ , respondent effect  $\theta_j$  and the distance between latent position  $w_i$  of item  $i$  and latent position  $z_j$  of respondent  $j$  in the shared metric space, with  $\gamma$  represents the weight of the distance term. For 2pl model, the item effect is assumed to have additional discrimination parameter  $\alpha_i$  multiplied by  $\theta_j$ :

$$\text{logit}(P(Y_{j,i} = 1 | \theta_j, \alpha_i, \beta_i, \gamma, z_j, w_i)) = \theta_j * \alpha_i + \beta_i - \gamma ||z_j - w_i||$$

## Value

lsirm2pl\_o returns an object of list containing the following components:

|          |   |
|----------|---|
| data     | Data frame or matrix containing the variables used in the model.                      |
| bic      | A numeric value representing the Bayesian Information Criterion (BIC).                |
| mcmc_inf | Details about the number of MCMC iterations, burn-in periods, and thinning intervals. |

|                      |  |
|----------------------|--|
| map_inf              | The log maximum a posteriori (MAP) value and the iteration number at which this MAP value occurs.  |
| beta_estimate        | Posterior estimates of the beta parameter.   |
| theta_estimate       | Posterior estimates of the theta parameter.  |
| sigma_theta_estimate | Posterior estimates of the standard deviation of theta.  |
| gamma_estimate       | Posterior estimates of gamma parameter.  |
| z_estimate           | Posterior estimates of the z parameter.  |
| w_estimate           | Posterior estimates of the w parameter.  |
| beta                 | Posterior samples of the beta parameter.   |
| theta                | Posterior samples of the theta parameter.  |
| theta_sd             | Posterior samples of the standard deviation of theta.  |
| gamma                | Posterior samples of the gamma parameter.  |
| z                    | Posterior samples of the z parameter, represented as a 3-dimensional matrix where the last axis denotes the dimension of the latent space. |
| w                    | Posterior samples of the w parameter, represented as a 3-dimensional matrix where the last axis denotes the dimension of the latent space. |
| accept_beta          | Acceptance ratio for the beta parameter.   |
| accept_theta         | Acceptance ratio for the theta parameter.  |
| accept_z             | Acceptance ratio for the z parameter.  |
| accept_w             | Acceptance ratio for the w parameter.  |
| accept_gamma         | Acceptance ratio for the gamma parameter.  |
| alpha_estimate       | Posterior estimates of the alpha parameter.  |
| alpha                | Posterior estimates of the alpha parameter.  |
| accept_alpha         | Acceptance ratio for the alpha parameter.  |

## Examples

```
# generate example item response matrix
data <- matrix(rbinom(500, size = 1, prob = 0.5), ncol=10, nrow=50)

lsirm_result <- lsirm2pl_o(data)

# The code following can achieve the same result.
lsirm_result <- lsirm(data ~ lsirm2pl(spikenslab = FALSE, fixed_gamma = FALSE))
```

lsirm2pl\_ss

*2PL LSIRM with model selection approach.***Description**

`lsirm2pl_ss` is used to fit 2PL LSIRM with model selection approach based on spike-and-slab priors. `lsirm2pl_ss` factorizes item response matrix into column-wise item effect, row-wise respondent effect and further embeds interaction effect in a latent space. Unlike 1PL model, 2PL model assumes the item effect can vary according to respondent, allowing additional parameter multiplied with respondent effect. The resulting latent space provides an interaction map that represents interactions between respondents and items.

**Usage**

```
lsirm2pl_ss(
  data,
  ndim = 2,
  niter = 15000,
  nburn = 2500,
  nthin = 5,
  nprint = 500,
  jump_beta = 0.4,
  jump_theta = 1,
  jump_alpha = 1,
  jump_gamma = 1,
  jump_z = 0.5,
  jump_w = 0.5,
  pr_mean_beta = 0,
  pr_sd_beta = 1,
  pr_mean_theta = 0,
  pr_spike_mean = -3,
  pr_spike_sd = 1,
  pr_slab_mean = 0.5,
  pr_slab_sd = 1,
  pr_mean_alpha = 0.5,
  pr_sd_alpha = 1,
  pr_a_theta = 0.001,
  pr_b_theta = 0.001,
  pr_xi_a = 1,
  pr_xi_b = 1,
  verbose = FALSE
)
```

**Arguments**

|                   |   |
|-------------------|---|
| <code>data</code> | Matrix; a binary or continuous item response matrix for analysis. Each row represents a respondent, and each column contains responses to the corresponding item. |
|-------------------|---|

|               |  |
|---------------|--|
| ndim          | Integer; the dimension of the latent space. Default is 2.  |
| niter         | Integer; the total number of MCMC iterations to run. Default is 15000.                               |
| nburn         | Integer; the number of initial MCMC iterations to discard as burn-in. Default is 2500.               |
| nthin         | Integer; the number of MCMC iterations to thin. Default is 5.  |
| nprint        | Integer; the interval at which MCMC samples are displayed during execution. Default is 500.          |
| jump_beta     | Numeric; the jumping rule for the beta proposal density. Default is 0.4.                             |
| jump_theta    | Numeric; the jumping rule for the theta proposal density. Default is 1.0.                            |
| jump_alpha    | Numeric; the jumping rule for the alpha proposal density. Default is 1.0.                            |
| jump_gamma    | Numeric; the jumping rule for the theta proposal density. Default is 1.0.                            |
| jump_z        | Numeric; the jumping rule for the z proposal density. Default is 0.5.                                |
| jump_w        | Numeric; the jumping rule for the w proposal density. Default is 0.5.                                |
| pr_mean_beta  | Numeric; the mean of the normal prior for beta. Default is 0.  |
| pr_sd_beta    | Numeric; the standard deviation of the normal prior for beta. Default is 1.0.                        |
| pr_mean_theta | Numeric; the mean of the normal prior for theta. Default is 0.                                       |
| pr_spike_mean | Numeric; the mean of spike prior for log gamma. Default is -3.                                       |
| pr_spike_sd   | Numeric; the standard deviation of spike prior for log gamma. Default is 1.                          |
| pr_slab_mean  | Numeric; the mean of spike prior for log gamma. Default is 0.5.                                      |
| pr_slab_sd    | Numeric; the standard deviation of spike prior for log gamma. Default is 1.                          |
| pr_mean_alpha | Numeric; the mean of the log normal prior for alpha. Default is 0.5.                                 |
| pr_sd_alpha   | Numeric; the standard deviation of the log normal prior for alpha. Default is 1.0.                   |
| pr_a_theta    | Numeric; the shape parameter of the inverse gamma prior for the variance of theta. Default is 0.001. |
| pr_b_theta    | Numeric; the scale parameter of the inverse gamma prior for the variance of theta. Default is 0.001. |
| pr_xi_a       | Numeric; the first shape parameter of beta prior for latent variable xi. Default is 1.               |
| pr_xi_b       | Numeric; the second shape parameter of beta prior for latent variable xi. Default is 1.              |
| verbose       | Logical; If TRUE, MCMC samples are printed for each nprint. Default is FALSE.                        |

### Details

lsirm2pl\_ss models the probability of correct response by respondent  $j$  to item  $i$  with item effect  $\beta_i$ , respondent effect  $\theta_j$  and the distance between latent position  $w_i$  of item  $i$  and latent position  $z_j$  of respondent  $j$  in the shared metric space, with  $\gamma$  represents the weight of the distance term. For 2pl model, the item effect is assumed to have additional discrimination parameter  $\alpha_i$  multiplied by  $\theta_j$ :

$$\text{logit}(P(Y_{j,i} = 1 | \theta_j, \alpha_i, \beta_i, z_j, w_i)) = \theta_j * \alpha_i + \beta_i - \gamma ||z_j - w_i||$$

lsirm2pl\_ss model include model selection approach based on spike-and-slab priors for log gamma. For detail of spike-and-slab priors, see References.

**Value**

lsirm2pl\_ss returns an object of list containing the following components:

|                      |   |
|----------------------|---|
| data                 | Data frame or matrix containing the variables used in the model.  |
| bic                  | A numeric value representing the Bayesian Information Criterion (BIC).  |
| mcmc_inf             | Details about the number of MCMC iterations, burn-in periods, and thinning intervals.   |
| map_inf              | The log maximum a posteriori (MAP) value and the iteration number at which this MAP value occurs.   |
| beta_estimate        | Posterior estimates of the beta parameter.  |
| theta_estimate       | Posterior estimates of the theta parameter.   |
| sigma_theta_estimate | Posterior estimates of the standard deviation of theta.   |
| gamma_estimate       | Posterior estimates of gamma parameter.   |
| z_estimate           | Posterior estimates of the z parameter.   |
| w_estimate           | Posterior estimates of the w parameter.   |
| beta                 | Posterior samples of the beta parameter.  |
| theta                | Posterior samples of the theta parameter.   |
| theta_sd             | Posterior samples of the standard deviation of theta.   |
| gamma                | Posterior samples of the gamma parameter.   |
| z                    | Posterior samples of the z parameter, represented as a 3-dimensional matrix where the last axis denotes the dimension of the latent space.  |
| w                    | Posterior samples of the w parameter, represented as a 3-dimensional matrix where the last axis denotes the dimension of the latent space.  |
| accept_beta          | Acceptance ratio for the beta parameter.  |
| accept_theta         | Acceptance ratio for the theta parameter.   |
| accept_z             | Acceptance ratio for the z parameter.   |
| accept_w             | Acceptance ratio for the w parameter.   |
| accept_gamma         | Acceptance ratio for the gamma parameter.   |
| pi_estimate          | Posterior estimation of phi. inclusion probability of gamma. if estimation of phi is less than 0.5, choose Rasch model with gamma = 0, otherwise latent space model with gamma > 0. |
| pi                   | Posterior samples of phi which is indicator of spike and slab prior. If phi is 1, log gamma follows the slab prior, otherwise follows the spike prior.                              |
| alpha_estimate       | Posterior estimates of the alpha parameter.   |
| alpha                | Posterior estimates of the alpha parameter.   |
| accept_alpha         | Acceptance ratio for the alpha parameter.   |

**References**

Ishwaran, H., & Rao, J. S. (2005). Spike and slab variable selection: Frequentist and Bayesian strategies. *The Annals of Statistics*, 33(2), 730-773.

### Examples

```
# generate example item response matrix
data <- matrix(rbinom(500, size = 1, prob = 0.5), ncol=10, nrow=50)

lsirm_result <- lsirm2pl_ss(data)

# The code following can achieve the same result.
lsirm_result <- lsirm(data ~ lsirm2pl(spikenslab = TRUE, fixed_gamma = FALSE))
```

---

onepl

1PL Rasch model.

---

### Description

[onepl](#) is used to fit 1PL Rasch model.

### Usage

```
onepl(
  data,
  niter = 15000,
  nburn = 2500,
  nthin = 5,
  nprint = 500,
  jump_beta = 0.4,
  jump_theta = 1,
  pr_mean_beta = 0,
  pr_sd_beta = 1,
  pr_mean_theta = 0,
  pr_a_theta = 0.001,
  pr_b_theta = 0.001
)
```

### Arguments

|           |  |
|-----------|--|
| data      | Matrix; binary item response matrix to be analyzed. Each row is assumed to be respondent and its column values are assumed to be response to the corresponding item. |
| niter     | Numeric; number of iterations to run MCMC sampling. default value is 15000.  |
| nburn     | Numeric; number of initial, pre-thinning, MCMC iterations to discard. default value is 2500.   |
| nthin     | Numeric; number of thinning, MCMC iterations to discard. default value is 5.   |
| nprint    | Numeric; MCMC samples is displayed during execution of MCMC chain for each nprint. default value is 500.   |
| jump_beta | Numeric; jumping rule of the proposal density for beta. default value is 0.4.  |



|               |  |
|---------------|--|
| jump_theta    | Numeric; jumping rule of the proposal density for theta. default value is 1.0.                 |
| pr_mean_beta  | Numeric; mean of normal prior for beta. default value is 0.                                    |
| pr_sd_beta    | Numeric; standard deviation of normal prior for beta. default value is 1.0.                    |
| pr_mean_theta | Numeric; mean of normal prior for theta. default value is 0.                                   |
| pr_a_theta    | Numeric; shape parameter of inverse gamma prior for variance of theta. default value is 0.001. |
| pr_b_theta    | Numeric; scale parameter of inverse gamma prior for variance of theta. default value is 0.001. |

### Details

onepl models the probability of correct response by respondent  $j$  to item  $i$  with item effect  $\beta_i$ , respondent effect  $\theta_j$ :

$$\text{logit}(P(Y_{j,i} = 1|\theta_j, \beta_i)) = \theta_j + \beta_i$$

### Value

onepl returns an object of list containing the following components:

|                      |  |
|----------------------|--|
| beta_estimate        | posterior estimation of beta.                        |
| theta_estimate       | posterior estimation of theta.                       |
| sigma_theta_estimate | posterior estimation of standard deviation of theta. |
| beta                 | posterior samples of beta.                           |
| theta                | posterior samples of theta.                          |
| theta_sd             | posterior samples of standard deviation of theta.    |
| accept_beta          | accept ratio of beta.                                |
| accept_theta         | accept ratio of theta.                               |

### Examples

```
# generate example item response matrix
data <- matrix(rbinom(500, size = 1, prob = 0.5), ncol=10, nrow=50)

result <- onepl(data)
```

---

|      |  |
|------|--|
| plot | <i>Plotting the interaction map or summarizing the parameter estimate of fitted LSIRM with box plot.</i> |
|------|--|

---

### Description

`plot` is used to plot the interaction map of fitted LSIRM or summarizing the parameter estimate of fitted LSIRM with box plot.

### Usage

```
plot(
  object,
  ...,
  option = "interaction",
  rotation = FALSE,
  cluster = NA,
  which.clust = "item",
  interact = FALSE,
  chain.idx = 1
)
```

### Arguments

|                          |  |
|--------------------------|--|
| <code>object</code>      | Object of class <code>lsirm</code> .   |
| <code>...</code>         | Additional arguments for the corresponding function.   |
| <code>option</code>      | Character; If value is "interaction", draw the interaction map that represents interactions between respondents and items. If value is "beta", draw the boxplot for the posterior samples of beta. If value is "theta", draw the distribution of the theta estimates per total test score for the data. If value is "alpha", draw the boxplot for the posterior samples of alpha. The "alpha" is only available for 2PL LSIRM. |
| <code>rotation</code>    | Logical; If TRUE the latent positions are visualized after oblique (oblimin) rotation.   |
| <code>cluster</code>     | Character; If value is "neyman" the cluster result are visualized by Point Process Cluster Analysis. If value is "spectral", spectral clustering method applied. Default is NA.  |
| <code>which.clust</code> | Character; Choose which values to clustering. "resp" is the option for respondent and "item" is the option for items. Default is "item".   |
| <code>interact</code>    | Logical; If TRUE, draw the interaction map interactively.  |
| <code>chain.idx</code>   | Numeric; Index of MCMC chain. Default is 1.  |

### Value

`plot` returns the interaction map or boxplot for parameter estimate.

**Examples**

```
# generate example item response matrix
data      <- matrix(rbinom(500, size = 1, prob = 0.5), ncol=10, nrow=50)
lsirm_result <- lsirm(data ~ lsirm1pl())
plot(lsirm_result)

# use oblique rotation
plot(lsirm_result, rotation = TRUE)

# interaction map interactively
plot(lsirm_result, interact = TRUE)

# clustering the respondents or items
plot(lsirm_result, cluster = TRUE)
```

---

```
print.summary.lsirm    Print the summary the result of LSIRM
```

---

**Description**

[print.summary.lsirm](#) is used to print summary the result of LSIRM.

**Usage**

```
## S3 method for class 'summary.lsirm'
print(x, ...)
```

**Arguments**

**x**                      List; summary of LSIRM with `summary.lsirm`.  
**...**                   Additional arguments.

**Value**

`print.summary.lsirm` return a summary of LSIRM.

**Examples**

```
# generate example item response matrix
data      <- matrix(rbinom(500, size = 1, prob = 0.5), ncol=10, nrow=50)
lsirm_result <- lsirm(data ~ lsirm1pl())
summary(lsirm_result)
```

---

|               |                                    |
|---------------|------------------------------------|
| summary.lsirm | <i>Summary the result of LSIRM</i> |
|---------------|------------------------------------|

---

## Description

`summary` is used to summary the result of LSIRM.

## Usage

```
## S3 method for class 'lsirm'
summary(object, chain.idx = 1, estimate = "mean", CI = 0.95, ...)
```

## Arguments

|                        |   |
|------------------------|---|
| <code>object</code>    | Object of class <code>lsirm</code> .  |
| <code>chain.idx</code> | Numeric; Index of MCMC chain. Default is 1.   |
| <code>estimate</code>  | Character; Specifies the type of posterior estimate to provide for beta parameters. Options are "mean", "median", or "mode". Default is "mean". |
| <code>CI</code>        | Numeric; The significance level for the highest posterior density interval (HPD) for the beta parameters. Default is 0.95.                      |
| <code>...</code>       | Additional arguments.   |

## Value

`summary.lsirm` contains following elements. A print method is available.

|                       |   |
|-----------------------|---|
| <code>call</code>     | R call used to fit the model.   |
| <code>coef</code>     | Covariate coefficients posterior means.   |
| <code>mcmc.opt</code> | The number of mcmc iteration, burn-in periods, and thinning intervals.                    |
| <code>map.inf</code>  | Value of log maximum a posterior and iteration number which have log maximum a posterior. |
| <code>BIC</code>      | Numeric value with the corresponding Bayesian information criterion (BIC).                |
| <code>method</code>   | Which model is fitted.  |
| <code>missing</code>  | The assumed missing type. One of NA, "mar" and "mcar".                                    |
| <code>dtype</code>    | Type of input data (Binary or Continuous).  |
| <code>ss</code>       | Whether a model selection approach using the spike-slab prior is applied.                 |

## Examples

```
# generate example item response matrix
data <- matrix(rbinom(500, size = 1, prob = 0.5), ncol=10, nrow=50)

# 1PL LSIRM object
lsirm_result <- lsirm(data ~ lsirm1pl())
summary(lsirm_result)
```

TDRI

*Inductive Reasoning Developmental Test***Description**

TDRI dataset is the answer to Inductive Reasoning Developmental Test of 1,803 Brazilians with age varying from 5 to 85 years.

**Usage**

```
data(TDRI)
```

**Format**

A binary matrix with 1,803 rows and 56 columns.

**Details**

It presents data from 1,803 Brazilians (52.5% female) with age varying from 5 to 85 years ( $M = 15.75$ ;  $SD = 12.21$ ) that answered to the Inductive Reasoning Developmental Test – IRDT, with 56 items designed to assess developmentally sequenced and hierarchically organized inductive reasoning.

**Source**

[https://figshare.com/articles/dataset/TDRI\\_dataset\\_csv/3142321](https://figshare.com/articles/dataset/TDRI_dataset_csv/3142321)

twopl

*2PL Rasch model.***Description**

`twopl` is used to fit 2PL Rasch model. Unlike 1PL model, 2PL model assumes the item effect can vary according to respondent, allowing additional parameter multiplied with respondent effect.

**Usage**

```
twopl(
  data,
  niter = 15000,
  nburn = 2500,
  nthin = 5,
  nprint = 500,
  jump_beta = 0.4,
  jump_theta = 1,
  jump_alpha = 1,
```

```

pr_mean_beta = 0,
pr_sd_beta = 1,
pr_mean_theta = 0,
pr_mean_alpha = 0.5,
pr_sd_alpha = 1,
pr_a_theta = 0.001,
pr_b_theta = 0.001
)

```

### Arguments

|               |  |
|---------------|--|
| data          | Matrix; binary item response matrix to be analyzed. Each row is assumed to be respondent and its column values are assumed to be response to the corresponding item. |
| niter         | Numeric; number of iterations to run MCMC sampling. default value is 15000.  |
| nburn         | Numeric; number of initial, pre-thinning, MCMC iterations to discard. default value is 2500.   |
| nthin         | Numeric; number of thinning, MCMC iterations to discard. default value is 5.   |
| nprint        | Numeric; MCMC samples is displayed during execution of MCMC chain for each nprint. default value is 500.   |
| jump_beta     | Numeric; jumping rule of the proposal density for beta. default value is 0.4.  |
| jump_theta    | Numeric; jumping rule of the proposal density for theta. default value is 1.0.   |
| jump_alpha    | Numeric; jumping rule of the proposal density for alpha default value is 1.0.  |
| pr_mean_beta  | Numeric; mean of normal prior for beta. default value is 0.  |
| pr_sd_beta    | Numeric; standard deviation of normal prior for beta. default value is 1.0.  |
| pr_mean_theta | Numeric; mean of normal prior for theta. default value is 0.   |
| pr_mean_alpha | Numeric; mean of normal prior for alpha. default value is 0.5.   |
| pr_sd_alpha   | Numeric; mean of normal prior for beta. default value is 1.0.  |
| pr_a_theta    | Numeric; shape parameter of inverse gamma prior for variance of theta. default value is 0.001.   |
| pr_b_theta    | Numeric; scale parameter of inverse gamma prior for variance of theta. default value is 0.001.   |

### Details

twopl models the probability of correct response by respondent  $j$  to item  $i$  with item effect  $\beta_i$ , respondent effect  $\theta_j$ . For 2pl model, the item effect is assumed to have additional discrimination parameter  $\alpha_i$  multiplied by  $\theta_j$ :

$$\text{logit}(P(Y_{j,i} = 1 | \theta_j, \beta_i, \alpha_i)) = \theta_j * \alpha_i + \beta_i$$

**Value**

twopl returns an object of list containing the following components:

|                      |  |
|----------------------|--|
| beta_estimate        | posterior estimation of beta.                        |
| theta_estimate       | posterior estimation of theta.                       |
| sigma_theta_estimate | posterior estimation of standard deviation of theta. |
| alpha_estimate       | posterior estimation of alpha.                       |
| beta                 | posterior samples of beta.                           |
| theta                | posterior samples of theta.                          |
| theta_sd             | posterior samples of standard deviation of theta.    |
| alpha                | posterior samples of alpha.                          |
| accept_beta          | accept ratio of beta.                                |
| accept_theta         | accept ratio of theta.                               |
| accept_alpha         | accept ratio of alpha.                               |

**Examples**

```
# generate example item response matrix
data <- matrix(rbinom(500, size = 1, prob = 0.5), ncol=10, nrow=50)

result <- twopl(data)
```

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