# Package 'independenceWeights'

October 13, 2022

Title Estimates Weights for Confounding Control for Continuous-Valued Exposures Version 0.0.1

**Description** Estimates weights to make a continuous-valued exposure statistically independent of a vector of pre-treatment covariates using the method proposed in Huling, Greifer, and Chen (2021) <a href="https://arxiv.2107.07086">arxiv.2107.07086</a>>.

License MIT + file LICENSE

**Encoding** UTF-8

RoxygenNote 7.1.1

**Depends** osqp (>= 0.6.0.3)

Imports locfit

Suggests cobalt

NeedsCompilation no

Author Jared Huling [aut, cre] (<https://orcid.org/0000-0003-0670-4845>), Noah Greifer [aut] (<https://orcid.org/0000-0003-3067-7154>)

Maintainer Jared Huling <jaredhuling@gmail.com>

**Repository** CRAN

Date/Publication 2022-05-10 15:20:02 UTC

# **R** topics documented:

independence_weights	2
print.independence_weights	4
simulate_confounded_data	5
weighted_energy_stats	7
weighted_kernel_est	8
	10

Index

independence\_weights Construction of distance covariance optimal weights weights

# Description

Constructs independence-inducing weights (distance covariance optimal weights) for estimation of causal quantities for continuous-valued treatments

#### Usage

```
independence_weights(
    A,
    X,
    lambda = 0,
    decorrelate_moments = FALSE,
    preserve_means = FALSE,
    dimension_adj = TRUE
)
```

#### Arguments

A	vector indicating the value of the treatment or exposure variable. Should be a numeric vector.	
Х	matrix of covariates with number of rows equal to the length of A and each column is a <b>pre-treatment</b> covariate to be balanced between treatment groups.	
lambda	tuning parameter for the penalty on the sum of squares of the weights	
decorrelate_moments		
	logical scalar. Whether or not to add constraints that result in exact decorrelation of weighted first order moments of X and A. Defaults to FALSE.	
preserve_means	logical scalar. Whether or not to add constraints that result in exact preservation of weighted first order moments of X and A. Defaults to FALSE.	
dimension_adj	logical scalar. Whether or not to add adjustment to energy distance terms that account for the dimensionality of X. Defaults to TRUE.	

#### Value

An object of class "independence_weights" with elements:	
weights	A vector of length nrow(X) containing the estimated sample weights
А	Treatment vector
opt	The optimization object returned by osqp::solve_osqp()
objective	The value of the objective function at its optimal value. This is the weighted dependence statistic plus any ridge penalty on the weights.
D_unweighted	The value of the weighted dependence distance using all weights = 1 (i.e. un-weighted)

D_w	The value of the weighted dependence distance of Huling, et al. (2021) using the optimal estimated weights. This is the weighted dependence statistic without the ridge penalty on the weights.		
distcov_unweig	hted		
_	The unweighted distance covariance term. This is the standard distance covariance of Szekely et al (2007). This term is always equal to D_unweighted.		
distcov_weight	ed		
	The weighted distance covariance term. This term itself does not directly mea- sure weighted dependence but is a critical component of it.		
energy_A	The weighted energy distance between A and its weighted version		
energy_X	The weighted energy distance between X and its weighted version		
ess	The estimated effective sample size of the weights using Kish's effective sample size formula.		
An object of class	An object of class "independence_weights".		
weights	the estimated weights, the distance covariance optimal weights (DCOWs)		
А	the treatment vector		
opt	the object returned by whatever optimization routine was used		
objective	the value of the optimized objective function		
distcov_unweighted			
	the unweighted distance covariance between treatment and covariates		
distcov_weight			
	the weighted distance covariance between treatment and covariates		
energy_A	the (energy) distance between the treatment distribution and the weighted treat- ment distribution. Smaller values mean the marginal distribution of the treat- ment is preserved after weighting		
energy_x	the (energy) distance between the covariate distribution and the weighted covari- ate distribution. Smaller values mean the marginal distribution of the covariates is preserved after weighting		
ess	the expected sample size after weighting. Kish's approximation is used		

#### References

Szekely, G. J., Rizzo, M. L., & Bakirov, N. K. (2007). Measuring and testing dependence by correlation of distances. Annals of Statistics 35(6) 2769-2794 doi: 10.1214/009053607000000505

Huling, J. D., Greifer, N., & Chen, G. (2021). Independence weights for causal inference with continuous exposures. arXiv preprint arXiv:2107.07086. https://arxiv.org/abs/2107.07086

#### See Also

print.independence\_weights for printing of fitted energy balancing objects

#### Examples

```
simdat <- simulate_confounded_data(seed = 999, nobs = 500)</pre>
y <- simdat$data$Y</pre>
A <- simdat$data$A
X <- as.matrix(simdat$data[c("Z1", "Z2", "Z3", "Z4", "Z5")])</pre>
dcows <- independence_weights(A, X)</pre>
print(dcows)
# distribution of response:
quantile(y)
## create grid
trt_vec <- seq(min(simdat$data$A), 50, length.out=500)</pre>
## estimate ADRF
adrf_hat <- weighted_kernel_est(A, y, dcows$weights, trt_vec)$est</pre>
## estimate naively without weights
adrf_hat_unwtd <- weighted_kernel_est(A, y, rep(1, length(y)), trt_vec)$est</pre>
ylims <- range(c(simdat$data$Y, simdat$true_adrf(trt_vec)))</pre>
plot(x = simdat$data$A, y = simdat$data$Y, ylim = ylims, xlim = c(0,50))
## true ADRF
lines(x = trt_vec, y = simdat$true_adrf(trt_vec), col = "blue", lwd=2)
## estimated ADRF
lines(x = trt_vec, y = adrf_hat, col = "red", lwd=2)
## naive estimate
lines(x = trt_vec, y = adrf_hat_unwtd, col = "green", lwd=2)
```

print.independence\_weights

Printing results for estimated energy balancing weights

#### Description

Prints results for energy balancing weights

Prints weighted energy statistics for given weights

#### Usage

```
## S3 method for class 'independence_weights'
print(x, digits = max(getOption("digits") - 3, 3), ...)
## S3 method for class 'weighted_energy_terms'
print(x, digits = max(getOption("digits") - 3, 3), ...)
```

4

#### Arguments

х	a fitted object from weighted_energy_stats
digits	minimal number of significant digits to print.
	further arguments passed to or from print.default.

#### Value

Nothing returned Nothing returned

#### See Also

independence\_weights for function which produces energy balancing weights
weighted\_energy\_stats for function which produces energy balancing weights

```
simulate_confounded_data
```

Simulation of confounded data with a continuous treatment

#### Description

Simulates confounded data with continuous treatment based on Vegetabile et al's simulation

#### Usage

```
simulate_confounded_data(
    seed = 1,
    nobs = 1000,
    MX1 = -0.5,
    MX2 = 1,
    MX3 = 0.3,
    A_effect = TRUE
)
```

# Arguments

seed	random seed for reproducibility
nobs	number of observations
MX1	the mean of the first covariate. Defaults to -0.5, the value used in the simulations of Vegetabile, et al (2021).
MX2	the mean of the second and fourth covariates. Defaults to 1, the value used in the simulations of Vegetabile, et al (2021).
MX3	the probability that the fifth covariate (a binary covariate) is equal to 1. Defaults to 0.3, the value used in the simulations of Vegetabile, et al (2021).
A_effect	whether (TRUE) or not (FALSE) the treatment has a causal effect on the outcome. If TRUE, the setting used is that of the main text of Vegetabile, et al (2021). If FALSE, the setting is that used in the Appendix of Vegetabile, et al (2021).

#### Value

An list with elements:

data	A simulated dataset with nobs rows	
true_adrf	A function that inputs values of the treatment A and outputs the true ADRF, $E(Y(A))$ , of the data-generating mechanism used to generate data.	
A list with the following elements		
data	a data.frame with the response (Y), treatment (A), confounders (Z1 to Z5), and true average dose response function truth	
true_adrf	a function; true average dose response function	
original_covariates		
	original, untransformed covariates in the simulation setup. Do not use, as it makes the simulation setup significantly easier.	

#### References

Vegetabile, B. G., Griffin, B. A., Coffman, D. L., Cefalu, M., Robbins, M. W., and McCaffrey, D. F. (2021). Nonparametric estimation of population average dose-response curves using entropy balancing weights for continuous exposures. Health Services and Outcomes Research Methodology, 21(1), 69-110.

#### Examples

```
simdat <- simulate_confounded_data(seed = 999, nobs = 500)
str(simdat$data)
A <- simdat$data$A
y <- simdat$data$A
y <- simdat$data$Y
trt_vec <- seq(min(simdat$data$A), max(simdat$data$A), length.out=500)
ylims <- range(c(simdat$data$Y, simdat$true_adrf(trt_vec)))
plot(x = simdat$data$A, y = simdat$data$Y, ylim = ylims)
lines(x = trt_vec, y = simdat$true_adrf(trt_vec), col = "blue", lwd=2)
## naive estimate of ADRF without weights
adrf_hat_unwtd <- weighted_kernel_est(A, y, rep(1, length(y)), trt_vec)$test</pre>
```

lines(x = trt\_vec, y = adrf\_hat\_unwtd, col = "green", lwd=2)

weighted\_energy\_stats Calculation of weighted energy statistics for weighted dependence

## Description

Calculates weighted energy statistics used to quantify weighted dependence

## Usage

```
weighted_energy_stats(A, X, weights, dimension_adj = TRUE)
```

#### Arguments

Α	treatment vector indicating values of the treatment/exposure variable.
Х	matrix of covariates with number of rows equal to the length of weights and each column is a covariate
weights	a vector of sample weights
dimension_adj	logical scalar. Whether or not to add adjustment to energy distance terms that account for the dimensionality of x. Defaults to TRUE.

#### Value

a list with the following components

D_w	The value of the weighted dependence distance of Huling, et al. (2021) using the optimal estimated weights. This is the weighted dependence statistic without the ridge penalty on the weights.	
distcov_unweigh	ted	
	The unweighted distance covariance term. This is the standard distance covariance of Szekely et al (2007). This term is always equal to D_unweighted.	
distcov_weighte	d	
	The weighted distance covariance term. This term itself does not directly measure weighted dependence but is a critical component of it.	
energy_A	The weighted energy distance between A and its weighted version	
energy_X	The weighted energy distance between X and its weighted version	
ess	The estimated effective sample size of the weights using Kish's effective sample size formula.	
An object of class "weighted_energy_terms".		
D_w distcov_unweigh	the value of the DCOW measure ted	
	the unweighted distance covariance between treatment and covariates	
distcov_weighted		
-	the weighted distance covariance between treatment and covariates	

energy_A	the (energy) distance between the treatment distribution and the weighted treat- ment distribution. Smaller values mean the marginal distribution of the treat- ment is preserved after weighting
energy_x	the (energy) distance between the covariate distribution and the weighted covari- ate distribution. Smaller values mean the marginal distribution of the covariates is preserved after weighting
ess	the expected sample size after weighting. Kish's approximation is used

#### References

Szekely, G. J., Rizzo, M. L., & Bakirov, N. K. (2007). Measuring and testing dependence by correlation of distances. Annals of Statistics 35(6) 2769-2794 doi: 10.1214/009053607000000505

Huling, J. D., Greifer, N., & Chen, G. (2021). Independence weights for causal inference with continuous exposures. arXiv preprint arXiv:2107.07086. https://arxiv.org/abs/2107.07086

#### Examples

simdat <- simulate\_confounded\_data(seed = 999, nobs = 100)
str(simdat\$data)
A <- simdat\$data\$A
X <- as.matrix(simdat\$data[c("Z1", "Z2", "Z3", "Z4", "Z5")])
wts <- runif(length(A))
weighted\_energy\_stats(A, X, wts)</pre>

weighted\_kernel\_est Calculation of weighted nonparametric regression estimate of the dose response function

#### Description

Calculates weighted nonparametric regression estimate of the causal average dose response function

#### Usage

```
weighted_kernel_est(A, y, weights, Aseq)
```

#### Arguments

А	vector indicating the value of the treatment or exposure variable. Should be a
	numeric vector.
У	vector of responses
weights	a vector of sample weights of length equal to the length of y
Aseq	a vector of new points for which to obtain estimates of E(Y(a))

## Value

A list with the following elements

fit	A fitted model object from the lp function
estimated	a vector of estimates of a causal ADRF at the values of the treatment specified
	by Aseq

# Index

independence\_weights, 2, 5

1p, <mark>9</mark>

simulate\_confounded\_data, 5

weighted\_energy\_stats, 5, 7
weighted\_kernel\_est, 8