# Package 'gam'

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**Description** Functions for fitting and working with generalized additive models, as described in chapter 7 of ``Statistical Models in S" (Chambers and Hastie (eds), 1991), and ``Generalized Additive Models" (Hastie and Tibshirani, 1990).

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gam-package

Generalized Additive Models

# Description

This package provides functions for fitting and working with generalized additive models as described in chapter 7 of "Statistical Models in S" (Chambers and Hastie (eds), 1991) and "Generalized Additive Models" (Hastie and Tibshirani, 1990).

# Author(s)

Trevor Hastie

anova.Gam

Analysis of Deviance for a Generalized Additive Model

# Description

Produces an ANODEV table for a set of GAM models, or else a summary for a single GAM model

#### Usage

```
## S3 method for class 'Gam'
anova(object, ..., test = c("Chisq", "F", "Cp"))
## S3 method for class 'Gam'
```

```
summary(object, dispersion = NULL, ...)
```

# Arguments

| object     | a fitted Gam   |
|------------|--|
|            | other fitted Gams for anova  |
| test       | a character string specifying the test statistic to be used. Can be one of '"F"', '"Chisq"' or '"Cp"', with partial matching allowed, or 'NULL' for no test. |
| dispersion | a dispersion parameter to be used in computing standard errors   |

# Details

These are methods for the functions anova or summary for objects inheriting from class Gam. See anova for the general behavior of this function and for the interpretation of test.

When called with a single Gam object, a special pair of anova tables for Gam models is returned. This gives a breakdown of the degrees of freedom for all the terms in the model, separating the projection part and nonparametric part of each, and returned as a list of two anova objects. For example, a term specified by s() is broken down into a single degree of freedom for its linear component, and the remainder for the nonparametric component. In addition, a type of score test is performed for each of the nonparametric terms. The nonparametric component is set to zero, and the linear part is updated, holding the other nonparametric terms fixed. This is done efficiently and simulataneously for all terms.

# Author(s)

Written by Trevor Hastie, following closely the design in the "Generalized Additive Models" chapter (Hastie, 1992) in Chambers and Hastie (1992).

#### References

Hastie, T. J. (1992) *Generalized additive models*. Chapter 7 of *Statistical Models in S* eds J. M. Chambers and T. J. Hastie, Wadsworth & Brooks/Cole.

Hastie, T. and Tibshirani, R. (1990) Generalized Additive Models. London: Chapman and Hall.

Venables, W. N. and Ripley, B. D. (2002) Modern Applied Statistics with S. New York: Springer.

# Examples

```
data(gam.data)
Gam.object <- gam(y~s(x,6)+z,data=gam.data)
anova(Gam.object)
Gam.object2 <- update(Gam.object, ~.-z)
anova(Gam.object, Gam.object2, test="Chisq")</pre>
```

gam

Fitting Generalized Additive Models

# Description

gam is used to fit generalized additive models, specified by giving a symbolic description of the additive predictor and a description of the error distribution. gam uses the *backfitting algorithm* to combine different smoothing or fitting methods. The methods currently supported are local regression and smoothing splines.

#### gam

# Usage

```
gam(
  formula,
  family = gaussian,
 data,
 weights,
  subset,
 na.action,
 start = NULL,
 etastart,
 mustart,
 control = gam.control(...),
 model = TRUE,
 method = "glm.fit",
 x = FALSE,
 y = TRUE,
  . . .
)
gam.fit(
 х,
 у,
  smooth.frame,
 weights = rep(1, nobs),
 start = NULL,
 etastart = NULL,
 mustart = NULL,
 offset = rep(0, nobs),
 family = gaussian(),
  control = gam.control()
)
```

# Arguments

| formula | a formula expression as for other regression models, of the form response ~ predictors. See the documentation of 1m and formula for details. Built-in nonparametric smoothing terms are indicated by s for smoothing splines or 1o for loess smooth terms. See the documentation for s and 1o for their arguments. Additional smoothers can be added by creating the appropriate interface functions. Interactions with nonparametric smooth terms are not fully supported, but will not produce errors; they will simply produce the usual parametric interaction. |
|---------|---|
| family  | a description of the error distribution and link function to be used in the model.<br>This can be a character string naming a family function, a family function or the<br>result of a call to a family function. (See family for details of family functions.)   |
| data    | an optional data frame containing the variables in the model. If not found in data, the variables are taken from environment(formula), typically the environment from which gam is called.  |

| weights      | an optional vector of weights to be used in the fitting process.  |
|--------------|---|
| subset       | an optional vector specifying a subset of observations to be used in the fitting process.   |
| na.action    | a function which indicates what should happen when the data contain NAs. The default is set by the na.action setting of options, and is na.fail if that is unset. The "factory-fresh" default is na.omit. A special method na.gam.replace allows for mean-imputation of missing values (assumes missing at random), and works gracefully with gam |
| start        | starting values for the parameters in the additive predictor.   |
| etastart     | starting values for the additive predictor.   |
| mustart      | starting values for the vector of means.  |
| control      | a list of parameters for controlling the fitting process. See the documentation for gam.control for details. These can also be set as arguments to gam() itself.  |
| model        | a logical value indicating whether <i>model frame</i> should be included as a compo-<br>nent of the returned value. Needed if gam is called and predicted from inside a<br>user function. Default is TRUE.  |
| method       | the method to be used in fitting the parametric part of the model. The default method "glm.fit" uses iteratively reweighted least squares (IWLS). The only current alternative is "model.frame" which returns the model frame and does no fitting.  |
| х, у         | For gam: logical values indicating whether the response vector and model matrix<br>used in the fitting process should be returned as components of the returned<br>value.   |
|              | For gam.fit: x is a model matrix of dimension $n * p$ , and y is a vector of observations of length n.  |
|              | further arguments passed to or from other methods.  |
| smooth.frame | for gam. fit only. This is essentially a subset of the model frame corresponding<br>to the smooth terms, and has the ingredients needed for smoothing each variable<br>in the backfitting algorithm. The elements of this frame are produced by the<br>formula functions lo and s.  |
| offset       | this can be used to specify an <i>a priori</i> known component to be included in the additive predictor during fitting.   |

# Details

The gam model is fit using the local scoring algorithm, which iteratively fits weighted additive models by backfitting. The backfitting algorithm is a Gauss-Seidel method for fitting additive models, by iteratively smoothing partial residuals. The algorithm separates the parametric from the non-parametric part of the fit, and fits the parametric part using weighted linear least squares within the backfitting algorithm. This version of gam remains faithful to the philosophy of GAM models as outlined in the references below.

An object gam.slist (currently set to c("lo", "s", "random")) lists the smoothers supported by gam. Corresponding to each of these is a smoothing function gam.lo, gam.s etc that take particular arguments and produce particular output, custom built to serve as building blocks in the backfitting algorithm. This allows users to add their own smoothing methods. See the documentation for these

methods for further information. In addition, the object gam.wlist (currently set to c("s", "lo")) lists the smoothers for which efficient backfitters are provided. These are invoked if all the smoothing methods are of one kind (either all "lo" or all "s").

# Value

gam returns an object of class Gam, which inherits from both glm and lm.

Gam objects can be examined by print, summary, plot, and anova. Components can be extracted using extractor functions predict, fitted, residuals, deviance, formula, and family. Can be modified using update. It has all the components of a glm object, with a few more. This also means it can be queried, summarized etc by methods for glm and lm objects. Other generic functions that have methods for Gam objects are step and preplot.

The following components must be included in a legitimate 'Gam' object. The residuals, fitted values, coefficients and effects should be extracted by the generic functions of the same name, rather than by the "\$" operator. The family function returns the entire family object used in the fitting, and deviance can be used to extract the deviance of the fit.

coefficients the coefficients of the parametric part of the additive.predictors, which multiply the columns of the model matrix. The names of the coefficients are the names of the single-degree-of-freedom effects (the columns of the model matrix). If the model is overdetermined there will be missing values in the coefficients corresponding to inestimable coefficients.

additive.predictors

the additive fit, given by the product of the model matrix and the coefficients, plus the columns of the \$smooth component.

- fitted.values the fitted mean values, obtained by transforming the component additive.predictors using the inverse link function.
- smooth, nl.df, nl.chisq, var

these four characterize the nonparametric aspect of the fit. smooth is a matrix of smooth terms, with a column corresponding to each smooth term in the model; if no smooth terms are in the Gam model, all these components will be missing. Each column corresponds to the strictly nonparametric part of the term, while the parametric part is obtained from the model matrix. nl.df is a vector giving the approximate degrees of freedom for each column of smooth. For smoothing splines specified by s(x), the approximate df will be the trace of the implicit smoother matrix minus 2. nl.chisq is a vector containing a type of score test for the removal of each of the columns of smooth. var is a matrix like smooth, containing the approximate pointwise variances for the columns of smooth.

- smooth.frame This is essentially a subset of the model frame corresponding to the smooth terms, and has the ingredients needed for making predictions from a Gam object
- residuals the residuals from the final weighted additive fit; also known as residuals, these are typically not interpretable without rescaling by the weights.
- deviance up to a constant, minus twice the maximized log-likelihood. Similar to the residual sum of squares. Where sensible, the constant is chosen so that a saturated model has deviance zero.
- null.deviance The deviance for the null model, comparable with deviance. The null model will include the offset, and an intercept if there is one in the model

| iter          | the number of local scoring iterations used to compute the estimates.  |
|---------------|--|
| bf.iter       | a vector of length iter giving number of backfitting iterations used at each inner loop.   |
| family        | a three-element character vector giving the name of the family, the link, and the variance function; mainly for printing purposes. |
| weights       | the <i>working</i> weights, that is the weights in the final iteration of the local scoring fit.                                   |
| prior.weights | the case weights initially supplied.   |
| df.residual   | the residual degrees of freedom.   |
| df.null       | the residual degrees of freedom for the null model.  |

The object will also have the components of a lm object: coefficients, residuals, fitted.values, call, terms, and some others involving the numerical fit. See lm.object.

#### Author(s)

Written by Trevor Hastie, following closely the design in the "Generalized Additive Models" chapter (Hastie, 1992) in Chambers and Hastie (1992), and the philosophy in Hastie and Tibshirani (1991). This version of gam is adapted from the S version to match the glm and lm functions in R.

Note that this version of gam is different from the function with the same name in the R library mgcv, which uses only smoothing splines with a focus on automatic smoothing parameter selection via GCV. To avoid issues with S3 method handling when both packages are loaded, the object class in package "gam" is now "Gam".

#### References

Hastie, T. J. (1991) *Generalized additive models*. Chapter 7 of *Statistical Models in S* eds J. M. Chambers and T. J. Hastie, Wadsworth & Brooks/Cole.

Hastie, T. and Tibshirani, R. (1990) *Generalized Additive Models*. London: Chapman and Hall. Venables, W. N. and Ripley, B. D. (2002) *Modern Applied Statistics with S*. New York: Springer.

# See Also

glm, family, lm.

# Examples

```
data(kyphosis)
gam(Kyphosis ~ s(Age,4) + Number, family = binomial, data=kyphosis,
trace=TRUE)
data(airquality)
gam(Ozone^(1/3) ~ lo(Solar.R) + lo(Wind, Temp), data=airquality, na=na.gam.replace)
gam(Kyphosis ~ poly(Age,2) + s(Start), data=kyphosis, family=binomial, subset=Number>2)
data(gam.data)
Gam.object <- gam(y ~ s(x,6) + z,data=gam.data)
summary(Gam.object)
plot(Gam.object,se=TRUE)
data(gam.newdata)</pre>
```

predict(Gam.object,type="terms",newdata=gam.newdata)

gam.control

Auxilliary for controlling GAM fitting

# Description

Auxiliary function as user interface for 'gam' fitting. Typically only used when calling 'gam' or 'gam.fit'.

# Usage

```
gam.control(
 epsilon = 1e-07,
 bf.epsilon = 1e-07,
 maxit = 30,
 bf.maxit = 30,
 trace = FALSE,
 ...
)
```

## Arguments

| epsilon    | convergence threshold for local scoring iterations                  |
|------------|---|
| bf.epsilon | convergence threshold for backfitting iterations                    |
| maxit      | maximum number of local scoring iterations                          |
| bf.maxit   | maximum number of backfitting iterations                            |
| trace      | should iteration details be printed while gam is fitting the model. |
|            | placemark for additional arguments                                  |

#### Value

a list is returned, consisting of the five parameters, conveniently packaged up to supply the control argument to gam. The values for gam.control can be supplied directly in a call to gam; these are then filtered through gam.control inside gam.

#### References

Hastie, T. J. (1992) *Generalized additive models*. Chapter 7 of *Statistical Models in S* eds J. M. Chambers and T. J. Hastie, Wadsworth & Brooks/Cole.

## Examples

```
## Not run: gam(formula, family, control = gam.control(bf.maxit=15))
## Not run: gam(formula, family, bf.maxit = 15) # these are equivalent
```

gam.data

# Description

A simple simulated dataset, used to test out the gam functions

## Format

A data frame with 100 observations on the following 6 variables:

x a numeric vector - predictor

y a numeric vector - the response

z a numeric vector - noise predictor

 ${\bf f}\,$  a numeric vector - true function

probf a numeric vector - probability function

ybin a numeric vector - binary response

# Details

This dataset is artificial, and is used to test out some of the features of gam.

# Examples

data(gam.data) gam(y  $\sim$  s(x) + z, data=gam.data)

| gam.exact | A method for gam producing asymptotically exact standard errors for |
|-----------|---|
|           | linear estimates  |

# Description

This function is a "wrapper" for a Gam object, and produces exact standard errors for each linear term in the gam call (except for the intercept).

# Usage

gam.exact(Gam.obj)

# Arguments

Gam.obj a Gam object

## Details

Only standard errors for the linear terms are produced. There is a print method for the Gamex class.

# Value

A list (of class Gamex) containing a table of coefficients and a variance covariance matrix for the linear terms in the formula of the gam call.

## Author(s)

Aidan McDermott, Department of Biostatistics, Johns Hopkins University. Modified by Trevor Hastie for R

# References

Issues in Semiparametric Regression: A Case Study of Time Series Models in Air Pollution and Mortality, Dominici F., McDermott A., Hastie T.J., *JASA*, December 2004, 99(468), 938-948. See https://hastie.su.domains/Papers/dominiciR2.pdf

#### Examples

```
set.seed(31)
n
      <- 200
      <- rnorm(n)
х
      <- rnorm(n)
у
а
      <- rep(1:10,length=n)
b
      <- rnorm(n)
    <- 1.4 + 2.1*a + 1.2*b + 0.2*sin(x/(3*max(x))) + 0.3*cos(y/(5*max(y))) + 0.5 * rnorm(n)
z
dat <- data.frame(x,y,a,b,z,testit=b*2)</pre>
### Model 1: Basic
Gam.o \leq gam(z \sim a + b + s(x,3) + s(y,5)), data=dat)
coefficients(summary.glm(Gam.o))
gam.exact(Gam.o)
### Model 2: Poisson
Gam.o \le gam(round(abs(z)) \ge a + b + s(x,3) + s(y,5), data=dat,family=poisson)
coefficients(summary.glm(Gam.o))
gam.exact(Gam.o)
```

```
gam.lo
```

Specify a loess fit in a GAM formula

# Description

A symbolic wrapper to indicate a smooth term in a formala argument to gam

# gam.lo

# Usage

```
gam.lo(
    x,
    y,
    w = rep(1, length(y)),
    span = 0.5,
    degree = 1,
    ncols = p,
    xeval = x
)
lo(..., span = 0.5, degree = 1)
```

# Arguments

| x      | for gam. lo, the appropriate basis of polynomials generated from the arguments to lo. These are also the variables that receive linear coefficients in the GAM fit.   |
|--------|---|
| У      | a response variable passed to gam. lo during backfitting  |
| W      | weights   |
| span   | the number of observations in a neighborhood. This is the smoothing parameter for a loess fit. If specified, the full argument name span must be written.   |
| degree | the degree of local polynomial to be fit; currently restricted to be 1 or 2. If specified, the full argument name degree must be written.   |
| ncols  | for gam.lo the number of columns in x used as the smoothing inputs to local regression. For example, if degree=2, then x has two columns defining a degree-2 polynomial basis. Both are needed for the parameteric part of the fit, but ncol=1 telling the local regression routine that the first column is the actually smoothing variable. |
| xeval  | If this argument is present, then gam.lo produces a prediction at xeval.  |
|        | the unspecified{} can be a comma-separated list of numeric vectors, numeric matrix, or expressions that evaluate to either of these. If it is a list of vectors, they must all have the same length.  |

# Details

A smoother in gam separates out the parametric part of the fit from the non-parametric part. For local regression, the parametric part of the fit is specified by the particular polynomial being fit locally. The workhorse function gam. lo fits the local polynomial, then strips off this parametric part. All the parametric pieces from all the terms in the additive model are fit simultaneously in one operation for each loop of the backfitting algorithm.

## Value

lo returns a numeric matrix. The simplest case is when there is a single argument to lo and degree=1; a one-column matrix is returned, consisting of a normalized version of the vector. If

degree=2 in this case, a two-column matrix is returned, consisting of a degree-2 polynomial basis. Similarly, if there are two arguments, or the single argument is a two-column matrix, either a two-column matrix is returned if degree=1, or a five-column matrix consisting of powers and products up to degree 2. Any dimensional argument is allowed, but typically one or two vectors are used in practice.

The matrix is endowed with a number of attributes; the matrix itself is used in the construction of the model matrix, while the attributes are needed for the backfitting algorithms general.wam (weighted additive model) or lo.wam (currently not implemented). Local-linear curve or surface fits reproduce linear responses, while local-quadratic fits reproduce quadratic curves or surfaces. These parts of the loess fit are computed exactly together with the other parametric linear parts

When two or more smoothing variables are given, the user should make sure they are in a commensurable scale; lo() does no normalization. This can make a difference, since lo() uses a spherical (isotropic) neighborhood when establishing the nearest neighbors.

Note that lo itself does no smoothing; it simply sets things up for gam; gam.lo does the actual smoothing. of the model.

One important attribute is named call. For example, lo(x) has a call component gam.lo(data[["lo(x)"]], z, w, span = 0.5, degree = 1, ncols = 1). This is an expression that gets evaluated repeatedly in general.wam (the backfitting algorithm).

gam. lo returns an object with components

| residuals | The residuals from the smooth fit. Note that the smoother removes the parametric part of the fit (using a linear fit with the columns in $x$ ), so these residual represent the nonlinear part of the fit. |
|-----------|--|
| nl.df     | the nonlinear degrees of freedom   |
| var       | the pointwise variance for the nonlinear fit   |

When gam. lo is evaluated with an xeval argument, it returns a matrix of predictions.

#### Author(s)

Written by Trevor Hastie, following closely the design in the "Generalized Additive Models" chapter (Hastie, 1992) in Chambers and Hastie (1992).

# References

Hastie, T. J. (1992) *Generalized additive models*. Chapter 7 of *Statistical Models in S* eds J. M. Chambers and T. J. Hastie, Wadsworth & Brooks/Cole.

Hastie, T. and Tibshirani, R. (1990) Generalized Additive Models. London: Chapman and Hall.

# See Also

s, bs, ns, poly, loess

## gam.random

## Examples

y ~ Age + lo(Start)
 # fit Start using a loess smooth with a (default) span of 0.5.
y ~ lo(Age) + lo(Start, Number)
y ~ lo(Age, span=0.3) # the argument name span cannot be abbreviated.

```
gam.random
```

Specify a Random Effects Fit in a GAM Formula

# Description

A symbolic wrapper for a factor term, to specify a random effect term in a formula argument to gam

## Usage

```
gam.random(f, y, w, df = sum(non.zero), lambda = 0, intercept = TRUE, xeval)
random(f, df = NULL, lambda = 0, intercept = TRUE)
```

# Arguments

| f         | factor variable, or expression that evaluates to a factor.   |
|-----------|--|
| У         | a response variable passed to gam. random during backfitting   |
| W         | weights  |
| df        | the target equivalent degrees of freedom, used as a smoothing parameter. The real smoothing parameter (lambda below) is found such that $df=tr(S)$ , where S is the implicit smoother matrix. Values for df should be greater than 0 and less than the number of levels of f. If both df and lambda are supplied, the latter takes precedence. Note that df is not necessarily an integer. |
| lambda    | the non-negative penalty parameter. This is interpreted as a variance ratio in a mixed effects model - namely the ratio of the noise variance to the random-effect variance.   |
| intercept | if intercept=TRUE (the default) then the estimated level effects are centered to average zero, otherwise they are left alone.  |
| xeval     | If this argument is present, then gam.random produces a prediction at xeval.   |

## Details

This "smoother" takes a factor as input and returns a shrunken-mean fit. If lambda=0, it simply computes the mean of the response at each level of f. With lambda>0, it returns a shrunken mean, where the j'th level is shrunk by nj/(nj+lambda), with nj being the number of observations (or sum of their weights) at level j. Using such smoother(s) in gam is formally equivalent to fitting a mixed-effect model by generalized least squares.

## Value

random returns the vector f, endowed with a number of attributes. The vector itself is used in computing the means in backfitting, while the attributes are needed for the backfitting algorithms general.wam. Note that random itself does no smoothing; it simply sets things up for gam.

One important attribute is named call. For example, random(f,lambda=2) has a call component gam.random(data[["random(f, lambda = 2)"]], z, w, df = NULL, lambda = 2, intercept = TRUE). This is an expression that gets evaluated repeatedly in general.wam (the backfitting algorithm).

gam. random returns an object with components

| residuals | The residuals from the smooth fit.  |
|-----------|-------------------------------------|
| nl.df     | the degrees of freedom              |
| var       | the pointwise variance for the fit  |
| lambda    | the value of lambda used in the fit |

When gam. random is evaluated with an xeval argument, it returns a vector of predictions.

# Author(s)

Written by Trevor Hastie, following closely the design in the "Generalized Additive Models" chapter (Hastie, 1992) in Chambers and Hastie (1992).

#### References

Hastie, T. J. (1992) *Generalized additive models*. Chapter 7 of *Statistical Models in S* eds J. M. Chambers and T. J. Hastie, Wadsworth & Brooks/Cole.

Hastie, T. and Tibshirani, R. (1990) Generalized Additive Models. London: Chapman and Hall.

Cantoni, E. and hastie, T. (2002) Degrees-of-freedom tests for smoothing splines, *Biometrika* 89(2), 251-263

# See Also

lo, s, bs, ns, poly

# Examples

# fit a model with a linear term in Age and a random effect in the factor Level y  $\sim$  Age + random(Level, lambda=1)

gam.s

## Description

A symbolic wrapper to indicate a smooth term in a formala argument to gam

#### Usage

```
gam.s(x, y, w = rep(1, length(x)), df = 4, spar = 1, xeval)
```

s(x, df = 4, spar = 1)

# Arguments

| х     | the univariate predictor, or expression, that evaluates to a numeric vector.  |
|-------|---|
| У     | a response variable passed to gam. s during backfitting   |
| W     | weights   |
| df    | the target equivalent degrees of freedom, used as a smoothing parameter. The real smoothing parameter (spar below) is found such that $df=tr(S)-1$ , where S is the implicit smoother matrix. Values for df should be greater than 1, with df=1 implying a linear fit. If both df and spar are supplied, the former takes precedence. Note that df is not necessarily an integer. |
| spar  | can be used as smoothing parameter, with values typically in $(0,1]$ . See smooth.spline for more details.  |
| xeval | If this argument is present, then gam.s produces a prediction at xeval.   |

# Value

s returns the vector x, endowed with a number of attributes. The vector itself is used in the construction of the model matrix, while the attributes are needed for the backfitting algorithms general.wam (weighted additive model) or s.wam. Since smoothing splines reproduces linear fits, the linear part will be efficiently computed with the other parametric linear parts of the model.

Note that s itself does no smoothing; it simply sets things up for gam.

One important attribute is named call. For example, s(x) has a call component gam. s(data[["s(x)"]], z, w, spar = 1, df = 4). This is an expression that gets evaluated repeatedly in general.wam (the backfitting algorithm).

gam. s returns an object with components

| residuals | The residuals from the smooth fit. Note that the smoother removes the paramet-<br>ric part of the fit (using a linear fit in $x$ ), so these residual represent the nonlinear<br>part of the fit. |
|-----------|---|
| nl.df     | the nonlinear degrees of freedom  |
| var       | the pointwise variance for the nonlinear fit  |

When gam.s is evaluated with an xeval argument, it returns a vector of predictions.

# Author(s)

Written by Trevor Hastie, following closely the design in the "Generalized Additive Models" chapter (Hastie, 1992) in Chambers and Hastie (1992).

## References

Hastie, T. J. (1992) *Generalized additive models*. Chapter 7 of *Statistical Models in S* eds J. M. Chambers and T. J. Hastie, Wadsworth & Brooks/Cole.

Hastie, T. and Tibshirani, R. (1990) *Generalized Additive Models*. London: Chapman and Hall. Cantoni, E. and hastie, T. (2002) Degrees-of-freedom tests for smoothing splines, *Biometrika* 89(2), 251-263

# See Also

lo, smooth.spline, bs, ns, poly

# Examples

```
# fit Start using a smoothing spline with 4 df.
y ~ Age + s(Start, 4)
# fit log(Start) using a smoothing spline with 5 df.
y ~ Age + s(log(Start), df=5)
```

gam.scope

Generate a scope for step.Gam

#### Description

Given a data.frame as an argument, generate a scope list for use in step.Gam, each element of which gives the candidates for that term.

## Usage

gam.scope(frame, response = 1, smoother = "s", arg = NULL, form = TRUE)

#### Arguments

| frame    | a data.frame to be used in step.Gam. Apart from the response column, all other columns will be used.  |
|----------|---|
| response | The column in frame used as the response. Default is 1.   |
| smoother | which smoother to use for the nonlinear terms; i.e. "s" or "lo", or any other supplied smoother. Default is "s".  |
| arg      | a character (vector), which is the argument to smoother. For example, $arg="df=6"$ would result in the expression $s(x, df=6)$ for a column named "x". This can be a vector, for example $arg=c("df=4", "df=6")$ , which would result two smooth terms. |
| form     | if TRUE, each term is a formula, else a character vector.   |

#### gam.smoothers

## Details

This function creates a similar scope formula for each variable in the frame. A column named "x" by default will generate a scope term  $\sim 1+x+s(x)$ . With  $\arg = c("df=4", "df=6")$  we get  $\sim 1+x+s(x, df=4)+s(x, df=6)$ . With form=FALSE, we would get the character vector c("1", "x", "s(x, df=4)", "s(x, df=6").

# Value

a scope list is returned, with either a formula or a character vector for each term, which describes the candidates for that term in the Gam.

#### Author(s)

Written by Trevor Hastie, following closely the design in the "Generalized Additive Models" chapter (Hastie, 1992) in Chambers and Hastie (1992). This version of gam. scope is adapted from the S version.

## References

Hastie, T. J. (1991) *Generalized additive models*. Chapter 7 of *Statistical Models in S* eds J. M. Chambers and T. J. Hastie, Wadsworth & Brooks/Cole.

# See Also

step.Gam

## Examples

```
data(gam.data)
gdata=gam.data[,1:3]
gam.scope(gdata,2)
gam.scope(gdata,2,arg="df=5")
gam.scope(gdata,2,arg="df=5",form=FALSE)
gam.scope(gdata,2,arg=c("df=4","df=6"))
```

gam. smoothers Smoothers available for backfitting

## Description

Auxiliary function as user interface for 'gam' fitting. Lists what smoothers are implemented, and allows users to include new smoothers.

# Usage

```
gam.smoothers(slist = c("s", "lo", "random"), wlist = c("s", "lo"))
```

## Arguments

| slist | character vector giving names of smoothers available for general backfitting. For every entry, eg "lo", there must exist a formula function "lo()" that prepares the data, and a fitting function with the name "gam.lo" which actually does the fitting. Look at "lo" and "s" as examples. |
|-------|---|
| wlist | character vector (subset of slist) giving names of smoothers for which a special backfitting algorithm is available, when only that smoother appears (multiple times) in the formula, along with other non smooth terms.  |

#### Value

a list is returned, consisting of the two named vectors. If the function is called with no arguments, it gets the version of "gam.smooth.list" in the search path, by default from the package name space. Once it is called with either of the arguments, it places a local copy in the users namespace.

## References

Hastie, T. J. (1992) *Generalized additive models*. Chapter 7 of *Statistical Models in S* eds J. M. Chambers and T. J. Hastie, Wadsworth & Brooks/Cole.

## Examples

## Not run: gam.smoothers()\$slist # get the gam.smooth.list, and extract component slist
## Not run: gam.smoothers(slist=c("s","lo","random","tps") # add a new smoother "tps" to the list

kyphosis

A classic example dataset for GAMs

## Description

Data on the results of a spinal operation "laminectomy" on children, to correct for a condition called "kyphosis"; see Hastie and Tibshirani (1990) for details

#### Usage

```
data(kyphosis)
```

# Format

A data frame with 81 observations on the following 4 variables.

**Kyphosis** a response factor with levels absent present.

Age of child in months, a numeric vector

Number of vertebra involved in the operation, a numeric vector

Start level of the operation, a numeric vector

#### na.gam.replace

#### Source

Hastie, T. and Tibshirani, R. (1990) Generalized Additive Models. London: Chapman and Hall.

na.gam.replace Missing Data Filter for GAMs

#### Description

A method for dealing with missing values, friendly to GAM models.

#### Usage

na.gam.replace(frame)

#### Arguments

frame a model or data frame

# Value

a model or data frame is returned, with the missing observations (NAs) replaced. The following rules are used. A factor with missing data is replaced by a new factor with one more level, labelled "NA", which records the missing data. Ordered factors are treated similarly, except the result is an unordered factor. A missing numeric vector has its missing entires replaced by the mean of the non-missing entries. Similarly, a matrix with missing entries has each missing entry replace by the mean of its column. If frame is a model frame, the response variable can be identified, as can the weights (if present). Any rows for which the response or weight is missing are removed entirely from the model frame.

The word "gam" in the name is relevant, because gam() makes special use of this filter. All columns of a model frame that were created by a call to lo() or s() have an attribute names "NAs" if NAs are present in their columns. Despite the replacement by means, these attributes remain on the object, and gam() takes appropriate action when smoothing against these columns. See section 7.3.2 in Hastie (1992) for more details.

## Author(s)

**Trevor Hastie** 

# References

Hastie, T. J. (1992) *Generalized additive models*. Chapter 7 of *Statistical Models in S* eds J. M. Chambers and T. J. Hastie, Wadsworth & Brooks/Cole.

# See Also

na.fail, na.omit, gam

# Examples

```
data(airquality)
gam(Ozone^(1/3) ~ lo(Solar.R) + lo(Wind, Temp), data=airquality, na=na.gam.replace)
```

plot.Gam

# Plot Components of a GAM Object

# Description

A plot method for GAM objects, which can be used on GLM and LM objects as well. It focuses on terms (main-effects), and produces a suitable plot for terms of different types

# Usage

```
## S3 method for class 'Gam'
plot(
    x,
    residuals = NULL,
    rugplot = TRUE,
    se = FALSE,
    scale = 0,
    ask = FALSE,
    terms = labels.Gam(x),
    ...
)
## S3 method for class 'Gam'
preplot(object, newdata, terms = labels.Gam(object), ...)
```

# Arguments

| X         | a Gam object, or a preplot.Gam object. The first thing plot.Gam() does is check if x has a component called preplot; if not, it computes one using preplot.Gam(). Either way, it is this preplot.Gam object that is required for plotting a Gam object.                               |
|-----------|---|
| residuals | if TRUE, partial deviance residuals are plotted along with the fitted terms—<br>default is FALSE. If residuals is a vector with the same length as each fitted<br>term in x, then these are taken to be the overall residuals to be used for con-<br>structing the partial residuals. |
| rugplot   | if TRUE (the default), a univariate histogram or rugplot is displayed along the base of each plot, showing the occurrence of each x; ties are broken by jittering.  |
| se        | if TRUE, upper and lower pointwise twice-standard-error curves are included for each plot. The default is FALSE.  |

## plot.Gam

| scale   | a lower limit for the number of units covered by the limits on the y for each plot.<br>The default is scale=0, in which case each plot uses the range of the functions<br>being plotted to create their ylim. By setting scale to be the maximum value of<br>diff(ylim) for all the plots, then all subsequent plots will produced in the same<br>vertical units. This is essential for comparing the importance of fitted terms in<br>additive models. |
|---------|---|
| ask     | if TRUE, plot.Gam() operates in interactive mode.   |
| terms   | subsets of the terms can be selected  |
|         | Additonal plotting arguments, not all of which will work (like xlim)  |
| object  | same as x   |
| newdata | if supplied to preplot.Gam, the preplot object is based on them rather than the original.   |

# Value

a plot is produced for each of the terms in the object x. The function currently knows how to plot all main-effect functions of one or two predictors. So in particular, interactions are not plotted. An appropriate x-y is produced to display each of the terms, adorned with residuals, standarderror curves, and a rugplot, depending on the choice of options. The form of the plot is different, depending on whether the x-value for each plot is numeric, a factor, or a matrix.

When ask=TRUE, rather than produce each plot sequentially, plot.Gam() displays a menu listing all the terms that can be plotted, as well as switches for all the options.

A preplot. Gam object is a list of precomputed terms. Each such term (also a preplot.Gam object) is a list with components x, y and others—the basic ingredients needed for each term plot. These are in turn handed to the specialized plotting function gplot(), which has methods for different classes of the leading x argument. In particular, a different plot is produced if x is numeric, a category or factor, a matrix, or a list. Experienced users can extend this range by creating more gplot() methods for other classes. Graphical parameters (see par) may also be supplied as arguments to this function. This function is a method for the generic function plot() for class "Gam".

It can be invoked by calling plot(x) for an object x of the appropriate class, or directly by calling plot.Gam(x) regardless of the class of the object.

## Author(s)

Written by Trevor Hastie, following closely the design in the "Generalized Additive Models" chapter (Hastie, 1992) in Chambers and Hastie (1992).

## References

Hastie, T. J. (1992) *Generalized additive models*. Chapter 7 of *Statistical Models in S* eds J. M. Chambers and T. J. Hastie, Wadsworth & Brooks/Cole.

Hastie, T. and Tibshirani, R. (1990) Generalized Additive Models. London: Chapman and Hall.

# See Also

preplot, predict.Gam

# Examples

```
data(gam.data)
Gam.object <- gam(y ~ s(x,6) + z,data=gam.data)
plot(Gam.object,se=TRUE)
data(gam.newdata)
preplot(Gam.object,newdata=gam.newdata)</pre>
```

predict.Gam

Predict method for GAM fits

# Description

Obtains predictions and optionally estimates standard errors of those predictions from a fitted generalized additive model object.

# Usage

```
## S3 method for class 'Gam'
predict(
   object,
   newdata,
   type = c("link", "response", "terms"),
   dispersion = NULL,
   se.fit = FALSE,
   na.action = na.pass,
   terms = labels(object),
   ...
)
```

## Arguments

| object     | a fitted Gam object, or one of its inheritants, such as a glm or lm object.   |
|------------|---|
| newdata    | a data frame containing the values at which predictions are required. This ar-<br>gument can be missing, in which case predictions are made at the same values<br>used to compute the object. Only those predictors, referred to in the right side<br>of the formula in object need be present by name in newdata.  |
| type       | type of predictions, with choices "link" (the default), "response", or "terms".<br>The default produces predictions on the scale of the additive predictors, and with<br>newdata missing, predict is simply an extractor function for this component<br>of a Gam object. If "response" is selected, the predictions are on the scale of<br>the response, and are monotone transformations of the additive predictors, using<br>the inverse link function. If type="terms" is selected, a matrix of predictions<br>is produced, one column for each term in the model. |
| dispersion | the dispersion of the GLM fit to be assumed in computing the standard errors.<br>If omitted, that returned by 'summary' applied to the object is used   |

#### predict.Gam

| se.fit    | if TRUE, pointwise standard errors are computed along with the predictions.  |
|-----------|--|
| na.action | function determining what should be done with missing values in 'newdata'. The default is to predict 'NA'.                 |
| terms     | if type="terms", the terms= argument can be used to specify which terms should be included; the default is labels(object). |
|           | Placemark for additional arguments to predict  |

#### Value

a vector or matrix of predictions, or a list consisting of the predictions and their standard errors if se.fit = TRUE. If type="terms", a matrix of fitted terms is produced, with one column for each term in the model (or subset of these if the terms= argument is used). There is no column for the intercept, if present in the model, and each of the terms is centered so that their average over the original data is zero. The matrix of fitted terms has a "constant" attribute which, when added to the sum of these centered terms, gives the additive predictor. See the documentation of predict for more details on the components returned.

When newdata are supplied, predict.Gam simply invokes inheritance and gets predict.glm to produce the parametric part of the predictions. For each nonparametric term, predict.Gam reconstructs the partial residuals and weights from the final iteration of the local scoring algorithm. The appropriate smoother is called for each term, with the appropriate xeval argument (see s or lo), and the prediction for that term is produced.

The standard errors are based on an approximation given in Hastie (1992). Currently predict.Gam does not produce standard errors for predictions at newdata.

Warning: naive use of the generic predict can produce incorrect predictions when the newdata argument is used, if the formula in object involves transformations such as sqrt(Age - min(Age)).

## Author(s)

Written by Trevor Hastie, following closely the design in the "Generalized Additive Models" chapter (Hastie, 1992) in Chambers and Hastie (1992). This version of predict.Gam is adapted from the S version to match the corresponding predict methods for glm and lm objects in R. The safe.predict.Gam function in S is no longer required, primarily because a safe prediction method is in place for functions like ns, bs, and poly.

#### References

Hastie, T. J. (1992) *Generalized additive models*. Chapter 7 of *Statistical Models in S* eds J. M. Chambers and T. J. Hastie, Wadsworth & Brooks/Cole.

Hastie, T. and Tibshirani, R. (1990) Generalized Additive Models. London: Chapman and Hall.

Venables, W. N. and Ripley, B. D. (2002) Modern Applied Statistics with S. New York: Springer.

# See Also

predict.glm, fitted, expand.grid

# Examples

```
data(gam.data)
Gam.object <- gam(y \sim s(x, 6) + z, data=gam.data)
predict(Gam.object) # extract the additive predictors
data(gam.newdata)
predict(Gam.object, gam.newdata, type="terms")
```

```
step.Gam
```

Stepwise model builder for GAM

## Description

Builds a GAM model in a step-wise fashion. For each "term" there is an ordered list of alternatives, and the function traverses these in a greedy fashion. Note: this is NOT a method for step, which used to be a generic, so must be invoked with the full name.

# Usage

```
step.Gam(
  object,
  scope,
  scale,
  direction = c("both", "backward", "forward"),
  trace = TRUE,
  keep = NULL,
  steps = 1000,
  parallel = FALSE,
  . . .
)
```

# Arguments

| object | An object of class Gam or any of it's inheritants.                              |
|--------|---|
| scope  | defines the range of models examined in the step-wise search. It is a list of   |
|        | formulas, with each formula corresponding to a term in the model. Each of       |
|        | these formulas specifies a "regimen" of candidate forms in which the particular |

e model. Each of hich the particular term may enter the model. For example, a term formula might be ~1+ Income  $+ \log(\text{Income}) + s(\text{Income})$ . This means that Income could either appear not at all, linearly, linearly in its logarithm, or as a smooth function estimated nonparametrically. A 1 in the formula allows the additional option of leaving the term out of the model entirely. Every term in the model is described by such a term formula, and the final model is built up by selecting a component from each formula.

As an alternative more convenient for big models, each list can have instead of a formula a character vector corresponding to the candidates for that term. Thus we could have c("1", "x", "s(x, df=5") rather than  $\sim 1+x+s(x, df=5)$ .

|           | The supplied model object is used as the starting model, and hence there is<br>the requirement that one term from each of the term formulas be present in<br>formula(object). This also implies that any terms in formula(object) <i>not</i><br>contained in any of the term formulas will be forced to be present in every model<br>considered. The function gam.scope is helpful for generating the scope argu-<br>ment for a large model. |
|-----------|--|
| scale     | an optional argument used in the definition of the AIC statistic used to evaluate<br>models for selection. By default, the scaled Chi-squared statistic for the initial<br>model is used, but if forward selection is to be performed, this is not necessarily<br>a sound choice.  |
| direction | The mode of step-wise search, can be one of "both", "backward", or "forward", with a default of "both". If scope is missing, the default for direction is "both".  |
| trace     | If TRUE (the default), information is printed during the running of step.Gam(). This is an encouraging choice in general, since step.Gam() can take some time to compute either for large models or when called with an an extensive scope= argument. A simple one line model summary is printed for each model selected. This argument can also be given as the binary 0 or 1. A value trace=2 gives a more verbose trace.                  |
| keep      | A filter function whose input is a fitted Gam object, and anything else passed via, and whose output is arbitrary. Typically keep() will select a subset of the components of the object and return them. The default is not to keep anything.   |
| steps     | The maximum number of steps to be considered. The default is 1000 (essentially as many as required). It is typically used to stop the process early.   |
| parallel  | If TRUE, use parallel foreach to fit each trial run. Must register parallel before hand, such as doMC or others. See the example below.  |
|           | Additional arguments to be passed on to keep   |

# Value

The step-wise-selected model is returned, with up to two additional components. There is an "anova" component corresponding to the steps taken in the search, as well as a "keep" component if the keep= argument was supplied in the call.

We describe the most general setup, when direction = "both". At any stage there is a current model comprising a single term from each of the term formulas supplied in the scope= argument. A series of models is fitted, each corrresponding to a formula obtained by moving each of the terms one step up or down in its regimen, relative to the formula of the current model. If the current value for any term is at either of the extreme ends of its regimen, only one rather than two steps can be considered. So if there are p term formulas, at most 2\*p - 1 models are considered. A record is kept of all the models ever visited (hence the -1 above), to avoid repetition. Once each of these models has been fit, the "best" model in terms of the AIC statistic is selected and defines the step. The entire process is repeated until either the maximum number of steps has been used, or until the AIC criterion can not be decreased by any of the eligible steps.

#### Author(s)

Written by Trevor Hastie, following closely the design in the "Generalized Additive Models" chapter (Hastie, 1992) in Chambers and Hastie (1992).

# References

Hastie, T. J. (1992) *Generalized additive models*. Chapter 7 of *Statistical Models in S* eds J. M. Chambers and T. J. Hastie, Wadsworth & Brooks/Cole.

Hastie, T. and Tibshirani, R. (1990) Generalized Additive Models. London: Chapman and Hall.

# See Also

gam.scope,step,glm,gam,drop1,add1,anova.Gam

# Examples

```
data(gam.data)
Gam.object <- gam(y~x+z, data=gam.data)
step.object <-step.Gam(Gam.object, scope=list("x"=~1+x+s(x,4)+s(x,6)+s(x,12),"z"=~1+z+s(z,4)))
## Not run:
# Parallel
require(doMC)
registerDoMC(cores=2)
step.Gam(Gam.object, scope=list("x"=~1+x+s(x,4)+s(x,6)+s(x,12),"z"=~1+z+s(z,4)),parallel=TRUE)
```

## End(Not run)

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