# Package 'fcaR'

November 30, 2023

Title Formal Concept Analysis

Version 1.2.2

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**Description** Provides tools to perform fuzzy formal concept

analysis, presented in Wille (1982) <doi:10.1007/978-3-642-01815-2\_23> and in Ganter and Obiedkov (2016) <doi:10.1007/978-3-662-49291-8>. It provides functions to load and save a formal context, extract its concept lattice and implications. In addition, one can use the implications to compute semantic closures of fuzzy sets and, thus, build recommendation systems.

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URL https://github.com/Malaga-FCA-group/fcaR

BugReports https://github.com/Malaga-FCA-group/fcaR/issues

**Depends** R (>= 4.1)

**Imports** dplyr, forcats, fractional, ggplot2, glue, grDevices, Matrix, methods, POSetR, R6, rlang, Rcpp, registry, settings, stringr, tibble, tidyr, tikzDevice, magrittr, purrr

**Suggests** arules, covr, hasseDiagram, knitr, markdown, rmarkdown, testthat (>= 2.1.0), tictoc, tinytex, parallel

LinkingTo Rcpp

VignetteBuilder knitr

**Encoding** UTF-8

LazyData true

**RoxygenNote** 7.2.3.9000

NeedsCompilation yes

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# **R** topics documented:

as_Set	. 2
as_vector	. 3
cobre32	. 4
cobre61	. 5
Concept	. 6
ConceptLattice	. 7
ConceptSet	. 12
equivalencesRegistry	. 14
fcaR_options	. 15
FormalContext	. 15
ImplicationSet	. 25
parse_implication	. 31
parse_implications	. 31
planets	. 32
scalingRegistry	. 33
Set	. 33
vegas	. 36
% &%	. 36
%entails%	. 37
%==%	. 38
%-%	. 39
%holds_in%	. 39
~	. 40
%or%	. 41
%respects%	. 42
%~%	. 42
	44

# Index

as\_Set

Convert Named Vector to Set

# Description

Convert Named Vector to Set

# Usage

as\_Set(A)

# Arguments

А

A named vector or matrix to build a new Set.

# as\_vector

# Value

A Set object.

# Examples

 $A \le c(a = 0.1, b = 0.2, p = 0.3, q = 0)$ as\_Set(A)

as_vector	Convert Set to vector	
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# Description

Convert Set to vector

# Usage

as\_vector(v)

# Arguments

v A Set to convert to vector.

#### Value

A vector.

# Examples

A <- c(a = 0.1, b = 0.2, p = 0.3, q = 0) v <- as\_Set(A) A2 <- as\_vector(v) all(A == A2) cobre32

#### Description

A subset of the COBRE dataset has been retrieved, by querying SchizConnect for 105 patients with neurological and clinical symptoms, collecting also their corresponding diagnosis.

#### Usage

cobre32

# Format

A matrix with 105 rows and 32 columns. Column names are related to different scales for depression and Schizophrenia:

- **COSAS\_n** The *Simpson-Angus Scale*, 7 items to evaluate Parkinsonism-like alterations, related to schizophrenia, in an individual.
- **FICAL\_n** The Calgary Depression Scale for Schizophrenia, 9 items (attributes) assessing the level of depression in schizophrenia, differentiating between positive and negative aspects of the disease.
- SCIDII\_n The Structured Clinical Interview for DSM-III-R Personality Disorders, with 14 variables related to the presence of signs affecting personality.
- **dx\_ss** if TRUE, the diagnosis is strict schizophrenia.
- dx\_other it TRUE, the diagnosis is other than schizophrenia, including schizoaffective, bipolar disorder and major depression.

In summary, the dataset consists in the previous 30 attributes related to signs or symptoms, and 2 attributes related to diagnosis (these diagnoses are mutually exclusive, thus only one of them is assigned to each patient). This makes a dataset with 105 objects (patients) and 32 attributes to explore. The symptom attributes are multi-valued.

Thus, according to the specific scales used, all attributes are fuzzy and graded. For a given attribute (symptom), the available grades range from *absent* to *extreme*, with *minimal*, *mild*, *moderate*, *moderate severe* and *severe* in between.

These fuzzy attributes are mapped to values in the interval [0, 1].

#### Source

Aine, C. J., Bockholt, H. J., Bustillo, J. R., Cañive, J. M., Caprihan, A., Gasparovic, C., ... & Liu, J. (2017). Multimodal neuroimaging in schizophrenia: description and dissemination. Neuroinformatics, 15(4), 343-364. https://pubmed.ncbi.nlm.nih.gov/26142271/

cobre61

#### Description

A subset of the COBRE dataset has been retrieved, by querying SchizConnect for 105 patients with neurological and clinical symptoms, collecting also their corresponding diagnosis.

#### Usage

cobre61

# Format

A matrix with 105 rows and 61 columns. Column names are related to different scales for depression and Schizophrenia:

- **COSAS\_n** The *Simpson-Angus Scale*, 7 items to evaluate Parkinsonism-like alterations, related to schizophrenia, in an individual.
- **FIPAN\_n** The *Positive and Negative Syndrome Scale*, a set of 29 attributes measuring different aspects and symptoms in schizophrenia.
- **FICAL\_n** The *Calgary Depression Scale for Schizophrenia*, 9 items (attributes) assessing the level of depression in schizophrenia, differentiating between positive and negative aspects of the disease.
- SCIDII\_n The Structured Clinical Interview for DSM-III-R Personality Disorders, with 14 variables related to the presence of signs affecting personality.
- dx\_ss if TRUE, the diagnosis is strict schizophrenia.
- dx\_other it TRUE, the diagnosis is other than schizophrenia, including schizoaffective, bipolar disorder and major depression.

In summary, the dataset consists in the previous 59 attributes related to signs or symptoms, and 2 attributes related to diagnosis (these diagnoses are mutually exclusive, thus only one of them is assigned to each patient). This makes a dataset with 105 objects (patients) and 61 attributes to explore. The symptom attributes are multi-valued.

Thus, according to the specific scales used, all attributes are fuzzy and graded. For a given attribute (symptom), the available grades range from *absent* to *extreme*, with *minimal*, *mild*, *moderate*, *moderate severe* and *severe* in between.

These fuzzy attributes are mapped to values in the interval [0, 1].

#### Source

Aine, C. J., Bockholt, H. J., Bustillo, J. R., Cañive, J. M., Caprihan, A., Gasparovic, C., ... & Liu, J. (2017). Multimodal neuroimaging in schizophrenia: description and dissemination. Neuroinformatics, 15(4), 343-364. https://pubmed.ncbi.nlm.nih.gov/26142271/

#### Concept

#### Description

This class implements the data structure and methods for fuzzy concepts.

#### Methods

#### **Public methods:**

- Concept\$new()
- Concept\$get\_extent()
- Concept\$get\_intent()
- Concept\$print()
- Concept\$to\_latex()
- Concept\$clone()

#### Method new(): Creator for objects of class Concept

Usage: Concept\$new(extent, intent)

Arguments:

extent (Set) The extent of the concept.

intent (Set) The intent of the concept.

Returns: An object of class Concept.

#### Method get\_extent(): Internal Set for the extent

Usage:

Concept\$get\_extent()

Returns: The Set representation of the extent.

#### Method get\_intent(): Internal Set for the intent

Usage: Concept\$get\_intent()

Returns: The Set representation of the intent.

#### Method print(): Prints the concept to console

Usage: Concept\$print()

Returns: A string with the elements of the set and their grades between brackets .

#### Method to\_latex(): Write the concept in LaTeX format

Usage:

# ConceptLattice

Concept\$to\_latex(print = TRUE)
Arguments:
print (logical) Print to output?
Returns: The fuzzy concept in LaTeX.

Method clone(): The objects of this class are cloneable with this method.

Usage: Concept\$clone(deep = FALSE) Arguments: deep Whether to make a deep clone.

# Examples

```
# Build a formal context and find its concepts
fc_planets <- FormalContext$new(planets)
fc_planets$find_concepts()
```

```
# Print the first three concepts
fc_planets$concepts[1:3]
```

# Select the first concept: C <- fc\_planets\$concepts\$sub(1)</pre>

```
# Get its extent and intent
C$get_extent()
C$get_intent()
```

ConceptLattice R6 class for a concept lattice

# Description

This class implements the data structure and methods for concept lattices.

# Super class

fcaR::ConceptSet -> ConceptLattice

# Methods

#### **Public methods:**

- ConceptLattice\$new()
- ConceptLattice\$plot()
- ConceptLattice\$sublattice()
- ConceptLattice\$top()

- ConceptLattice\$bottom()
- ConceptLattice\$join\_irreducibles()
- ConceptLattice\$meet\_irreducibles()
- ConceptLattice\$decompose()
- ConceptLattice\$supremum()
- ConceptLattice\$infimum()
- ConceptLattice\$subconcepts()
- ConceptLattice\$superconcepts()
- ConceptLattice\$lower\_neighbours()
- ConceptLattice\$upper\_neighbours()
- ConceptLattice\$clone()

**Method** new(): Create a new ConceptLattice object.

#### Usage:

```
ConceptLattice$new(extents, intents, objects, attributes, I = NULL)
```

Arguments:

extents (dgCMatrix) The extents of all concepts

intents (dgCMatrix) The intents of all concepts

objects (character vector) Names of the objects in the formal context

attributes (character vector) Names of the attributes in the formal context

I (dgCMatrix) The matrix of the formal context

*Returns:* A new ConceptLattice object.

#### Method plot(): Plot the concept lattice

# Usage:

ConceptLattice\$plot(object\_names = TRUE, to\_latex = FALSE, ...)

Arguments:

object\_names (logical) If TRUE, plot object names, otherwise omit them from the diagram.

- to\_latex (logical) If TRUE, export the plot as a tikzpicture environment that can be included in a LaTeX file.
- ... Other parameters to be passed to the tikzDevice that renders the lattice in LaTeX, or for the figure caption. See Details.

*Details:* Particular parameters that control the size of the tikz output are: width, height (both in inches), and pointsize (in points), that should be set to the font size used in the documentclass header in the LaTeX file where the code is to be inserted.

If a caption is provided, the whole tikz picture will be wrapped by a figure environment and the caption set.

*Returns:* If to\_latex is FALSE, it returns nothing, just plots the graph of the concept lattice. Otherwise, this function returns the LaTeX code to reproduce the concept lattice.

Method sublattice(): Sublattice

Usage: ConceptLattice\$sublattice(...)

# ConceptLattice

Arguments:

... See Details.

*Details:* As argument, one can provide both integer indices or Concepts, separated by commas. The corresponding concepts are used to generate a sublattice.

Returns: The generated sublattice as a new ConceptLattice object.

Method top(): Top of a Lattice

Usage: ConceptLattice\$top() Returns: The top of the Concept Lattice Examples: fc <- FormalContext\$new(planets) fc\$find\_concepts() fc\$concepts\$top()

# Method bottom(): Bottom of a Lattice

Usage: ConceptLattice\$bottom() Returns: The bottom of the Concept Lattice Examples: fc <- FormalContext\$new(planets) fc\$find\_concepts() fc\$concepts\$bottom()

#### Method join\_irreducibles(): Join-irreducible Elements

Usage:

ConceptLattice\$join\_irreducibles()

Returns: The join-irreducible elements in the concept lattice.

Method meet\_irreducibles(): Meet-irreducible Elements

Usage:

ConceptLattice\$meet\_irreducibles()

*Returns:* The meet-irreducible elements in the concept lattice.

Method decompose(): Decompose a concept as the supremum of meet-irreducible concepts

Usage:

ConceptLattice\$decompose(C)

Arguments:

C A list of Concepts

*Returns:* A list, each field is the set of meet-irreducible elements whose supremum is the corresponding element in C.

Method supremum(): Supremum of Concepts

Usage:

ConceptLattice\$supremum(...)

Arguments:

... See Details.

*Details:* As argument, one can provide both integer indices or Concepts, separated by commas. The corresponding concepts are used to compute their supremum in the lattice.

Returns: The supremum of the list of concepts.

Method infimum(): Infimum of Concepts

Usage: ConceptLattice\$infimum(...)

Arguments:

... See Details.

*Details:* As argument, one can provide both integer indices or Concepts, separated by commas. The corresponding concepts are used to compute their infimum in the lattice.

Returns: The infimum of the list of concepts.

Method subconcepts(): Subconcepts of a Concept

Usage:

ConceptLattice\$subconcepts(C)

Arguments:

C (numeric or SparseConcept) The concept to which determine all its subconcepts.

Returns: A list with the subconcepts.

Method superconcepts(): Superconcepts of a Concept

Usage:

ConceptLattice\$superconcepts(C)

Arguments:

C (numeric or SparseConcept) The concept to which determine all its superconcepts.

Returns: A list with the superconcepts.

Method lower\_neighbours(): Lower Neighbours of a Concept

Usage:

ConceptLattice\$lower\_neighbours(C)

Arguments:

C (SparseConcept) The concept to which find its lower neighbours

Returns: A list with the lower neighbours of C.

**Method** upper\_neighbours(): Upper Neighbours of a Concept *Usage:* 

10

# ConceptLattice

ConceptLattice\$upper\_neighbours(C)

Arguments:

C (SparseConcept) The concept to which find its upper neighbours

Returns: A list with the upper neighbours of C.

Method clone(): The objects of this class are cloneable with this method.

Usage: ConceptLattice\$clone(deep = FALSE)

Arguments:

deep Whether to make a deep clone.

# Examples

```
# Build a formal context
fc_planets <- FormalContext$new(planets)</pre>
```

```
# Find the concepts
fc_planets$find_concepts()
```

```
# Find join- and meet- irreducible elements
fc_planets$concepts$join_irreducibles()
fc_planets$concepts$meet_irreducibles()
```

```
# Get concept support
fc_planets$concepts$support()
```

```
## -----
## Method `ConceptLattice$top`
## -----
```

```
fc <- FormalContext$new(planets)
fc$find_concepts()
fc$concepts$top()</pre>
```

```
## ------
## Method `ConceptLattice$bottom`
## ------
```

```
fc <- FormalContext$new(planets)
fc$find_concepts()
fc$concepts$bottom()</pre>
```

ConceptSet

#### Description

This class implements the data structure and methods for concept sets.

#### Methods

#### **Public methods:**

- ConceptSet\$new()
- ConceptSet\$size()
- ConceptSet\$is\_empty()
- ConceptSet\$extents()
- ConceptSet\$intents()
- ConceptSet\$print()
- ConceptSet\$to\_latex()
- ConceptSet\$to\_list()
- ConceptSet\$[()
- ConceptSet\$sub()
- ConceptSet\$support()
- ConceptSet\$clone()

#### Method new(): Create a new ConceptLattice object.

#### Usage:

ConceptSet\$new(extents, intents, objects, attributes, I = NULL)

Arguments:

extents (dgCMatrix) The extents of all concepts

intents (dgCMatrix) The intents of all concepts

objects (character vector) Names of the objects in the formal context

attributes (character vector) Names of the attributes in the formal context

I (dgCMatrix) The matrix of the formal context

Returns: A new ConceptLattice object.

#### Method size(): Size of the Lattice

# Usage: ConceptSet\$size()

Returns: The number of concepts in the lattice.

Method is\_empty(): Is the lattice empty?

Usage: ConceptSet\$is\_empty()

# ConceptSet

Returns: TRUE if the lattice has no concepts.

Method extents(): Concept Extents

Usage:

ConceptSet\$extents()

*Returns:* The extents of all concepts, as a dgCMatrix.

#### Method intents(): Concept Intents

Usage: ConceptSet\$intents() Returns: The intents of all concepts, as a dgCMatrix.

#### Method print(): Print the Concept Set

Usage: ConceptSet\$print() Returns: Nothing, just prints the concepts

**Method** to\_latex(): Write in LaTeX

Usage:

ConceptSet\$to\_latex(print = TRUE, ncols = 1, numbered = TRUE, align = TRUE)

Arguments:

print (logical) Print to output? ncols (integer) Number of columns of the output. numbered (logical) Number the concepts? align (logical) Align objects and attributes independently? Returns: The LaTeX code to list all concepts.

Method to\_list(): Returns a list with all the concepts

Usage: ConceptSet\$to\_list() Returns: A list of concepts.

Method [(): Subsets a ConceptSet

Usage:

ConceptSet\$[(indices)

Arguments:

indices (numeric or logical vector) The indices of the concepts to return as a list of Concepts. It can be a vector of logicals where TRUE elements are to be retained.

Returns: Another ConceptSet.

Method sub(): Individual Concepts

Usage: ConceptSet\$sub(index) Arguments: index (numeric) The index of the concept to return. *Returns:* The Concept.

Method support(): Get support of each concept

Usage: ConceptSet\$support() *Returns:* A vector with the support of each concept.

Method clone(): The objects of this class are cloneable with this method.

Usage: ConceptSet\$clone(deep = FALSE) Arguments: deep Whether to make a deep clone.

# Examples

```
# Build a formal context
fc_planets <- FormalContext$new(planets)</pre>
```

```
# Find the concepts
fc_planets$find_concepts()
```

```
# Find join- and meet- irreducible elements
fc_planets$concepts$join_irreducibles()
fc_planets$concepts$meet_irreducibles()
```

equivalencesRegistry Equivalence Rules Registry

#### Description

Equivalence Rules Registry

#### Usage

equivalencesRegistry

#### Format

An object of class equivalence\_registry (inherits from registry) of length 6.

#### Details

This is a registry that stores the equivalence rules that can be applied using the apply\_rules() method in an ImplicationSet.

One can obtain the list of available equivalence operators by: equivalencesRegistry\$get\_entry\_names()

14

fcaR\_options

#### Description

Set or get options for fcaR

#### Usage

fcaR\_options(...)

#### Arguments

. . .

Option names to retrieve option values or [key]=[value] pairs to set options.

#### **Supported options**

The following options are supported

decimal\_places (numeric;2) The number of decimal places to show when printing or exporting to LATEX sets, implications, concepts, etc.

latex\_size (character;"normalsize") Size to use when exporting to LaTeX.

reduced\\_lattice (logical;TRUE) Plot the reduced concept lattice?

FormalContext R6 class for a formal context

#### Description

This class implements the data structure and methods for formal contexts.

#### **Public fields**

I The table of the formal context as a matrix.

attributes The attributes of the formal context.

objects The objects of the formal context.

grades\_set The set of degrees (in [0, 1]) the whole set of attributes can take.

expanded\_grades\_set The set of degrees (in [0, 1]) each attribute can take.

concepts The concept lattice associated to the formal context as a ConceptLattice.

implications A set of implications on the formal context as an ImplicationSet.

# Methods

#### **Public methods:**

- FormalContext\$new()
- FormalContext\$is\_empty()
- FormalContext\$scale()
- FormalContext\$get\_scales()
- FormalContext\$background\_knowledge()
- FormalContext\$dual()
- FormalContext\$intent()
- FormalContext\$uparrow()
- FormalContext\$extent()
- FormalContext\$downarrow()
- FormalContext\$closure()
- FormalContext\$obj\_concept()
- FormalContext\$att\_concept()
- FormalContext\$is\_concept()
- FormalContext\$is\_closed()
- FormalContext\$clarify()
- FormalContext\$reduce()
- FormalContext\$standardize()
- FormalContext\$find\_concepts()
- FormalContext\$find\_implications()
- FormalContext\$to\_transactions()
- FormalContext\$save()
- FormalContext\$load()
- FormalContext\$dim()
- FormalContext\$print()
- FormalContext\$to\_latex()
- FormalContext\$incidence()
- FormalContext\$subcontext()
- FormalContext\$[()
- FormalContext\$plot()
- FormalContext\$use\_logic()
- FormalContext\$get\_logic()
- FormalContext\$use\_connection()
- FormalContext\$get\_connection()
- FormalContext\$clone()

#### Method new(): Creator for the Formal Context class

#### Usage:

FormalContext\$new(I, filename, remove\_const = FALSE)
Arguments:

16

I (numeric matrix) The table of the formal context.

filename (character) Path of a file to import.

remove\_const (logical) If TRUE, remove constant columns. The default is FALSE.

*Details:* Columns of I should be named, since they are the names of the attributes of the formal context.

If no I is used, the resulting FormalContext will be empty and not usable unless for loading a previously saved one. In this case, one can provide a filename to import. Only RDS, CSV and CXT files are currently supported.

Returns: An object of the FormalContext class.

Method is\_empty(): Check if the FormalContext is empty

Usage:

FormalContext\$is\_empty()

*Returns:* TRUE if the FormalContext is empty, that is, has not been provided with a matrix, and FALSE otherwise.

Method scale(): Scale the context

Usage:

FormalContext\$scale(attributes, type, ...)

Arguments:

attributes The attributes to scale

type Type of scaling.

• • •

*Details:* The types of scaling are implemented in a registry, so that scalingRegistry\$get\_entries() returns all types.

In the dots argument, the user can supply the value for bg (logical), which, if set to TRUE, indicates to compute background knowledge as implications on the scales; if FALSE, no implications will be computed on the scales.

Returns: The scaled formal context

Examples:

```
filename <- system.file("contexts", "aromatic.csv", package = "fcaR")
fc <- FormalContext$new(filename)
fc$scale("nitro", "ordinal", comparison = `>=`, values = 1:3)
fc$scale("OS", "nominal", c("O", "S"))
fc$scale(attributes = "ring", type = "nominal")
```

Method get\_scales(): Scales applied to the formal context

Usage:

FormalContext\$get\_scales(attributes = names(private\$scales))

Arguments:

attributes (character) Name of the attributes for which scales (if applied) are returned.

*Returns:* The scales that have been applied to the specified attributes of the formal context. If no attributes are passed, then all applied scales are returned.

#### Examples:

```
filename <- system.file("contexts", "aromatic.csv", package = "fcaR")
fc <- FormalContext$new(filename)
fc$scale("nitro", "ordinal", comparison = `>=`, values = 1:3)
fc$scale("OS", "nominal", c("O", "S"))
fc$scale(attributes = "ring", type = "nominal")
fc$get_scales()
```

Method background\_knowledge(): Background knowledge of a scaled formal context

Usage:

FormalContext\$background\_knowledge()

Returns: An ImplicationSet with the implications extracted from the application of scales.

Examples:

```
filename <- system.file("contexts", "aromatic.csv", package = "fcaR")
fc <- FormalContext$new(filename)
fc$scale("nitro", "ordinal", comparison = `>=`, values = 1:3)
fc$scale("OS", "nominal", c("O", "S"))
fc$scale(attributes = "ring", type = "nominal")
fc$background_knowledge()
```

Method dual(): Get the dual formal context

Usage:
FormalContext\$dual()

Returns: A FormalContext where objects and attributes have interchanged their roles.

Method intent(): Get the intent of a fuzzy set of objects

Usage: FormalContext\$intent(S) Arguments: S (Set) The set of objects to compute the intent for.

*Returns:* A Set with the intent.

Method uparrow(): Get the intent of a fuzzy set of objects

Usage:
FormalContext\$uparrow(S)

Arguments:

S (Set) The set of objects to compute the intent for.

*Returns:* A Set with the intent.

Method extent(): Get the extent of a fuzzy set of attributes

Usage:
FormalContext\$extent(S)

Arguments:

18

#### FormalContext

 ${\tt S}~({\tt Set})$  The set of attributes to compute the extent for.

Returns: A Set with the intent.

#### Method downarrow(): Get the extent of a fuzzy set of attributes

Usage:
FormalContext\$downarrow(S)
Arguments:
S (Set) The set of attributes to compute the extent for.

*Returns:* A Set with the intent.

Method closure(): Get the closure of a fuzzy set of attributes

Usage:
FormalContext\$closure(S)

Arguments:

S (Set) The set of attributes to compute the closure for.

Returns: A Set with the closure.

# Method obj\_concept(): Object Concept

Usage:
FormalContext\$obj\_concept(object)

*Arguments:* object (character) Name of the object to compute its associated concept *Returns:* The object concept associated to the object given.

#### Method att\_concept(): Attribute Concept

Usage:
FormalContext\$att\_concept(attribute)
Arguments:
attribute (character) Name of the attribute to compute its associated concept
Returns: The attribute concept associated to the attribute given.

#### Method is\_concept(): Is a Concept?

Usage: FormalContext\$is\_concept(C) Arguments: C A Concept object Returns: TRUE if C is a concept.

Method is\_closed(): Testing closure of attribute sets

Usage:
FormalContext\$is\_closed(S)

Arguments:

S A Set of attributes

Returns: TRUE if the set S is closed in this formal context.

Method clarify(): Clarify a formal context

Usage:

FormalContext\$clarify(copy = FALSE)

Arguments:

copy (logical) If TRUE, a new FormalContext object is created with the clarified context, otherwise the current one is overwritten.

Returns: The clarified FormalContext.

Method reduce(): Reduce a formal context

Usage:

FormalContext\$reduce(copy = FALSE)

Arguments:

copy (logical) If TRUE, a new FormalContext object is created with the clarified and reduced context, otherwise the current one is overwritten.

Returns: The clarified and reduced FormalContext.

Method standardize(): Build the Standard Context

Usage:

FormalContext\$standardize()

Details: All concepts must be previously computed.

Returns: The standard context using the join- and meet- irreducible elements.

Method find\_concepts(): Use Ganter Algorithm to compute concepts

Usage:

FormalContext\$find\_concepts(verbose = FALSE)

Arguments:

verbose (logical) TRUE will provide a verbose output.

Returns: A list with all the concepts in the formal context.

**Method** find\_implications(): Use modified Ganter algorithm to compute both concepts and implications

Usage:

```
FormalContext$find_implications(save_concepts = TRUE, verbose = FALSE)
```

Arguments:

save\_concepts (logical) TRUE will also compute and save the concept lattice. FALSE is usually faster, since it only computes implications.

verbose (logical) TRUE will provide a verbose output.

Returns: Nothing, just updates the internal fields concepts and implications.

#### FormalContext

**Method** to\_transactions(): Convert the formal context to object of class transactions from the arules package

Usage:
FormalContext\$to\_transactions()

Returns: A transactions object.

Method save(): Save a FormalContext to RDS or CXT format

Usage:

FormalContext\$save(filename = tempfile(fileext = ".rds"))

Arguments:

filename (character) Path of the file where to store the FormalContext.

Details: The format is inferred from the extension of the filename.

Returns: Invisibly the current FormalContext.

**Method** load(): Load a FormalContext from a file

Usage:

FormalContext\$load(filename)

Arguments:

filename (character) Path of the file to load the FormalContext from.

Details: Currently, only RDS, CSV and CXT files are supported.

Returns: The loaded FormalContext.

Method dim(): Dimensions of the formal context

Usage:

FormalContext\$dim()

Returns: A vector with (number of objects, number of attributes).

Method print(): Prints the formal context

Usage:

FormalContext\$print()

Returns: Prints information regarding the formal context.

Method to\_latex(): Write the context in LaTeX format

Usage:

FormalContext\$to\_latex(table = TRUE, label = "", caption = "")

Arguments:

table (logical) If TRUE, surrounds everything between \begin{table} and \end{table}.

label (character) The label for the table environment.

caption (character) The caption of the table.

fraction (character) If none, no fractions are produced. Otherwise, if it is frac, dfrac or sfrac, decimal numbers are represented as fractions with the corresponding LaTeX type-setting.

Returns: A table environment in LaTeX.

Method incidence(): Incidence matrix of the formal context

Usage:

FormalContext\$incidence()

Returns: The incidence matrix of the formal context

Examples:

fc <- FormalContext\$new(planets)</pre>

fc\$incidence()

Method subcontext(): Subcontext of the formal context

Usage:

FormalContext\$subcontext(objects, attributes)

Arguments:

objects (character array) Name of the objects to keep.

attributes (character array) Names of the attributes to keep.

*Details:* A warning will be issued if any of the names is not present in the list of objects or attributes of the formal context.

If objects or attributes is empty, then it is assumed to represent the whole set of objects or attributes of the original formal context.

*Returns:* Another FormalContext that is a subcontext of the original one, with only the objects and attributes selected.

Examples:

fc <- FormalContext\$new(planets)
fc\$subcontext(attributes = c("moon", "no\_moon"))</pre>

Method [(): Subcontext of the formal context

Usage:

FormalContext\$[(objects, attributes)

Arguments:

objects (character array) Name of the objects to keep.

attributes (character array) Names of the attributes to keep.

*Details:* A warning will be issued if any of the names is not present in the list of objects or attributes of the formal context.

If objects or attributes is empty, then it is assumed to represent the whole set of objects or attributes of the original formal context.

*Returns:* Another FormalContext that is a subcontext of the original one, with only the objects and attributes selected.

Examples:

fc <- FormalContext\$new(planets)
fc[, c("moon", "no\_moon")]</pre>

Method plot(): Plot the formal context table

#### FormalContext

#### Usage:

FormalContext\$plot(to\_latex = FALSE, ...)

Arguments:

- to\_latex (logical) If TRUE, export the plot as a tikzpicture environment that can be included in a LaTeX file.
- ... Other parameters to be passed to the tikzDevice that renders the lattice in LaTeX, or for the figure caption. See Details.

*Details:* Particular parameters that control the size of the tikz output are: width, height (both in inches), and pointsize (in points), that should be set to the font size used in the documentclass header in the LaTeX file where the code is to be inserted.

If a caption is provided, the whole tikz picture will be wrapped by a figure environment and the caption set.

*Returns:* If to\_latex is FALSE, it returns nothing, just plots the graph of the formal context. Otherwise, this function returns the LaTeX code to reproduce the formal context plot.

Method use\_logic(): Sets the logic to use

Usage:

FormalContext\$use\_logic(name = available\_logics())

Arguments:

name The name of the logic to use. To see the available names, run available\_logics().

Method get\_logic(): Gets the logic used

Usage:

FormalContext\$get\_logic()

*Returns:* A string with the name of the logic.

Method use\_connection(): Sets the name of the Galois connection to use

Usage:

FormalContext\$use\_connection(connection)

Arguments:

connection The name of the Galois connection. Available connections are "standard" (antitone), "benevolent1" and "benevolent2" (isotone)

Method get\_connection(): Gets the name of the Galois connection

Usage:

FormalContext\$get\_connection()

Returns: A string with the name of the Galois connection

Method clone(): The objects of this class are cloneable with this method.

Usage:

FormalContext\$clone(deep = FALSE)

Arguments:

deep Whether to make a deep clone.

#### References

Guigues J, Duquenne V (1986). "Familles minimales d'implications informatives résultant d'un tableau de données binaires." *Mathématiques et Sciences humaines*, 95, 5-18.

Ganter B, Wille R (1999). Formal concept analysis : mathematical foundations. Springer. ISBN 3540627715.

Belohlavek R (2002). "Algorithms for fuzzy concept lattices." In *Proc. Fourth Int. Conf. on Recent Advances in Soft Computing*. Nottingham, United Kingdom, 200-205.

Hahsler M, Grun B, Hornik K (2005). "arules - a computational environment for mining association rules and frequent item sets." *J Stat Softw*, *14*, 1-25.

#### Examples

```
# Build and print the formal context
fc_planets <- FormalContext$new(planets)</pre>
print(fc_planets)
# Define a set of attributes
S <- Set$new(attributes = fc_planets$attributes)</pre>
S_{assign(moon = 1, large = 1)}
# Compute the closure of S
Sc <- fc_planets$closure(S)</pre>
# Is Sc a closed set?
fc_planets$is_closed(Sc)
# Clarify and reduce the formal context
fc2 <- fc_planets$reduce(TRUE)</pre>
# Find implications
fc_planets$find_implications()
# Read a formal context from CSV
filename <- system.file("contexts", "airlines.csv", package = "fcaR")</pre>
fc <- FormalContext$new(filename)</pre>
# Read a formal context from a CXT file
filename <- system.file("contexts", "lives_in_water.cxt", package = "fcaR")</pre>
fc <- FormalContext$new(filename)</pre>
## -----
## Method `FormalContext$scale`
## ------
filename <- system.file("contexts", "aromatic.csv", package = "fcaR")</pre>
fc <- FormalContext$new(filename)</pre>
fc$scale("nitro", "ordinal", comparison = `>=`, values = 1:3)
fc$scale("OS", "nominal", c("0", "S"))
```

fc\$scale(attributes = "ring", type = "nominal")

#### ImplicationSet

```
## -----
## Method `FormalContext$get_scales`
## -----
filename <- system.file("contexts", "aromatic.csv", package = "fcaR")</pre>
fc <- FormalContext$new(filename)</pre>
fc$scale("nitro", "ordinal", comparison = `>=`, values = 1:3)
fc$scale("OS", "nominal", c("0", "S"))
fc$scale(attributes = "ring", type = "nominal")
fc$get_scales()
## -----
## Method `FormalContext$background_knowledge`
## -----
filename <- system.file("contexts", "aromatic.csv", package = "fcaR")</pre>
fc <- FormalContext$new(filename)</pre>
fc$scale("nitro", "ordinal", comparison = `>=`, values = 1:3)
fc$scale("OS", "nominal", c("O", "S"))
fc$scale(attributes = "ring", type = "nominal")
fc$background_knowledge()
## ------
## Method `FormalContext$incidence`
## ------
fc <- FormalContext$new(planets)</pre>
fc$incidence()
## ------
## Method `FormalContext$subcontext`
## ------
fc <- FormalContext$new(planets)</pre>
fc$subcontext(attributes = c("moon", "no_moon"))
## -----
## Method `FormalContext$[`
## -----
fc <- FormalContext$new(planets)</pre>
fc[, c("moon", "no_moon")]
```

ImplicationSet

*R6 Class for Set of implications* 

#### Description

This class implements the structure needed to store implications and the methods associated.

# Methods

**Public methods:** 

- ImplicationSet\$new()
- ImplicationSet\$get\_attributes()
- ImplicationSet\$[()
- ImplicationSet\$to\_arules()
- ImplicationSet\$add()
- ImplicationSet\$cardinality()
- ImplicationSet\$is\_empty()
- ImplicationSet\$size()
- ImplicationSet\$closure()
- ImplicationSet\$recommend()
- ImplicationSet\$apply\_rules()
- ImplicationSet\$to\_basis()
- ImplicationSet\$print()
- ImplicationSet\$to\_latex()
- ImplicationSet\$get\_LHS\_matrix()
- ImplicationSet\$get\_RHS\_matrix()
- ImplicationSet\$filter()
- ImplicationSet\$support()
- ImplicationSet\$clone()

Method new(): Initialize with an optional name

Usage:

ImplicationSet\$new(...)

Arguments:

... See Details.

*Details:* Creates and initialize a new ImplicationSet object. It can be done in two ways: initialize(name, attributes, lhs, rhs) or initialize(rules)

In the first way, the only mandatory argument is attributes, (character vector) which is a vector of names of the attributes on which we define the implications. Optional arguments are: name (character string), name of the implication set, lhs (a dgCMatrix), initial LHS of the implications stored and the analogous rhs.

The other way is used to initialize the ImplicationSet object from a rules object from package arules.

Returns: A new ImplicationSet object.

Method get\_attributes(): Get the names of the attributes

Usage:

ImplicationSet\$get\_attributes()

Returns: A character vector with the names of the attributes used in the implications.

Method [(): Get a subset of the implication set

26

Usage:

ImplicationSet\$[(idx)

Arguments:

idx (integer or logical vector) Indices of the implications to extract or remove. If logical vector, only TRUE elements are retained and the rest discarded.

*Returns:* A new ImplicationSet with only the rules given by the idx indices (if all idx > 0 and all but idx if all idx < 0.

Method to\_arules(): Convert to arules format

Usage:

ImplicationSet\$to\_arules(quality = TRUE)

Arguments:

quality (logical) Compute the interest measures for each rule?

Returns: A rules object as used by package arules.

Method add(): Add a precomputed implication set

Usage:

ImplicationSet\$add(...)

Arguments:

... An ImplicationSet object, a rules object, or a pair lhs, rhs of Set objects or dgCMatrix. The implications to add to this formal context.

*Returns:* Nothing, just updates the internal implications field.

Method cardinality(): Cardinality: Number of implications in the set

Usage:

ImplicationSet\$cardinality()

Returns: The cardinality of the implication set.

Method is\_empty(): Empty set

Usage:

ImplicationSet\$is\_empty()

Returns: TRUE if the set of implications is empty, FALSE otherwise.

Method size(): Size: number of attributes in each of LHS and RHS

Usage:

ImplicationSet\$size()

*Returns:* A vector with two components: the number of attributes present in each of the LHS and RHS of each implication in the set.

**Method** closure(): Compute the semantic closure of a fuzzy set with respect to the implication set

Usage:

```
ImplicationSet$closure(S, reduce = FALSE, verbose = FALSE)
```

#### Arguments:

S (a Set object) Fuzzy set to compute its closure. Use class Set to build it. reduce (logical) Reduce the implications using simplification logic? verbose (logical) Show verbose output?

*Returns:* If reduce == FALSE, the output is a fuzzy set corresponding to the closure of S. If reduce == TRUE, a list with two components: closure, with the closure as above, and implications, the reduced set of implications.

Method recommend(): Generate a recommendation for a subset of the attributes

Usage:

ImplicationSet\$recommend(S, attribute\_filter)

Arguments:

S (a vector) Vector with the grades of each attribute (a fuzzy set).

attribute\_filter (character vector) Names of the attributes to get recommendation for.

*Returns:* A fuzzy set describing the values of the attributes in attribute\_filter within the closure of S.

Method apply\_rules(): Apply rules to remove redundancies

```
Usage:
ImplicationSet$apply_rules(
  rules = c("composition", "generalization"),
  batch_size = 25000L,
  parallelize = FALSE,
  reorder = FALSE
)
```

Arguments:

rules (character vector) Names of the rules to use. See details.

batch\_size (integer) If the number of rules is large, apply the rules by batches of this size. parallelize (logical) If possible, should we parallelize the computation among different batches? reorder (logical) Should the rules be randomly reordered previous to the computation?

*Details:* Currently, the implemented rules are "generalization", "simplification", "reduction" and "composition".

*Returns:* Nothing, just updates the internal matrices for LHS and RHS.

Method to\_basis(): Convert Implications to Canonical Basis

Usage:

ImplicationSet\$to\_basis()

Returns: The canonical basis of implications obtained from the current ImplicationSet

Method print(): Print all implications to text

Usage:

ImplicationSet\$print()

Returns: A string with all the implications in the set.

#### ImplicationSet

```
Method to_latex(): Export to LaTeX
Usage:
ImplicationSet$to_latex(
    print = TRUE,
    ncols = 1,
    numbered = TRUE,
    numbers = seq(self$cardinality())
)
Arguments:
print (logical) Print to output?
ncols (integer) Number of columns for the output.
numbered (logical) If TRUE (default), implications will be numbered in the output.
```

numbers (vector) If numbered, use these elements to enumerate the implications. The default is to enumerate 1, 2, ..., but can be changed.

Returns: A string in LaTeX format that prints nicely all the implications.

Method get\_LHS\_matrix(): Get internal LHS matrix

Usage:

ImplicationSet\$get\_LHS\_matrix()

Returns: A sparse matrix representing the LHS of the implications in the set.

#### Method get\_RHS\_matrix(): Get internal RHS matrix

Usage: ImplicationSet\$get\_RHS\_matrix()

Returns: A sparse matrix representing the RHS of the implications in the set.

Method filter(): Filter implications by attributes in LHS and RHS

```
Usage:
ImplicationSet$filter(
    lhs = NULL,
    not_lhs = NULL,
    rhs = NULL,
    not_rhs = NULL,
    drop = FALSE
)
```

Arguments:

- 1hs (character vector) Names of the attributes to filter the LHS by. If NULL, no filtering is done on the LHS.
- not\_lhs (character vector) Names of the attributes to not include in the LHS. If NULL (the default), it is not considered at all.
- rhs (character vector) Names of the attributes to filter the RHS by. If NULL, no filtering is done on the RHS.
- not\_rhs (character vector) Names of the attributes to not include in the RHS. If NULL (the default), it is not considered at all.

drop (logical) Remove the rest of attributes in RHS?

*Returns:* An ImplicationSet that is a subset of the current set, only with those rules which has the attributes in 1hs and rhs in their LHS and RHS, respectively.

Method support(): Compute support of each implication

Usage:

ImplicationSet\$support()

*Returns:* A vector with the support of each implication

Method clone(): The objects of this class are cloneable with this method.

Usage:

ImplicationSet\$clone(deep = FALSE)

Arguments:

deep Whether to make a deep clone.

#### References

Ganter B, Obiedkov S (2016). Conceptual Exploration. Springer. https://doi.org/10.1007/978-3-662-49291-8

Hahsler M, Grun B, Hornik K (2005). "arules - a computational environment for mining association rules and frequent item sets." *J Stat Softw*, *14*, 1-25.

Belohlavek R, Cordero P, Enciso M, Mora Á, Vychodil V (2016). "Automated prover for attribute dependencies in data with grades." *International Journal of Approximate Reasoning*, 70, 51-67.

Mora A, Cordero P, Enciso M, Fortes I, Aguilera G (2012). "Closure via functional dependence simplification." *International Journal of Computer Mathematics*, 89(4), 510-526.

#### Examples

```
# Build a formal context
fc_planets <- FormalContext$new(planets)</pre>
```

```
# Find its implication basis
fc_planets$find_implications()
```

```
# Print implications
fc_planets$implications
```

```
# Cardinality and mean size in the ruleset
fc_planets$implications$cardinality()
sizes <- fc_planets$implications$size()
colMeans(sizes)
```

```
# Simplify the implication set
fc_planets$implications$apply_rules("simplification")
```

parse\_implication Parses a string into an implication

#### Description

Parses a string into an implication

#### Usage

parse\_implication(string, attributes)

#### Arguments

string	(character) The string to be parsed
attributes	(character vector) The attributes' names

#### Value

Two vectors as sparse matrices representing the LHS and RHS of the implication

parse\_implications Parses several implications given as a string

#### Description

Parses several implications given as a string

#### Usage

```
parse_implications(input)
```

# Arguments

input (character) The string with the implications or a file containing the implications

#### Details

The format for the input file is:

- Every implication in its own line or separated by semicolon (;)
- Attributes are separated by commas (,)
- The LHS and RHS of each implication are separated by an arrow (->)

## Value

An ImplicationSet

#### Examples

```
input <- system.file("implications", "ex_implications", package = "fcaR")
imps <- parse_implications(input)</pre>
```

planets

Planets data

# Description

This dataset records some properties of the planets in our solar system.

# Usage

planets

# Format

A matrix with 9 rows (the planets) and 7 columns, representing additional features of the planets:

small 1 if the planet is small, 0 otherwise.

medium 1 if the planet is medium-sized, 0 otherwise.

large 1 if the planet is large, 0 otherwise.

near 1 if the planet belongs in the inner solar system, 0 otherwise.

far 1 if the planet belongs in the outer solar system, 0 otherwise.

moon 1 if the planet has a natural moon, 0 otherwise.

**no\_moon** 1 if the planet has no moon, 0 otherwise.

#### Source

Wille R (1982). "Restructuring Lattice Theory: An Approach Based on Hierarchies of Concepts." In Ordered Sets, pp. 445–470. Springer.

#### 32

scalingRegistry Scaling Registry

# Description

Scaling Registry

#### Usage

scalingRegistry

#### Format

An object of class scaling\_registry (inherits from registry) of length 6.

# Details

This is a registry that stores the implemented scales that can be applied using the scale() method in an FormalContext.

One can obtain the list of available equivalence operators by: scalingRegistry\$get\_entry\_names()

Set

R6 class for a fuzzy set with sparse internal representation

# Description

This class implements the data structure and methods for fuzzy sets.

#### Methods

**Public methods:** 

- Set\$new()
- Set\$assign()
- Set\$[()
- Set\$cardinal()
- Set\$get\_vector()
- Set\$get\_attributes()
- Set\$length()
- Set\$print()
- Set\$to\_latex()
- Set\$clone()

Method new(): Creator for objects of class Set

Usage:

Set\$new(attributes, M = NULL, ...)

Arguments:

attributes (character vector) Names of the attributes that will be available in the fuzzy set.

M (numeric vector or column Matrix) Values (grades) to be assigned to the attributes. ... key = value pairs, where the value value is assigned to the key attribute name.

*Details:* If M is omitted and no pair key = value, the fuzzy set is the empty set. Later, one can use the assign method to assign grades to any of its attributes.

Returns: An object of class Set.

Method assign(): Assign grades to attributes in the set

Usage:

Set\$assign(attributes = c(), values = c(), ...)

Arguments:

attributes (character vector) Names of the attributes to assign a grade to.

values (numeric vector) Grades to be assigned to the previous attributes.

... key = value pairs, where the value value is assigned to the key attribute name.

Details: One can use both of: S\$assign(A = 1, B = 0.3) S\$assign(attributes = c(A, B), values = c(1, 0.3)).

Method [(): Get elements by index

Usage: Set\$[(indices)

Arguments:

indices (numeric, logical or character vector) The indices of the elements to return. It can be a vector of logicals where TRUE elements are to be retained.

Returns: A Set but with only the required elements.

Method cardinal(): Cardinal of the Set

Usage:

Set\$cardinal()

Returns: the cardinal of the Set, counted as the sum of the degrees of each element.

Method get\_vector(): Internal Matrix

Usage: Set\$get\_vector()

Returns: The internal sparse Matrix representation of the set.

Method get\_attributes(): Attributes defined for the set

Usage:

Set\$get\_attributes()

Returns: A character vector with the names of the attributes.

#### Method length(): Number of attributes

Usage: Set\$length()

Returns: The number of attributes that are defined for this fuzzy set.

Method print(): Prints the set to console

Usage: Set\$print(eol = TRUE) Arguments: eol (logical) If TRUE, adds an end of line to the output.

Returns: A string with the elements of the set and their grades between brackets .

Method to\_latex(): Write the set in LaTeX format

```
Usage:
Set$to_latex(print = TRUE)
Arguments:
print (logical) Print to output?
Returns: The fuzzy set in LaTeX.
```

Method clone(): The objects of this class are cloneable with this method.

Usage: Set\$clone(deep = FALSE)

Arguments:

deep Whether to make a deep clone.

#### Examples

```
S <- Set$new(attributes = c("A", "B", "C"))
S$assign(A = 1)
print(S)
S$to_latex()
S <- Set$new(c("A", "B", "C"), C = 1, B = 0.5)
S</pre>
```

#### vegas

#### Description

The dataset vegas is the binary translation of the Las Vegas Strip dataset (@moro2017stripping), which records more than 500 TripAdvisor reviews of hotels in Las Vegas Strip. The uninformative attributes (such as the user continent or the weekday of the review) are removed.

#### Usage

vegas

#### Format

A matrix with 504 rows and 25 binary columns. Column names are related to different features of the hotels:

- **Period of Stay** 4 categories are present in the original data, which produces as many binary variables: Period of stay=Dec-Feb, Period of stay=Mar-May, Period of stay=Jun-Aug and Period of stay=Sep-Nov.
- **Traveler type** Five binary categories are created from the original data: Traveler type=Business, Traveler type=Couples, Traveler type=Families, Traveler type=Friends and Traveler type=Solo.
- Pool, Gym, Tennis court, Spa, Casino, Free internet Binary variables for the services offered by each destination hotel
- **Stars** Five binary variables are created, according to the number of stars of the hotel, Stars=3, Stars=3.5, Stars=4, Stars=4.5 and Stars=5.

**Score** The score assigned in the review, from Score=1 to Score=5.

#### Source

Moro, S., Rita, P., & Coelho, J. (2017). Stripping customers' feedback on hotels through data mining: The case of Las Vegas Strip. Tourism Management Perspectives, 23, 41-52.

%&%

Intersection (Logical AND) of Fuzzy Sets

#### Description

Intersection (Logical AND) of Fuzzy Sets

#### Usage

S1 %&% S2

#### %entails%

#### Arguments

S1	A Set
S2	A Set

# Details

Both S1 and S2 must be Sets.

# Value

Returns the intersection of S1 and S2.

# Examples

```
# Build two sparse sets
S <- Set$new(attributes = c("A", "B", "C"))
S$assign(A = 1, B = 1)
T <- Set$new(attributes = c("A", "B", "C"))
T$assign(A = 1, C = 1)
# Intersection
S %&% T</pre>
```

%entails%

# Entailment between implication sets

# Description

Entailment between implication sets

# Usage

imps %entails% imps2

# Arguments

imps	(ImplicationSet) A set of implications.
imps2	(ImplicationSet) A set of implications which is tested to check if it follows semantically from imps.

# Value

A logical vector, where element k is TRUE if the k-th implication in imps2 follows from imps.

# Examples

```
fc <- FormalContext$new(planets)
fc$find_implications()
imps <- fc$implications[1:4]$clone()
imps2 <- fc$implications[3:6]$clone()
imps %entails% imps2</pre>
```

%==%

#### Equality in Sets and Concepts

# Description

Equality in Sets and Concepts

# Usage

C1 %==% C2

# Arguments

C1	A Set or Concept
C2	A Set or Concept

# Details

Both C1 and C2 must be of the same class.

# Value

Returns TRUE if C1 is equal to C2.

# Examples

```
# Build two sparse sets
S <- Set$new(attributes = c("A", "B", "C"))
S$assign(A = 1)
T <- Set$new(attributes = c("A", "B", "C"))
T$assign(A = 1)
# Test whether S and T are equal
S %==% T</pre>
```

38

%-%

# Description

Difference in Sets

# Usage

S1 %-% S2

# Arguments

S1	A Set
S2	A Set

# Details

Both S1 and S2 must be Sets.

# Value

Returns the difference S1 - S2.

# Examples

```
# Build two sparse sets
S <- Set$new(attributes = c("A", "B", "C"))
S$assign(A = 1, B = 1)
T <- Set$new(attributes = c("A", "B", "C"))
T$assign(A = 1)
# Difference
c @ 0 T</pre>
```

S %-% T

%holds\_in%

# Implications that hold in a Formal Context

# Description

Implications that hold in a Formal Context

# Usage

imps %holds\_in% fc

%<=%

# Arguments

imps	(ImplicationSet) The set of implications to test if hold in the formal context.
fc	$({\tt FormalContext}) \ A \ formal \ context \ where \ to \ test \ if \ the \ implications \ hold.$

# Value

A logical vector, indicating if each implication holds in the formal context.

# Examples

```
fc <- FormalContext$new(planets)
fc$find_implications()
imps <- fc$implications$clone()
imps %holds_in% fc</pre>
```

%<=%

#### Partial Order in Sets and Concepts

# Description

Partial Order in Sets and Concepts

# Usage

C1 %<=% C2

# Arguments

C1	A Set or Concept
C2	A Set or Concept

# Details

Both C1 and C2 must be of the same class.

# Value

Returns TRUE if concept C1 is subconcept of C2 or if set C1 is subset of C2.

%or%

# Examples

```
# Build two sparse sets
S <- Set$new(attributes = c("A", "B", "C"))
S$assign(A = 1)
T <- Set$new(attributes = c("A", "B", "C"))
T$assign(A = 1, B = 1)
# Test whether S is subset of T
S %<=% T</pre>
```

%or%

# Union (Logical OR) of Fuzzy Sets

# Description

Union (Logical OR) of Fuzzy Sets

# Usage

S1 %|% S2

#### Arguments

S1	A Set
S2	A Set

## Details

Both S1 and S2 must be Sets.

# Value

Returns the union of S1 and S2.

#### Examples

```
# Build two sparse sets
S <- Set$new(attributes = c("A", "B", "C"))
S$assign(A = 1, B = 1)
T <- Set$new(attributes = c("A", "B", "C"))
T$assign(C = 1)
# Union
S %|% T</pre>
```

%respects%

# Description

Check if Set or FormalContext respects an ImplicationSet

#### Usage

```
set %respects% imps
```

# Arguments

set	(list of Sets, or a FormalContext) The sets of attributes to check whether they
	respect the ImplicationSet.
imps	(ImplicationSet) The set of implications to check.

# Value

A logical matrix with as many rows as Sets and as many columns as implications in the ImplicationSet. A TRUE in element (i, j) of the result means that the i-th Set respects the j-th implication of the ImplicationSet.

# Examples

```
fc <- FormalContext$new(planets)
fc$find_implications()
imps <- fc$implications$clone()
fc %respects% imps</pre>
```

%~%

Equivalence of sets of implications

# Description

Equivalence of sets of implications

## Usage

```
imps %~% imps2
```

#### Arguments

imps	A ImplicationSet.
imps2	Another ImplicationSet.

%~%

# Value

TRUE of and only if imps and imps2 are equivalent, that is, if every implication in imps follows from imps2 and viceversa.

# Examples

```
fc <- FormalContext$new(planets)
fc$find_implications()
imps <- fc$implications$clone()
imps2 <- imps$clone()
imps2$apply_rules(c("simp", "rsimp"))
imps %~% imps2
imps %~% imps2[1:9]</pre>
```

# Index

```
* datasets
    cobre32,4
    cobre61,5
    equivalencesRegistry, 14
    planets, 32
    scalingRegistry, 33
    vegas, 36
%-%, 39
%<=%, 40
%==%, 38
%&%, 36
%~%, 42
%entails%, 37
%holds_in%, 39
%or%, 41
%respects%, 42
as_Set, 2
as_vector, 3
cobre32,4
cobre61,5
Concept, 6
ConceptLattice, 7, 15
ConceptSet, 12
equivalencesRegistry, 14
fcaR::ConceptSet, 7
fcaR_options, 15
FormalContext, 15
ImplicationSet, 15, 25
parse_implication, 31
parse_implications, 31
planets, 32
scalingRegistry, 33
Set, 33
```

vegas, 36