

Package ‘edina’

October 13, 2022

Title Bayesian Estimation of an Exploratory Deterministic Input, Noisy and Gate Model

Version 0.1.1

Description Perform a Bayesian estimation of the exploratory deterministic input, noisy and gate (EDINA) cognitive diagnostic model described by Chen et al. (2018) <doi:10.1007/s11336-017-9579-4>.

URL <https://github.com/tmsalab/edina>

BugReports <https://github.com/tmsalab/edina/issues>

License GPL (>= 2)

Depends R (>= 3.5.0)

Imports Rcpp, ggplot2, jjb, reshape2

LinkingTo Rcpp, RcppArmadillo, rgen

Suggests simcdm

LazyData true

RoxygenNote 7.1.0

Encoding UTF-8

Language en-US

NeedsCompilation yes

Author James Joseph Balamuta [aut, cre, cph] (<<https://orcid.org/0000-0003-2826-8458>>), Steven Andrew Culpepper [aut, cph] (<<https://orcid.org/0000-0003-4226-6176>>), Jeffrey A. Douglas [aut]

Maintainer James Joseph Balamuta <balamut2@illinois.edu>

Repository CRAN

Date/Publication 2020-03-25 13:50:15 UTC

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as_q_matrix *Coerce data.frame and matrix classes to Q Matrix.*

Description

`as.q_matrix` acts as an aliases.

Usage

```
as_q_matrix(x, ...)

## S3 method for class 'data.frame'
as_q_matrix(x, ...)

## S3 method for class 'matrix'
as_q_matrix(x, ...)

## Default S3 method:
as_q_matrix(x, ...)
```

Arguments

| | |
|-----|---|
| x | Either a <code>data.frame</code> or <code>matrix</code> . |
| ... | Not used |

Value

A q_matrix object.

See Also

[q_matrix\(\)](#)

Examples

```
# Q matrix values
x = matrix(c(1, 0, 0, 1), nrow = 2)

# Construct class
q_mat = as_q_matrix(x)
```

autoplot.auto_edina *Graph the Auto EDINA Object*

Description

Presents either the fitting of model heuristics or the evolution of parameters on a graph

Usage

```
## S3 method for class 'auto_edina'
autoplot(
  object,
  type = c("selection", "guessing", "slipping", "evolution"),
  ...
)
```

Arguments

| | |
|--------|--|
| object | An auto_edina object. |
| type | Kind of graph to display. Valid types: "selection" or "evolution". |
| ... | Not used. |

Value

A ggplot2 object.

See Also

[auto_edina\(\)](#), [best_model\(\)](#), [model_selection_graph\(\)](#), [parameter_evolution_graph\(\)](#)

Examples

```

if(requireNamespace("simcdm", quietly = TRUE)) {

  # Set a seed for reproducibility
  set.seed(1512)

  # Setup data simulation parameters
  N = 2      # Number of Examinees / Subjects
  J = 10     # Number of Items
  K = 2      # Number of Skills / Attributes

  # Note:
  # Sample size and attributes have been reduced to create a minimally
  # viable example that can be run during CRAN's automatic check.
  # Please make sure to have a larger sample size...

  # Assign slipping and guessing values for each item
  ss = gs = rep(.2, J)

  # Simulate an identifiable Q matrix
  Q = simcdm::sim_q_matrix(J, K)

  # Simulate subject attributes
  subject_alphas = simcdm::sim_subject_attributes(N, K)

  # Simulate items under the DINA model
  items_dina = simcdm::sim_dina_items(subject_alphas, Q, ss, gs)

  # Requires at least 15 seconds of execution time.
  # Three EDINA models will be fit with increasing number of attributes.
  model_set_edina = auto_edina(items_dina, k = 2:4)

  # Visualize results results
  autoplot(model_set_edina, type = "selection")

  # Equivalent to:
  model_selection_graph(model_set_edina)

  # View model parameters
  autoplot(model_set_edina, type = "guessing")

  # Or directly call with:
  parameter_evolution_graph(model_set_edina, type = "guessing")
}

```

Description

Automatically select an appropriate K dimension for a Q matrix under the Exploratory Deterministic Input, Noise And gate (EDINA) Model.

Usage

```
auto_edina(data, k = 2:4, burnin = 10000, chain_length = 20000)
```

Arguments

| | |
|--------------|---|
| data | Binary responses to assessments in matrix form with dimensions $N \times J$. |
| k | Number of Attribute Levels as a positive integer. |
| burnin | Number of Observations to discard on the chain. |
| chain_length | Length of the MCMC chain |

Value

An auto_edina object that contains:

- edina_models: A list containing all estimated edina model objects.
- criterions: Information criterions calculated for each model
- k_checked: Varying k dimensions checked.
- j: Number of Items

See Also

[autoplot.auto_edina\(\)](#), [best_model\(\)](#), [model_selection_graph\(\)](#), [parameter_evolution_graph\(\)](#)

Examples

```
if(requireNamespace("simcdm", quietly = TRUE)) {

  # Set a seed for reproducibility
  set.seed(1512)

  # Setup data simulation parameters
  N = 15    # Number of Examinees / Subjects
  J = 10    # Number of Items
  K = 2     # Number of Skills / Attributes

  # Note:
  # Sample size and attributes have been reduced to create a minimally
  # viable example that can be run during CRAN's automatic check.
  # Please make sure to have a larger sample size...

  # Assign slipping and guessing values for each item
  ss = gs = rep(.2, J)

  # Simulate an identifiable Q matrix
```

```

Q = simcdm::sim_q_matrix(J, K)

# Simulate subject attributes
subject_alphas = simcdm::sim_subject_attributes(N, K)

# Simulate items under the DINA model
items_dina = simcdm::sim_dina_items(subject_alphas, Q, ss, gs)

# Requires at least 15 seconds of execution time.
# Three EDINA models will be fit with increasing number of attributes.
model_set_edina = auto_edina(items_dina, k = 2:4)

# Display results
model_set_edina

# Retrieve criterion table
table = summary(model_set_edina)

# Extract "best model"
best_model(model_set_edina)

}

```

best_model*Extract the Best Model***Description**

Extracts the best model from the `auto_*`() search procedure.

Usage

```

best_model(x, ...)

## S3 method for class 'auto_edina'
best_model(x, ic = c("ppp", "bic", "dic"), ...)

```

Arguments

| | |
|------------------|--|
| <code>x</code> | An <code>auto_edina</code> object |
| <code>...</code> | Not used. |
| <code>ic</code> | Information criterion name. Default "ppp". |

Value

An `edina` model object corresponding to the smallest value of requested information criterion.

See Also

[DIC.edina\(\)](#), [BIC.edina\(\)](#), [PPP.edina\(\)](#)

BIC.edina

Bayesian Information Criterion (BIC)

Description

Calculate BIC for EDINA models.

Usage

```
## S3 method for class 'edina'  
BIC(object, ...)
```

Arguments

| | |
|--------|-----------------|
| object | An edina object |
| ... | Not used. |

Value

The BIC value of the given model.

BIC Computation Procedure

$$BIC = -2 \log p(\mathbf{y}|\hat{\theta}) + ((k+2)*j + 2^k) \log(n)$$

See Also

[PPP.edina\(\)](#), [DIC.edina\(\)](#)
[PPP.edina\(\)](#), [DIC.edina\(\)](#)

DIC

*Deviance Information Criterion (DIC)***Description**

Calculate DIC for EDINA models.

Usage

```
DIC(object, ...)
## S3 method for class 'edina'
DIC(object, ...)
```

Arguments

| | |
|--------|-----------------|
| object | An edina object |
| ... | Not used. |

Value

The DIC value of the given model.

DIC Computation Procedure

$$DIC = -2 \left(\log p(\mathbf{y}|\hat{\theta}) - 2 \left(\log p(\mathbf{y}|\hat{\theta}) - \frac{1}{N} \sum_{n=1}^N \log p(\mathbf{y}|\theta_s) \right) \right)$$

See Also

[PPP.edina\(\)](#), [BIC.edina\(\)](#)

edina

*EDINA Estimation Routine***Description**

Performs the Exploratory Deterministic Input, Noise and Gate Model (EDINA) estimation on a given data set with a prespecified k value.

Usage

```
edina(data, k = 3, burnin = 10000, chain_length = 20000)
```

Arguments

| | |
|--------------|---|
| data | Binary responses to assessments in matrix form with dimensions $N \times J$. |
| k | Number of Attribute Levels as a positive integer. |
| burnin | Number of Observations to discard on the chain. |
| chain_length | Length of the MCMC chain |

Value

An edina object that contains:

- coefficients: Estimated coefficients of the model fit
- loglike_summed: Summed log-likelihood
- loglike_pmean: Mean of log-likelihood
- pi_classes: Latent classes
- avg_q: Estimated Averaged Q Matrix
- est_q: Estimated Dichotomous Q Matrix
- or_tested: Odds Ratio used in the model selection.
- sample_or: Odds Ratio for the sample.
- n: Number of Observations
- j: Number of Items
- k: Number of Traits
- burnin: Amount of iterations to discard
- chain_length: Amount of iterations to retain.
- timing: Duration of the run
- dataset_name: Name of the data set used in estimation.

See Also

[auto_edina\(\)](#), [summary.edina\(\)](#), [print.edina\(\)](#)

Examples

```
if(requireNamespace("simcdm", quietly = TRUE)) {  
  
  # Set a seed for reproducibility  
  set.seed(1512)  
  
  # Setup data simulation parameters  
  N = 1      # Number of Examinees / Subjects  
  J = 10     # Number of Items  
  K = 2      # Number of Skills / Attributes  
  
  # Note:  
  # Sample size and attributes have been reduced to create a minimally  
  # viable example that can be run during CRAN's automatic check.  
}
```

```

# Please make sure to have a larger sample size...

# Assign slipping and guessing values for each item
ss = gs = rep(.2, J)

# Simulate an identifiable Q matrix
Q = simcdm::sim_q_matrix(J, K)

# Simulate subject attributes
subject_alphas = simcdm::sim_subject_attributes(N, K)

# Simulate items under the DINA model
items_dina = simcdm::sim_dina_items(subject_alphas, Q, ss, gs)

# Compute the edina model
edina_model = edina(items_dina, k = K)

# Display results
edina_model

# Provide a summary overview
summary(edina_model)
}

```

extract_q_matrix *Extract Q Matrix*

Description

Given a modeling object, extract the Q Matrix

Usage

```

extract_q_matrix(x, ...)

## S3 method for class 'q_matrix'
extract_q_matrix(x, ...)

## S3 method for class 'edina'
extract_q_matrix(x, binary = TRUE, ...)

## Default S3 method:
extract_q_matrix(x, ...)

```

Arguments

| | |
|-----|-----------------------------|
| x | An edina or q_matrix object |
| ... | Additional parameters |

binary Boolean to indicate whether the Q matrix is shown in dichotomous form or in an estimated form.

Value

A matrix that is either dichotomous or estimated depending on the value of the `binary` parameter.

See Also

[q_matrix\(\)](#), [as_q_matrix\(\)](#), [edina\(\)](#), [auto_edina\(\)](#)

Examples

```
# Q matrix values
x = matrix(c(1, 0, 0, 1), nrow = 2)

# Show Q matrix structure
Q = q_matrix(x)

# Retrieve Q matrix
extract_q_matrix(Q)
```

model_selection_graph *View Model Selection Statistics Across Models*

Description

Displays information about the value of each model information criterion for a given model across the dimensions the Q matrix is estimated.

Usage

```
model_selection_graph(x, ...)
```

Arguments

x An `auto_edina` or `auto_errum` object.
... Not used

Value

A ggplot2 object

See Also

[autoplot.auto_edina\(\)](#)

`parameter_evolution_graph`

View Slipping and Guessing Parameter Changes Across Models

Description

Displays the slipping and guessing parameter changes for each model across the dimensions the Q matrix is estimated.

Usage

```
parameter_evolution_graph(x, ...)
```

Arguments

| | |
|------------------|---|
| <code>x</code> | An <code>auto_edina</code> or <code>auto_errum</code> object. |
| <code>...</code> | Not used |

Value

A `ggplot2` object

See Also

[autoplot.auto_edina\(\)](#)

`PPP`

Posterior Predictive Probabilities (PPPs)

Description

Computes posterior predictive probabilities (PPPs) based on the odds ratios for each pair of items.

Usage

```
PPP(object, ...)
## S3 method for class 'edina'
PPP(object, alpha = 0.05, ...)
```

Arguments

| | |
|---------------------|---|
| <code>object</code> | An <code>edina</code> object |
| <code>...</code> | Not used. |
| <code>alpha</code> | Defining region to indicate the level of extremeness the data must before the model is problematic. |

Details

PPPs that smaller than 0.05 or greater than 0.95 tend to be extreme and evidence of misfit. As a result, this is more of a heuristic metric.

Value

The PPP value given the specified alpha value.

PPP Computation Procedure

1. simulate observed responses $\mathbf{Y}^{(r)}$ using model parameters from iteration r of the MCMC sampler
2. computing the odds ratio for each pair of items at iteration r as

$$OR^{(r)} = n_{11}^{(r)} n_{00}^{(r)} / \left(n_{10}^{(r)} n_{01}^{(r)} \right)$$

, where $n_{11}^{(r)}$ is the frequency of ones on both variables at iteration r , $n_{10}^{(r)}$ is the frequency of ones on the first item and zeros on the second at iteration r , etc.; and

3. computing PPPs for each item pair as the proportion of generated $OR^{(r)}$'s that exceeded elements of the observed odds ratios.

`print.auto_edina` *Print method for auto_edina*

Description

Custom print method for displaying the results of the Auto EDINA method.

Usage

```
## S3 method for class 'auto_edina'
print(x, ...)
```

Arguments

| | |
|------------------|---|
| <code>x</code> | An <code>auto_edina</code> object |
| <code>...</code> | Additional values passed onto the <code>print.data.frame</code> method. |

Value

None.

The function provides a side-effect of displaying the overview of computed results across all models estimated.

`print.edina`*Printing out the EDINA Object***Description**

Custom print method for computing the EDINA.

Usage

```
## S3 method for class 'edina'
print(x, binary = FALSE, ...)
```

Arguments

- | | |
|---------------------|--|
| <code>x</code> | An <code>edina</code> object |
| <code>binary</code> | Boolean to indicate whether the Q matrix is shown in dichotomous form or in an estimated form. |
| <code>...</code> | Additional methods passed onto the <code>print.matrix</code> method. |

Value

None.

The function provides a side-effect of displaying the overview of the model estimated.

`print.q_matrix`*Printing out a Q Matrix Object***Description**

Custom print method for the Q Matrix Object.

Usage

```
## S3 method for class 'q_matrix'
print(x, ...)
```

Arguments

- | | |
|------------------|--|
| <code>x</code> | An <code>q_matrix</code> object |
| <code>...</code> | Additional methods passed onto the <code>print.matrix</code> method. |

Value

An invisible `matrix` without the `q_matrix` class displayed as a part of the output displayed.

See Also`q_matrix(), as_q_matrix()`**Examples**

```
# Q matrix values
x = matrix(c(1, 0, 0, 1), nrow = 2)

# Show Q matrix structure
q_matrix(x)
```

```
print.summary_auto_edina
      Print the auto_edina model summary
```

Description

Custom method for displaying the results of the `summary(auto_edina)`.

Usage

```
## S3 method for class 'summary_auto_edina'
print(x, ...)
```

Arguments

| | |
|------------------|---|
| <code>x</code> | A <code>summary_auto_edina</code> object |
| <code>...</code> | Additional values passed onto the <code>print.data.frame</code> method. |

Value

None.

The function provides a side-effect of displaying the overview of computed results across all models estimated.

`print.summary_edina` *Printing out the Summary EDINA Object*

Description

Custom print method for displaying the EDINA model summary information.

Usage

```
## S3 method for class 'summary_edina'
print(x, binary = FALSE, ...)
```

Arguments

| | |
|---------------------|--|
| <code>x</code> | A <code>summary_edina</code> object |
| <code>binary</code> | Boolean to indicate whether the Q matrix is shown in dichotomous form or in an estimated form. |
| <code>...</code> | Past onto the <code>print.data.frame</code> method. |

Value

None.

The function provides a side-effect of displaying the overview of the model estimated.

`q_graph`

Graph Q Matrix

Description

Provides a heatmap approach to showing the estimated binary or averaged values of the Q Matrix.

Usage

```
q_graph(x, ...)

## S3 method for class 'auto_edina'
q_graph(x, binary = TRUE, ic = c("ppp", "bic", "dic"), ...)

## S3 method for class 'edina'
q_graph(x, binary = TRUE, ...)

## S3 method for class 'matrix'
q_graph(x, ...)

## S3 method for class 'q_matrix'
q_graph(x, ...)
```

Arguments

- x Either an `edina`, `auto_edina`, or `q_matrix` object.
- ... Additional parameters not used
- binary Boolean to indicate if a classified Q (dichotomous by decision rule) or an estimate Q (non-dichotomous) or should be shown. Default: TRUE.
- ic Information criterion name. Default "ppp".

Value

A `ggplot2` object with a heatmap overview of the estimated Q matrix.

Examples

```
q = q_matrix(matrix(c(1, 0, 1, 1, 0, 1), ncol = 3))
q_graph(q)
```

q_matrix*Create a Q Matrix Object*

Description

Provides a way to create an object as a "q_matrix".

Usage

```
q_matrix(x)
```

Arguments

- x Either a `data.frame` or `matrix`.

Value

A `q_matrix` object.

See Also

[as_q_matrix\(\)](#)

Examples

```
# Q matrix values
x = matrix(c(1, 0, 0, 1), nrow = 2)

# Q matrix wrapper
q_mat = q_matrix(x)

# Data Frame encoding of Q
q_df = data.frame(
  k1 = c(1, 0),
  k2 = c(0, 1)
)

# Create a Q matrix
q_mat = q_matrix(q_df)
```

summary.auto_edina *Summarize auto_edina model data*

Description

Custom method for displaying the results of the `auto_edina`.

Usage

```
## S3 method for class 'auto_edina'
summary(object, ...)
```

Arguments

| | |
|--------|-----------------------------------|
| object | An <code>auto_edina</code> object |
| ... | Not used. |

Value

The original `auto_edina` object with an added class of `summary.auto_edina`.

summary.edina *Summarize the EDINA Object*

Description

Provide a more detailed view inside of edina model object.

Usage

```
## S3 method for class 'edina'  
summary(object, alpha = 0.05, ...)
```

Arguments

| | |
|--------|---|
| object | An edina object |
| alpha | Defining region to indicate the level of extremeness the data must before the model is problematic. |
| ... | Not used. |

Value

A summary object that includes everything in the original [edina\(\)](#) object and:

- `model_fit`: Matrix of model fit summary statistics.
- `alpha`: Alpha-value used to compute `PPP()`s.

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