Package 'UStatBookABSC'

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Title A Companion Package to the Book ``U-Statistics, M-Estimation and Resampling"

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Description A set of functions leading to multivariate response L1 regression. This includes functions on computing Euclidean inner products and norms, weighted least squares estimates on multivariate responses, function to compute fitted values and residuals. This package is a companion to the book ``U-Statistics, M-estimation and Resampling", by Arup Bose and Snigdhansu Chatterjee, to appear in 2017 as part of the ``Texts and Readings in Mathematics" (TRIM) series of Hindustan Book Agency and Springer-Verlag.

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CCU12_Precip

Description

Precipitation for June-September 2012 recorded in Kolkata

Usage

data(CCU12_Precip)

Format

A data frame with columns

Date The data in Year-Month-Day format

Precip Precipitation in millimeters

TMax Maximum temperature, in Celcius

TMin Minimum temperature, in Celcius

Examples

Precip <-CCU12_Precip\$Precip
TMax <-CCU12_Precip\$TMax
plot(TMax, Precip)</pre>

FitAndResidualsComputes a linear regression fit and residuals on possibly multivariate
responses

Description

Computes a linear regression fit and residuals on possibly multivariate responses

Usage

FitAndResiduals(Y, X, BetaHat)

Arguments

Υ	a numeric matrix, to act as response
Х	a numeric matrix, to act as covariates
BetaHat	a numeric matrix, to act as slope

IdentityMatrix

Value

a list consisting of two vectors, the fitted values and residuals

Examples

```
## Not run:
DataY = cbind(CCU12_Precip$Precip, CCU12_Precip$TMax);
DataX = cbind(rep(1, length(CCU12_Precip$Precip)), CCU12_Precip$TMin)
BetaHat.New = WLS(DataY, DataX)
Results.New = FitAndResiduals(DataY, DataX, BetaHat.New);
```

End(Not run)

IdentityMatrix Obtains the identity matrix of dimension n

Description

Obtains the identity matrix of dimension n

Usage

IdentityMatrix(n)

Arguments

n

an integer

Value

an identity matrix

Examples

I.3 = IdentityMatrix(3)
print(I.3)

InnerProduct

Description

Computes the Euclidean inner product

Usage

InnerProduct(a, b, na.rm)

Arguments

а	a numeric vector
b	another numeric vector
na.rm	logical

Value

a real number

Examples

```
x <- c(1, 2, 3)
y <- c(3, 0, 1)
InnerProduct(x, y)</pre>
```

L1Regression

Computes a L1 multivariate regression This is the equivalent of median regression when the response is possibly multivariate

Description

Computes a L1 multivariate regression This is the equivalent of median regression when the response is possibly multivariate

Usage

```
L1Regression(Data.Y, Data.X, Weights,
InitialValue = "WLS", MaxIteration, epsilon, lambda)
```

Norm

Arguments

Data.Y	a numeric matrix, to act as response
Data.X	a numeric matrix, to act as covariates
Weights	a numeric matrix, to act as weights
InitialValue	a character, to denote how the initial estimate will be computed currently the only available option is WLS
MaxIteration	an integer, for the maximum number of iterations allowed
epsilon	a positive real number, as tolerance value for convergence
lambda	a real number between 0 and 1, to control the amount of update allowed in each iteration

Value

a list consisting of the iteration value at the last step, the difference in norms between the last two iterations, and the estimate of slope

Examples

```
## Not run:
DataY = cbind(CCU12_Precip$Precip, CCU12_Precip$TMax);
DataX = cbind(rep(1, length(CCU12_Precip$Precip)), CCU12_Precip$TMin)
A2 = L1Regression(DataY, DataX)
```

End(Not run)

Norm

Computes the Euclidean norm

Description

Computes the Euclidean norm

Usage

Norm(a, na.rm)

Arguments

а	a numeric vector
na.rm	logical

Value

a real number

Examples

x <- c(1, 2) Norm(x)

WLS	Computes a weighted least squares linear regression on possibly mul-
	tivariate responses

Description

Computes a weighted least squares linear regression on possibly multivariate responses

Usage

WLS(Y, X, W)

Arguments

Υ	a numeric matrix, to act as response
Х	a numeric matrix, to act as covariates
W	a numeric matrix, to act as weights

Value

a vector of regression coefficients

Examples

```
## Not run:
DataY = cbind(CCU12_Precip$Precip, CCU12_Precip$TMax);
DataX = cbind(rep(1, length(CCU12_Precip$Precip)), CCU12_Precip$TMin)
BetaHat.New = WLS(DataY, DataX)
```

End(Not run)

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