Package 'ShrinkCovMat'

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Type Package

Title Shrinkage Covariance Matrix Estimators

Version 1.4.0

Description Provides nonparametric Steinian shrinkage estimators of the covariance matrix that are suitable in high dimensional settings, that is when the number of variables is larger than the sample size.

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Depends R (>= 2.10)

LazyData true

NeedsCompilation yes

Encoding UTF-8

URL http://github.com/AnestisTouloumis/ShrinkCovMat

BugReports http://github.com/AnestisTouloumis/ShrinkCovMat/issues

RoxygenNote 6.1.1

Suggests testthat (>= 2.1.0), covr

Imports Rcpp (>= 1.0.1)

LinkingTo Rcpp, RcppArmadillo

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Repository CRAN

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Contents

ShrinkCovMat-package   *Shrinkage Covariance Matrix Estimators*

Description

Provides nonparametric Stein-type shrinkage estimators of the covariance matrix that are suitable and statistically efficient when the number of variables is larger than the sample size. These estimators are non-singular and well-conditioned regardless of the dimensionality.

Details

Each of the implemented shrinkage covariance matrix estimators is a convex linear combination of the sample covariance matrix and of a target matrix. Three options are considered for the target matrix: (a) the diagonal matrix with diagonal elements the average of the sample variances (shrinkcovmat.equal), (b) the diagonal matrix with diagonal elements the corresponding sample variances (shrinkcovmat.unequal), and (c) the identity matrix (shrinkcovmat.identity). The optimal shrinkage intensity determines how much the sample covariance matrix will be shrunk towards the selected target matrix. Estimation of the corresponding optimal shrinkage intensities is discussed in *Touloumis (2015)*. The function targetselection is designed to ease the selection of the target matrix.

Author(s)

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References

Touloumis, A. (2015) Nonparametric Stein-type Shrinkage Covariance Matrix Estimators in High-Dimensional Settings. *Computational Statistics & Data Analysis* **83**, 251–261.

See Also

Useful links:

- http://github.com/AnestisTouloumis/ShrinkCovMat

- Report bugs at http://github.com/AnestisTouloumis/ShrinkCovMat/issues

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colon	*Colon Cancer Dataset*

Description

The dataset describes a colon cancer study (*Alon et al., 1999*) in which gene expression levels were measured on 40 normal tissues and on 22 tumor colon tissues. Note that a logarithmic (base 10) transformation has been applied to the gene expression levels.

Format

A data frame in which the rows correspond to 2000 genes and the columns to 62 tissues. The first 40 columns belong to the normal tissue group while the last 22 columns to the tumor colon tissue group.

Source

<http://genomics-pubs.princeton.edu/oncology/affydata> # nolint [Last Assessed: 2016-05-21]

References

Alon, U., Barkai, N., Notterman, D.A., Gish, K., Ybarra, S., Mack, D. and Levine, A.J. (1999) Broad patterns of gene expression revealed by clustering analysis of tumor and normal colon tissues probed by oligonucleotide arrays. *Proceedings of the National Academy of Sciences of the United States of America* **96**, 6745–6750.

Examples

```
data(colon)
summary(colon)
```

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shrinkcovmat.equal	*Shrinking the Sample Covariance Matrix Towards a Sphericity Matrix*

Description

Provides a nonparametric Stein-type shrinkage estimator of the covariance matrix that is a linear combination of the sample covariance matrix and of a diagonal matrix with the average of the sample variances on the diagonal and zeros elsewhere.

Usage

```
shrinkcovmat.equal(data, centered = FALSE)
```

Arguments

data	a numeric matrix containing the data.
centered	a logical indicating if the mean vector is the zero vector.

Details

The rows of the data matrix data correspond to variables and the columns to subjects.

Value

Returns an object of the class 'shrinkcovmathat' that has components:

SigmaHat	The Stein-type shrinkage estimator of the covariance matrix.
lambdahat	The estimated optimal shrinkage intensity.
sigmasample	The sample covariance matrix.
Target	The target covariance matrix.
centered	If the data are centered around their mean vector.

Author(s)

Anestis Touloumis

References

Touloumis, A. (2015) nonparametric Stein-type Shrinkage Covariance Matrix Estimators in High-Dimensional Settings. *Computational Statistics & Data Analysis* **83**, 251–261.

See Also

shrinkcovmat.unequal and shrinkcovmat.identity.

Examples

```
data(colon)
normal_group <- colon[, 1:40]
tumor_group <- colon[, 41:62]
sigma_hat_normal_group <- shrinkcovmat.equal(normal_group)
sigma_hat_normal_group
sigma_hat_tumor_group <- shrinkcovmat.equal(tumor_group)
sigma_hat_tumor_group
```

shrinkcovmat.identity   *Shrinking the Sample Covariance Matrix Towards the Identity Matrix*

Description

Provides a nonparametric Stein-type shrinkage estimator of the covariance matrix that is a linear combination of the sample covariance matrix and of the identity matrix.

Usage

```
shrinkcovmat.identity(data, centered = FALSE)
```

Arguments

data   a numeric matrix containing the data.

centered   a logical indicating if the mean vector is the zero vector.

Details

The rows of the data matrix data correspond to variables and the columns to subjects.

Value

Returns an object of the class 'shrinkcovmathat' that has components:

Sigmahat   The Stein-type shrinkage estimator of the covariance matrix.

lambdahat   The estimated optimal shrinkage intensity.

Sigmasample   The sample covariance matrix.

Target   The target covariance matrix.

centered   If the data are centered around their mean vector.

Author(s)

Anestis Touloumis

References

Touloumis, A. (2015) nonparametric Stein-type Shrinkage Covariance Matrix Estimators in High-Dimensional Settings. *Computational Statistics & Data Analysis* **83**, 251–261.

See Also

[shrinkcovmat.equal](#) and [shrinkcovmat.unequal](#).

Examples

```
data(colon)
normal_group <- colon[, 1:40]
tumor_group <- colon[, 41:62]
sigma_hat_normal_group <- shrinkcovmat.identity(normal_group)
sigma_hat_normal_group
sigma_hat_tumor_group <- shrinkcovmat.identity(tumor_group)
sigma_hat_tumor_group
```

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shrinkcovmat.unequal   *Shrinking the Sample Covariance Matrix Towards a Diagonal Matrix*
                            with Diagonal Elements the Sample Variances.

Description

Provides a nonparametric Stein-type shrinkage estimator of the covariance matrix that is a linear combination of the sample covariance matrix and of the diagonal matrix with elements the corresponding sample variances on the diagonal and zeros elsewhere.

Usage

```
shrinkcovmat.unequal(data, centered = FALSE)
```

Arguments

data	a numeric matrix containing the data.
centered	a logical indicating if the vectors are centered around their mean vector.

Details

The rows of the data matrix `data` correspond to variables and the columns to subjects.

Value

Returns an object of the class 'shrinkcovmathat' that has components:

Sigmahat	The Stein-type shrinkage estimator of the covariance matrix.
lambdahat	The estimated optimal shrinkage intensity.
Sigmasample	The sample covariance matrix.
Target	The target covariance matrix.
centered	If the data are centered around their mean vector.

Author(s)

Anestis Touloumis

References

Touloumis, A. (2015) nonparametric Stein-type Shrinkage Covariance Matrix Estimators in High-Dimensional Settings. *Computational Statistics & Data Analysis* **83**, 251–261.

See Also

shrinkcovmat.equal and shrinkcovmat.identity.

Examples

```
data(colon)
normal_group <- colon[, 1:40]
tumor_group <- colon[, 41:62]
sigma_hat_normal_group <- shrinkcovmat.unequal(normal_group)
sigma_hat_normal_group
sigma_hat_tumor_group <- shrinkcovmat.unequal(tumor_group)
sigma_hat_tumor_group
```

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targetselection   *Target Matrix Selection*

Description

Implements the rule of thumb proposed by Touloumis (2015) for target matrix selection. If the estimated optimal shrinkage intensities of the three target matrices are of similar magnitude, then the average and the range of the sample variances should be inspected in order to adopt the most plausible target matrix.

Usage

```
targetselection(data, centered = FALSE)
```

Arguments

data	a numeric matrix containing the data.
centered	a logical indicating if the mean vector is the zero vector.

Details

The rows of the data matrix data correspond to variables and the columns to subjects.

Value

Prints the estimated optimal shrinkage intensities, the range and average of the sample variances and returns an object of the class 'targetsel' that has components:

optimal_sphericity
                  The estimated optimal intensity for a target matrix with equal variances.
optimal_identity
                  The estimated optimal shrinkage intensity for the identity target matrix.
optimal_diagonal
                  The estimated optimal intensity for a target matrix with unequal variances.
range   The range of the sample variances.
average   The average of the sample variances.

Author(s)

Anestis Touloumis

References

Touloumis, A. (2015) Nonparametric Stein-type Shrinkage Covariance Matrix Estimators in High-Dimensional Settings. *Computational Statistics & Data Analysis* **83**, 251–261.

Examples

```
data(colon)
normal_group <- colon[, 1:40]
targetselection(normal_group)
## Similar intensities, the range of the sample variances is small and the
## average is not close to one. The scaled identity matrix seems to be the
## most suitable target matrix for the normal group.

tumor_group <- colon[, 41:62]
targetselection(tumor_group)
## Similar intensities, the range of the sample variances is small and the
## average is not close to one. The scaled identity matrix seems to be the
## most suitable target matrix for the colon group.
```

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