## Package 'RPtests'

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Type Package

Version 0.1.5

**Description** Performs goodness of fits tests for both high and low-dimensional linear models. It can test for a variety of model misspecifications including nonlinearity and heteroscedasticity. In addition one can test the significance of potentially large groups of variables, and also produce p-values for the significance of individual variables in high-dimensional linear regression.

**License** GPL ( $\geq 2$ )

Imports glmnet, parallel, randomForest, Rcpp, stats

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Author Rajen Shah [aut, cre], Peter Buhlmann [aut]

Maintainer Rajen Shah <r.shah@statslab.cam.ac.uk>

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Title Goodness of Fit Tests for High-Dimensional Linear Regression Models

pval

#### Description

Produces p-values given a list of simulated test statistics and the true test statistic (which may be a vector if it is the output of multiple RP functions).

## Usage

pval(test, test\_sim)

## Arguments

test	A numeric vector of test statistics.
test_sim	A list of test statisites, each component of which is a numeric vector.

## Details

In the case where the individual test statistics are vectors, the first component of test is compared against the first components of test\_sim[[1]], test\_sim[[2]] etc. and the results of these multiple comparisons are combined into a single p-value (see the reference). When the lengths of the test statistics differ, the final components are first discarded to make all the test statistics have equal length.

## Value

A single p-value.

## References

Shah, R. D., Buhlmann, P. (2017) *Goodness of fit tests for high-dimensional linear models* https://rss.onlinelibrary.wiley.com/doi/10.1111/rssb.12234

## See Also

RPtest the output of which this would typically be applied to.

#### Description

Can test for the significance of (potentially large) groups of predictors and the presence of nonlinearity or heteroscedasticity in the context of both low and high-dimensional linear models. Outputs a p-value. Also allows for the calibration of arbitrary goodness of fit tests via specification of RPfunction.

## Usage

```
RPtest(
 х,
 у,
  resid_type = c("Lasso", "OLS"),
  test = c("nonlin", "group", "hetero"),
 x_alt,
 RPfunction = NULL,
 B = 49L,
 rand_gen = rnorm,
 noise_matrix = NULL,
 mc.cores = 1L,
 nfolds = 5L,
 nperms = 2L,
 beta_est = NULL,
  resid_only = FALSE,
 output_all = FALSE,
  verbose = FALSE
)
```

## Arguments

x	Input matrix with nobs rows, each an observation vector.
У	Response vector.
resid_type	Type of residuals used for the test (see details below). Use Lasso when the null model is high-dimensional; otherwise use OLS.
test	Type of departure from the linear model to test for (see details below). Ignored if RPfunction is given.
x_alt	If test is group, this gives the set of variables whose significance we wish to ascertain, after controlling for those in x. If RPfunction is given, it is the input matrix passed to the function RPfunction.
RPfunction	A residual prediction (RP) function that must permit calling as RPfunction( $x_alt$ , resid) where resid is a numeric vector with nobs components. The output must be either a single number or a numeric vector (in the latter case RPfunction would encode a number of RP functions).

В	The number of bootstrap samples to use - note the p-value produced will always be at least 1/B.
rand_gen	A function to generate the simulated errors up to an unknown scale factor. It must permit calling as rand_gen(nobs*B). Determines the form of errors in the null model. The default rnorm equates to a null of a (sparse) Gaussian linear model. Setting rand_gen=NULL resamples residuals to generate simulated errors and approximates a null of i.i.d. errors with unknown distribution.
noise_matrix	An optional matrix whose columns are the simulated errors to use. Note that B and rand_gen will be ignored if this is supplied.
mc.cores	The number of cores to use. Will always be 1 in Windows.
nfolds	Number of folds to use when performing cross-validation to obtain beta_est, the initial estimate of the vector of regression coefficients, via Lasso estimation.
nperms	Number of permutations of the data for which nfolds cross-validation is to be performed. Thus in total prediction errors on nfolds*nperms folds are averaged over.
beta_est	An optional user-supplied estimate.
resid_only	If TRUE only outputs the residuals without applying an RP function.
output_all	In addition to the p-value, gives further output (see Value below).
verbose	Whether to print addition information.

#### Details

The function works by first computing residuals from a regression of y on x. Next B sets of errors generated through rand\_gen are added to a signal derived from beta\_est and aritificial residuals are computed. The option resid\_only=TRUE then outputs these residuals along with the original residuals, scaled to have 1\_2-norm squared equal to nobs. The residuals in question are OLS residuals when resid\_type=OLS (case a - for use when the null hypothesis is low-dimensional so the number of columns of x is smaller than nobs-1), and square-root / scaled Lasso residuals otherwise (case b). The options for test then apply different functions to the residuals as described below.

- nonlin In case (a), the test statistic is the RSS (residual sum of squares) of a randomForest fit from regressing the residuals on to x; case (b) is similar but the OOB error is used and the regression is carried out on the equicorrelation set rather than all of x.
- group x\_alt is first residualised with respect to x by (a) OLS or (b) sparse\_proj. Then the RSS from Lasso fits from regressions of the residuals on to x\_alt are used.
- hetero Uses the RSS from Lasso fits from regressions of the squared residuals to the equicorrelation set (b) or all of x (a).

#### Value

When resid\_only=FALSE and output\_all=FALSE, the output is a single p-value. Otherwise, a list with some of the following components is returned (resid\_only=FALSE causes the last two components to be omitted):

p-value p-value

beta\_est estimated vector of regression coefficients beta\_est

- sigma\_est set to 1 when resid\_type=OLS; otherwise the normalised root-RSS derived from beta\_est
  used in generated the simulated errors
- resid scaled residuals
- resid\_sim simulated scaled residuals
- test the test statistic(s) may be a vector if multiple RP functions are being used such as when test=group
- test\_sim a list of simulated test statistics

#### References

Shah, R. D., Buhlmann, P. (2017) *Goodness-of-fit tests for high dimensional linear models* https://rss.onlinelibrary.wiley.com/doi/10.1111/rssb.12234

#### See Also

RPtest\_single and sqrt\_lasso

#### Examples

```
# Testing for nonlinearity
set.seed(1)
x <- scale(matrix(runif(100*200), 100, 200))</pre>
y <- x[, 1] + x[, 1]^4 + rnorm(nrow(x))</pre>
out <- RPtest(x, y, test="nonlin", B=9L, nperms=2, resid_type = "Lasso")</pre>
# Testing significance of a group
y <- x[, 1:5] %*% rep(1, 5) + x[, 151] + rnorm(nrow(x))</pre>
(out <- RPtest(x[, 1:150], y, test="group", x_alt = x[, 151:200], B=9L, nperms=1))
# Testing for heteroscedasticity
x <- scale(matrix(runif(250*100), 250, 100))</pre>
hetero_sig <- x[, 1] + x[, 2]
var_vec <- hetero_sig - min(hetero_sig) + 0.01</pre>
var_vec <- var_vec / mean(var_vec)</pre>
sd_vec <- sqrt(var_vec)</pre>
y <- x[, 1:5] %*% rep(1, 5) + sd_vec*rnorm(nrow(x))</pre>
(out <- RPtest(x, y, test="hetero", B=9L, nperms=1))</pre>
```

RPtest\_single Test significance of single predictors

#### Description

Compute p-values for the significance of each variable in x.

#### Usage

```
RPtest_single(x, y, x_alt, B = 100L, rand_gen = rnorm, mc.cores = 1L)
```

## Arguments

х	Input matrix with nobs rows, each an observation vector.
У	Response variable; shoud be a numeric vector.
x_alt	Optional: a matrix with jth column the sparse projection of the jth column of x on all its other columns i.e. the output of sparse_proj. If not supplied this is computed by the function.
В	Number of bootstrap samples. If set to 0, the asymptotic ditribution is used for calibration.
rand_gen	A function to generate the simulated errors up to an unknown scale factor. It must permit calling as rand_gen(nobs*B). Determines the form of errors in each of the null models, though the results are broadly insensitive to this choice. The default rnorm equates to null hypotheses of (sparse) Gaussian linear models. Setting rand_gen=NULL resamples residuals to generate simulated errors and approximates nulls of i.i.d. errors with unknown distributions.
mc.cores	Number of cores to use.

## Value

A vector of p-values for each variable.

#### References

Shah, R. D., Buhlmann, P. (2017) *Goodness of fit tests for high-dimensional linear models* https://rss.onlinelibrary.wiley.com/doi/10.1111/rssb.12234

#### See Also

RPtest and sparse\_proj

## Examples

```
x <- scale(matrix(rnorm(50*100), 50, 100))
x <- scale(x)
y <- as.numeric(x[, 1:5] %*% rep(1, 5) + rnorm(nrow(x)))
out <- RPtest_single(x=x, y=y, B=25)</pre>
```

sparse\_proj

Sparse projections using the square-root Lasso

## Description

Regresses each column of x against all others in turn, using the square-root Lasso, and outputs residuals from the regressions. Thus it outputs a form of sparse projection of each column on all others. Alternatively, given two matrices x\_null and x\_alt, it regresses each column of x\_null on x\_alt in a similar fashion.

## sqrt\_lasso

#### Usage

sparse\_proj(x, x\_null, x\_alt, mc.cores = 1L, rescale = FALSE, ...)

#### Arguments

х	Matrix with each row an observation vector. Need not be supplied if $x_alt$ and $x_null$ are given.
x_null	Matrix whose columns are to be regressed on to x_alt.
x_alt	Matrix which the columns of x_null are regressed on to. Must be specified if x_null is given.
mc.cores	The number of cores to use. Will always be 1 in Windows.
rescale	Should the columns of the output be rescaled to have l_2-norm the square-root of the number of observations? Default is FALSE.
	Additional arguments to be passed to sqrt_lasso.

## Value

A matrix where each column gives the residuals.

#### References

A. Belloni, V. Chernozhukov, and L. Wang. (2011) Square-root lasso: pivotal recovery of sparse signals via conic programming. Biometrika, 98(4):791-806.

T. Sun and C.-H. Zhang. (2012) Scaled sparse linear regression. Biometrika, 99(4):879-898.

T. Sun and C.-H. Zhang. (2013) Sparse matrix inversion with scaled lasso. The Journal of Machine Learning Research, 14(1):3385-3418.

## See Also

sqrt\_lasso and RPtest\_single.

#### Examples

```
x <- matrix(rnorm(50*100), 50, 100)
out <- sparse_proj(x)</pre>
```

sqrt\_lasso

Square-root Lasso regression

## Description

Fits a linear model to potentially high-dimensional data using the square-root Lasso, also known as the scaled Lasso. The Lasso path is computed using the **glmnet** package.

#### Usage

```
sqrt_lasso(x, y, lam0 = NULL, exclude = integer(0), output_all = FALSE, ...)
```

#### Arguments

x	Input matrix of dimension nobs by nvars; each row is an observation vector.
У	Response variable; shoud be a numeric vector.
lam0	Tuning parameter for the square-root / scaled Lasso. If left blank (recommended) this is chosen using the method of Sun & Zhang (2013) implemented in the <b>scalreg</b> package.
exclude	Indices of variables to be excluded from the model; default is none.
output_all	In addition to the vector of coefficients, if TRUE, also outputs the intercept, an estimate of the noise standard deviation, and the output of glmnet.
	Additional arguments to be passed to glmnet.

### Details

First the Lasso path is computed using glmnet from **glmnet**. Next the particular point on the path corresponding to the square-root Lasso solution is found. As the path is only computed on a grid of points, the square-root Lasso solution is approximate.

## Value

Either an estimated vector of regression coefficients with nvars components or, if output\_all is true, a list with components

beta the vector of regression coefficents

a0 an intercept term

- sigma\_hat an estimate of the noise standard deviation; this is calculated as square-root of the average residual sums of squares
- glmnet\_obj the fitted glmnet object, an S3 class "glmnet"
- lamda\_index the index of the lambda vector in the glmnet object corresponding to the square-root Lasso solution

## References

A. Belloni, V. Chernozhukov, and L. Wang. (2011) Square-root lasso: pivotal recovery of sparse signals via conic programming. Biometrika, 98(4):791-806.

T. Sun and C.-H. Zhang. (2012) Scaled sparse linear regression. Biometrika, 99(4):879-898.

T. Sun and C.-H. Zhang. (2013) Sparse matrix inversion with scaled lasso. The Journal of Machine Learning Research, 14(1):3385-3418.

## See Also

glmnet and scalreg.

sqrt\_lasso

## Examples

```
x <- matrix(rnorm(100*250), 100, 250)
y <- x[, 1] + x[, 2] + rnorm(100)
out <- sqrt_lasso(x, y)</pre>
```

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