# Package 'PLreg'

January 20, 2025

Title Power Logit Regression for Modeling Bounded Data

Version 0.4.1

Description Power logit regression models for bounded

continuous data, in which the density generator may be normal, Student-t, power exponential, slash, hyperbolic, sinh-normal, or type II logistic. Diagnostic tools associated with the fitted model, such as the residuals, local influence measures, leverage measures, and goodness-of-fit statistics, are implemented. The estimation process follows the maximum likelihood approach and, currently, the package supports two types of estimators: the usual maximum likelihood estimator and the penalized maximum likelihood estimator. More details about power logit regression models are described in Queiroz and Ferrari (2022) <a href="https://www.arxiv.2202.01697">arXiv:2202.01697</a>>.

## URL https://github.com/ffqueiroz/PLreg

License GPL (>= 3)

**Encoding** UTF-8

LazyData true

RoxygenNote 7.2.1

**Imports** BBmisc, EnvStats, Formula, gamlss.dist, GeneralizedHyperbolic, methods, nleqslv, stats, VGAM, zipfR

**Suggests** rmarkdown, knitr, testthat (>= 3.0.0)

Config/testthat/edition 3

**Depends** R (>= 2.10)

NeedsCompilation no

Author Felipe Queiroz [aut, cre], Silvia Ferrari [aut]

Maintainer Felipe Queiroz <ffelipeq@outlook.com>

**Repository** CRAN

Date/Publication 2023-02-16 08:20:07 UTC

## Contents

bodyfat_Aeolus	2
CI.lambda	3
envelope	4
extra.parameter	5
Firm	7
influence	
methodsPLreg	9
PeruVotes	10
PL	11
plot.PLreg	13
PLreg	15
PLregcontrol	20
residuals.PLreg	21
sandwich	22
	24

## Index

bodyfat\_Aeolus

Body Fat of Little Brown Bat

#### Description

A dataset containing the percent body fat of little brown bats sampled in Aeolus Cave, located in East Dorset, Vermont, in the North Eastern United States.

#### Usage

data(bodyfat\_Aeolus)

#### Format

A data frame with 159 rows and 4 variables:

sex sex of the sampled bat, M for masculine and F for feminine.

percentfat percent body fat.

year year the bat was sampled.

days hibernation time, defined as days since the fall equinox.

## Details

The complete dataset was collected by Cheng et al. (2019) in five different regions of the United States. bodyfat\_Aeolus is the subset of the data collected in Aeolus Cave, located in East Dorset, Vermont, in the North Eastern United States.

## Source

https://datadryad.org/stash/dataset/doi:10.5061/dryad.sh487nh

#### CI.lambda

#### References

Cheng TL, Gerson A, Moore MS, et al. (2019) Higher fat stores contribute to persistence of little brown bat populations with white-nose syndrome. *J Anim Ecol.* 88:591-600. https://doi.org/10.1111/1365-2656.12954

## Examples

CI.lambda

Confidence Interval for the Skewness Parameter

#### Description

The CI.lambda function provides a plot of the profile (penalized) likelihood ratio statistics for lambda, useful to obtain confidence intervals for the skewness parameter (see Queiroz and Ferrari (2022)).

## Usage

```
CI.lambda(object, conf.coef = 0.95, lower = NULL, upper = NULL)
```

#### Arguments

object	fitted model object of class "PLreg".
conf.coef	confidence level of the confidence interval. Default is 0.95.
lower	a numeric value representing the lower limit of the interval for the skewness parameter. If lower = NULL, the lower limit is selected by the function.
upper	a numeric value representing the upper limit of the interval for the skewness parameter. If upper = NULL, the upper limit is selected by the function.

## Value

The function returns a plot of the profile penalized likelihood ratio statistics for lambda with a horizontal dashed line, indicating the confidence interval for lambda. It also shows the confidence interval obtained.

## Examples

```
data("PeruVotes")
fitPL <- PLreg(votes ~ HDI | HDI,</pre>
  data = PeruVotes,
  family = "TF", zeta = 5)
CI.lambda(fitPL)
```

envelope	Normal Probability Plots with Simulated Envelope of Residuals for
	PLreg Objects

## Description

envelope is used to display normal probability plots with simulated envelope of residuals for the power logit models. Currently, three types of residuals are supported: quantile, deviance and standardized residuals.

## Usage

```
envelope(
 object,
  type = c("quantile", "deviance", "standardized"),
  rep = 40,
  conf = 0.95,
 xlab,
 ylab,
 main,
 envcol,
 ylim,
 xlim
```

## Arguments

)

object	fitted model object of class "PLreg".
type	character specifying the type of residuals to be used, see residuals.PLreg. Default is type = "standardized".
rep	a positive integer representing the number of iterations to calculate the simulated envelopes. Default is rep=40.
conf	a numeric value in the interval $(0,1)$ that represents the confidence level of the simulated envelopes. Default is conf=0.95.
xlab	character specifying the label for $x$ axis (optional). Default is "Quantile N(0,1)".
ylab	character specifying the label for $y$ axis (optional). Default is the name of the used residual.

4

#### extra.parameter

main	character specifying the overall title for the plot.
envcol	character specifying the color of the envelope.
ylim, xlim	numeric values, specifying the left/lower limit and the right/upper limit of the scale.

## Details

The envelope uses the idea of Atkinson (1985) to create normal probability plots with simulated envelope. Under the correct model, approximately 100\*conf of the residuals are expected to be inside the envelope.

#### Value

envelope returns normal probability plot with simulated envelopes for the residuals.

#### References

Queiroz, F. F. and Ferrari, S. L. P. (2022). Power logit regression for modeling bounded data. *arXiv*:2202.01697.

Atkinson, A. C. (1985) Plots, transformations and regression: an introduction to graphical methods of diagnostic regression analysis. *Oxford Science Publications*, Oxford.

#### See Also

PLreg, residuals.PLreg

#### Examples

extra.parameter Procedure to Select the Extra Parameter for PLreg Objects

#### Description

The extra.parameter function is used to select the extra parameter of some power logit models. It provides plots of -2logLik and the Upsilon measure (see Queiroz and Ferrari (2022)) versus  $\zeta$ , the extra parameter.

## Usage

extra.parameter(object, lower, upper, grid = 10, graph = TRUE)

## Arguments

object	fitted model object of class "PLreg".
lower	a numeric value representing the lower limit of the interval for the extra parameter.
upper	a numeric value representing the upper limit of the interval for the extra parameter.
grid	a positive integer representing the number of points in the plots. Default is grid=10. If grid is less than 10, then grid=10.
graph	logical. If graph = TRUE the plots are shown, if graph = FALSE the plots are not shown. Default is graph = TRUE.

## Value

extra.parameter returns a list with five objects:

zeta.Ups	The selected zeta based on the Upsilon measure.
zeta.loglik	The selected zeta based on -2logLik.
zeta.values	The values of zeta used in the graphs.
Upsilon.values	-2logLik evaluated at each value of zeta.
loglik.values	Upsilon measure evaluated at each value of zeta.

## References

Queiroz, F. F. and Ferrari, S. L. P. (2022). Power logit regression for modeling bounded data. *arXiv*:2202.01697.

### See Also

PLreg

## Examples

data("bodyfat\_Aeolus")

Firm

## Description

A dataset on risk management practices of 73 firms.

#### Usage

data(Firm)

#### Format

A data frame with 73 rows and 7 variables:

firmcost total property and casualty premiums and uninsured losses as a percentage of total assets.

assume per occurrence retention amount as a percentage of total assets.

**cap** indicates that the firm owns a captive insurance company; 1 if the firm uses a captive, 0 otherwise.

sizelog logarithm of total assets.

indcost a measure of the firm's industry risk.

**central** a measure of the importance of the local managers in choosing the amount of risk to be retained.

soph a measure of the degree of importance in using analytical tools.

### Details

The dataset was introduced and analyzed by Schmit and Roth (1990) and is available in the personal web page of Professor E. Frees (Wisconsin School of Business Research). The response variable is FIRMCOST, smaller values of firm cost are attributed to firms that have a good risk management performance.

#### Source

https://instruction.bus.wisc.edu/jfrees/jfreesbooks/Regression%20Modeling/BookWebDec2010/ CSVData/RiskSurvey.csv

#### References

Schmit, J.T. and Roth, K. (1990). Cost effectiveness of risk management practices. *Journal of Risk and Insurance*. 57:455-470.

## Examples

influence

Influence Diagnostics for PLreg Objects

## Description

The influence function provides two influence measures and the generalized leverage for power logit regression models.

#### Usage

```
influence(model, graph = TRUE, ...)
```

#### Arguments

model	fitted model object of class "PLreg".
graph	logical. If graph = TRUE the plots are shown, if graph = FALSE the plots are not shown. Default is graph = TRUE.
	currently not used.

## Value

influence returns a list with three objects:

case.weights	The values of $h_{max}$ eigenvector based on case weights perturbation scheme (see Queiroz and Ferrari (2022)).
totalLI	The total local influence (see Lesaffre and Verbeke (1998))
GL	The diagonal elements of the generalized leverage matrix.

## References

Queiroz, F. F. and Ferrari, S. L. P. (2022). Power logit regression for modeling bounded data. *arXiv*:2202.01697.

#### See Also

PLreg, residuals.PLreg, envelope, plot.PLreg

8

## methodsPLreg

#### Examples

methodsPLreg Methods for PLreg Objects

#### Description

Some S3 Methods for PLreg regression models.

### Usage

```
## S3 method for class 'PLreg'
summary(object, type = "standardized", ...)
## S3 method for class 'PLreg'
print(x, ...)
## S3 method for class 'summary.PLreg'
print(x, ...)
## S3 method for class 'PLreg'
coef(object, ...)
## S3 method for class 'PLreg'
vcov(object, ...)
## S3 method for class 'PLreg'
logLik(object, ...)
## S3 method for class 'PLreg'
model.matrix(object, model = c("median", "dispersion"), ...)
```

## Arguments

object, x	fitted model object of class "PLreg".
type	character specifying the type of residuals to be included in the summary output,
	see residuals.PLreg.

	currently not used.
model	character specifying for which component of the model the coefficients/covariance
	are extracted.

#### Details

A set of methods for objects of class "PLreg", including methods for the functions summary and vcov, which print the estimated coefficients along with some other information and presents the covariance matrix, respectively. The summary also presents the partial Wald tests for the model parameters. Finally, summary returns an object of class "summary.PLreg" containing information to be printed using the print method.

#### See Also

PLreg

## Examples

data("bodyfat\_Aeolus")

PeruVotes

Peru Blank Votes

#### Description

A dataset on the blank votes in the 2006 Peruvian general election.

#### Usage

data(PeruVotes)

#### Format

A data frame with 194 rows and 2 variables:

votes proportion of blank votes in the 2006 Peruvian general election.

HDI Human Development Index.

#### PL

## Details

The dataset was collected by Bayes et al. (2012) and the response variable is votes, proportion of blank votes in the 2006 Peruvian general election. Bayes et al. (2012) analyzed the influence of the Human Development Index (HDI) on the proportion of blank votes using a beta rectangular regression model. Lemonte and Bazan (2015) also analyzed the data using GJS regression models.

#### Source

https://www.undp.org/es/peru

#### References

Bayes, C., Bazan, J. L. and Garcia, C. (2012). A new robust regression model for proportions. *Bayesian Analysis*. 7:771-796

Lemonte, A. J. and Bazan, J. L. (2015). New class of Johnson SB distributions and its associated regression model for rates and proportions. *Biometrical Journal*. 58:727-746.

#### Examples

ΡL

#### Power Logit Distributions

#### Description

Density, distribution function, quantile function and random generation for power logit distributions.

#### Usage

dPL(x, mu, sigma, lambda, zeta = 2, family, log = FALSE)
pPL(q, mu, sigma, lambda, zeta = 2, family, lower.tail = TRUE, log.p = FALSE)
qPL(p, mu, sigma, lambda, zeta = 2, family, lower.tail = TRUE, log.p = FALSE)
rPL(n, mu, sigma, lambda, zeta = 2, family)

## Arguments

x, q	vector of quantiles.
mu	vector of medians.
sigma	vector of dispersion parameters.
lambda	vector of skewness parameters.
zeta	vector of extra parameters.
family	string that specifies the family used to define the power logit distribution. The family is NO, TF, LO, PE, SHN, Hyp and SLASH for normal, Student-t, type II logis- tic, power exponential, sinh-normal, hyperbolic and slash distribution, respec- tively.
log,log.p	logical; if TRUE, probabilities p are given as log(p). Default is FALSE.
lower.tail	logical; if TRUE (default), probabilities are $P(X \le x)$ otherwise, $P(X > x)$ .
р	vector of probabilities.
n	number of observations. If $length(n) > 1$ , the length is taken to be the number required.

## Details

If zeta is not specified, it assumes the default value 2. The power logit distribution has density

$$f(y;\mu,\sigma,\lambda) = \lambda r(z^2) / (\sigma y(1-y^{\lambda})),$$

for  $y \in (0, 1)$ , in which  $z = [logit(y^{\lambda}) - logit(\mu^{\lambda})]/\sigma$ ,  $r(\cdot)$  is the density generator and  $\mu \in (0, 1)$ ,  $\sigma > 0$  and  $\lambda > 0$  are the median, dispersion and skewness of the distribution. It is possible to consider  $\lambda = 0$  to obtain the limiting case, the log-log distribution. This distribution

It is possible to consider  $\lambda = 0$  to obtain the limiting case, the log-log distribution. This distribution has density

$$f(y; \mu, \sigma, \lambda) = r(z^2) / (\sigma y(-log(y))),$$

for  $y \in (0, 1)$ , in which  $z = [-log(-log(y)) - (-log(-log(y)))]/\sigma$ . The family argument defines the density generator  $r(\cdot)$ , which may depend on an extra parameter (zeta).

## Value

dPL gives the density, pPL gives the distribution function, qPL gives the quantile function, and rPL generates random variables.

#### References

Queiroz, F. F. and Ferrari, S. L. P. (2022). Power logit regression for modeling bounded data. *arXiv* preprint arXiv:2202.01697.

#### plot.PLreg

### Examples

```
dPL(0.2, mu = 0.3, sigma = 1, lambda=1, zeta = 2, family = "PE")
mu = 0.3; sigma = 1; lambda = 2
set.seed(1)
PLsample = rPL(1000, mu, sigma, lambda, family = "SN", zeta = 2.5)
hist(PLsample, prob = TRUE, breaks = 15, main = "", las = 1)
curve(dPL(x, mu, sigma, lambda, family = "SN", zeta = 2.5),
      from = 0.01, to = 0.8, add = TRUE, col = "red")
rug(PLsample)
x = seq(0.01, 0.9, 0.01)
y = dPL(x, mu, sigma, lambda, family = "Hyp", zeta = 2)
plot(x, y, type = "l", lwd = 2, las = 1)
x1 = seq(0.01, 0.4, 0.01)
v1 = dPL(x1, mu, sigma, lambda, family = "Hyp", zeta = 2)
polygon(c(x1, 0.4, 0), c(y1, 0, 0), col = "lightblue")
text(mu-0.025, 1, paste("P(Y<0.4) = ",</pre>
                        round(pPL(0.4, mu, sigma, lambda,
                        family = "Hyp",
                        zeta = 2), 2)),
     font = 1, cex = 0.8)
plot(x, pPL(x, mu, sigma, lambda, family = "PE", zeta = 1.3),
     type = "1", las = 1, lwd = 2,
     ylab = expression(P(Y<y)),</pre>
     xlab = "y")
p = pPL(0.5, mu, sigma, lambda, family = "PE", zeta = 1.3)
q = qPL(p, mu, sigma, lambda, family = "PE", zeta = 1.3)
points(q, p, pch = 16, col = 2, cex = 1.5)
text(0.55, 0.83, paste("(", 0.5, ",", round(p, 2), ")"), font = 2,
     cex = 0.8, col = "red")
```

plot.PLreg

Diagnostic Plots for PLreg Objects

#### Description

This function provides plots for diagnostic analysis of power logit regression models.

#### Usage

```
## S3 method for class 'PLreg'
plot(x, which = 1:4, type = "standardized", pch = "+", las = 1, cex = 0.8, ...)
```

## Arguments ×

fitted model object of class "PLreg".

	numeric specifying a subset of plots (numbers between 1 and 7). which = 1:4.	Default is
type	character specifying the type of residuals, see residuals.PLreg. type = "standardized".	Default is
pch, las, cex,		
	graphical parameters (see par)	

## Details

The plot method for PLreg objects provides 7 types of diagnostic plots in the following order.

Residuals vs indexes of obs. An index plot of the residuals versus indexes of observations.

- **Case-weight perturbation** An index plot of local influence based on the case-weight perturbation scheme.
- **Generalized leverage** A dispersion diagram of the generalized leverage versus the predicted values.

Residuals vs linear predictor A dispersion diagram of the residuals versus the linear predictors.

Normal probability plot A normal probability plot of the residuals.

- **Predicted vs observed values** A dispersion diagram of the predicted values versus the observed values.
- **Residuals vs v(z) function** A dispersion diagram of the v(z) function versus the residuals. For some power logit models, the v(z) function may be interpreted as weights in the estimation process. If family = "N0", the v(z) function is constant.

The which argument can be used to select a subset of the implemented plots. Default is which = 1:4.

## Value

plot method for PLreg objects returns 7 types of diagnostic plots.

#### See Also

PLreg, residuals.PLreg, envelope, influence

#### Examples

```
data("Firm")
```

## Description

PLreg is used to fit power logit regression model for continuous and bounded variables via maximum likelihood approach. Both median and dispersion of the response variable are modeled through parametric functions.

#### Usage

```
PLreg(
  formula,
  data,
  subset.
  na.action,
  family = c("NO", "LO", "TF", "PE", "SN", "SLASH", "Hyp"),
  zeta = NULL,
  link = c("logit", "probit", "cloglog", "cauchit", "loglog"),
  link.sigma = NULL,
  type = c("pML", "ML"),
  control = PLreg.control(...),
 model = TRUE,
 y = TRUE,
  x = FALSE,
  . . .
)
PLreg.fit(
  Χ,
  у,
  S = NULL,
  family,
  type = "pML",
  zeta = zeta,
  link = "logit",
  link.sigma = "log",
  control = PLreg.control()
)
```

## Arguments

formula a symbolic description of the model. See details for further information. data, subset, na.action

arguments controlling formula processing via model.frame.

family	a description of the symmetric distribution to be used for generating the power logit model. Supported families include "NO", "LO", "TF", "PE", "Hyp", SHN" and "SLASH", which correspond to the power logit normal, type II logistic, Student- t, power exponential, hyperbolic, sinh-normal, and slash distributions, respectively.
zeta	a numeric value or numeric vector that represents the extra parameter of the distribution. For the PL-NO and PL-LO models, no extra parameter is needed.
link	an optional character that specifies the link function of the median submodel (mu). The "logit", "probit", "cloglog", "cauchit", "loglog" functions are supported. The logit function is the default.
link.sigma	an optional character that specifies the link function of the dispersion submodel (sigma). The "log", "sqrt" functions are supported. The default is log.
type	character specifying the type of estimator for the skewness parameter. Currently, penalized maximum likelihood ("pML") and maximum likelihood ("ML") are supported. If the skewness parameter is fixed, ML type is used.
control	a list of control arguments specified via PLreg.control.
model,y,x	logicals. If TRUE the corresponding components of the fit (model frame, response, model matrix) are returned. For PLreg.fit, y must be the numeric response vector (with values in $(0,1)$ ).
	arguments passed to PLreg.control.
Х	numeric regressor matrix for the median submodel.
S	numeric regressor matrix for the dispersion submodel.

#### Details

The power logit regression models, proposed by Queiroz and Ferrari (2022), is useful in situations when the response variable is continuous and bounded on the unit interval (0, 1). The median and the dispersion parameters are modeled through parametric link functions. The models depend on a skewness parameter (called  $\lambda$ ). When the skewness parameter is fixed and equal to 1, the power logit models coincide with the GJS regression models (Lemonte and Bazan, 2016). Queiroz and Ferrari (2022) suggest using a penalized maximum likelihood method to estimate the parameters. This method is implemented in PLreg by default when  $\lambda$  is not fixed. If convergence is not reached, maximum likelihood estimation is performed. The estimation process uses optim. If no starting values are specified, the PLreg function uses those suggested by Queiroz and Ferrari (2022). This function also fits the log-log regression models by setting  $\lambda$  at zero ( $\lambda = 0$  represents  $\lambda \rightarrow 0^+$ ).

The formulation of the model has the same structure as in the usual functions lm and glm. The argument formula could comprise of three parts (separated by the symbols " " and "|"), namely: observed response variable in the unit interval, predictor of the median submodel, with link function link and predictor of the dispersion submodel, with link.sigma link function. If the model has constant dispersion, the third part may be omitted and the link function for sigma is "log" by default. The skewness parameter lambda may be treated as fixed or not (default). If lambda is fixed, its value must be specified in the control argument.

Some methods are available for objects of class "PLreg", see plot.PLreg, summary.PLreg, coef.PLreg, vcov.PLreg, and residuals.PLreg, for details and other methods.

# PLreg

## Value

PLreg returns an object of class "PLreg" with the following components (the PLreg.fit returns elements up to v).

coefficients	a list with the "median", "dispersion" and "skewness" (if lambda = NULL) co- efficients.
residuals	a vector of the raw residuals (the difference between the observed and the fitted response).
fitted.values	a vector with the fitted values of the median submodel.
optim	a list with the output from optim. When lambda is not fixed, if type = "pML", the output refers to the iterative process of the median and dispersion parameters only and, if type = "ML", on the maximization of the likelihood for all the parameters.
family	a character specifying the family used.
method	the method argument passed to the optim call.
control	the control arguments passed to the optim call.
start	a vector with the starting values used in the iterative process.
nobs	number of observations.
df.null	residual degrees of freedom in the null model (constant median and dispersion), i.e., $n - 3$ .
df.residual	residual degrees of freedom in the fitted model.
lambda	value of the skewness parameter lambda (NULL when lambda is not fixed).
loglik	log-likelihood of the fitted model.
loglikp	penalized profile log-likelihood for lambda. If lambda is equal to zero, loglikp returns 1.
vcov	covariance matrix of all the parameters.
pseudo.r.squar	
	pseudo R-squared value.
Upsilon.zeta	an overall goodness-of-fit measure.
link	a list with elements "median" and "dispersion" containing the link objects for the respective models.
converged	logical indicating successful convergence of the iterative process.
zeta	a numeric specifying the value of zeta used in the estimation process.
type	a character specifying the estimation method used.
v	a vector with the $v(z)$ values for all the observations (see Queiroz and Ferrari(2021)).
call	the original function call.
formula	the formula used.
terms	a list with elements "median", "dispersion" and "full" containing the term objects for the respective models.

levels	a list with elements "median", "dispersion" and "full" containing the levels of the categorical regressors.
contrasts	a list with elements "median" and "dispersion" containing the contrasts corre- sponding to levels from the respective models.
model	the full model frame (if y = TRUE).
У	the response variable (if y = TRUE).
x	a list with elements "median" and "dispersion" with the matrices from the median and dispersion submodels (if $x = TRUE$ ).

#### Author(s)

Francisco Felipe de Queiroz (<ffelipeq@outlook.com>) and Silvia L. P. Ferrari.

#### References

Queiroz, F. F. and Ferrari, S. L. P. (2022). Power logit regression for modeling bounded data. *arXiv*:2202.01697.

Lemonte, A. J. and Bazan, J. L. (2015). New class of Johnson SB distributions and its associated regression model for rates and proportions. *Biometrical Journal*. 58:727-746.

#### See Also

summary.PLreg, PLreg.control, residuals.PLreg

## Examples

```
#### Body fat data
data("bodyfat_Aeolus")
#Initial model with zeta = 2
fit1 <- PLreg(percentfat ~ days + sex + year, data = bodyfat_Aeolus,</pre>
             family = "PE", zeta = 2)
summary(fit1)
# Choosing the best value for zeta
# extra.parameter(fit1, lower = 1, upper = 4, grid = 15)
# Using zeta = 1.7
fit2 <- PLreg(percentfat ~ days + sex + year, data = bodyfat_Aeolus,</pre>
             family = "PE", zeta = 1.7)
summary(fit2)
# Fixing lambda = 1
fit3 <- PLreg(percentfat ~ days + sex + year, data = bodyfat_Aeolus,</pre>
             family = "PE", zeta = 1.7,
             control = PLreg.control(lambda = 1))
summary(fit3)
# Comparing the AIC and Upsilon values between fit2 and fit3
AIC(fit2) < AIC(fit3) # TRUE
```

## PLreg

```
fit2$Upsilon.zeta < fit3$Upsilon.zeta #TRUE</pre>
#### Firm cost data
data("Firm")
fitPL <- PLreg(firmcost ~ sizelog + indcost | sizelog + indcost,</pre>
              data = Firm,
              family = "SLASH",
              zeta = 2.13)
summary(fitPL)
#extra.parameter(fitPL, lower = 1.2, upper = 4, grid = 10)
#plot(fitPL, type = "standardized")
#envelope(fitPL, type = "standardized")
fitPL_wo72 <- PLreg(firmcost ~ sizelog + indcost | sizelog + indcost,</pre>
                    data = Firm[-72,],
                    family = "SLASH",
                    zeta = 2.13)
fitPL_wo15 <- PLreg(firmcost ~ sizelog + indcost | sizelog + indcost,</pre>
                    data = Firm[-15,],
                    family = "SLASH",
                   zeta = 2.13)
fitPL_wo16 <- PLreg(firmcost ~ sizelog + indcost | sizelog + indcost,</pre>
                   data = Firm[-16,],
                    family = "SLASH",
                    zeta = 2.13)
           <- coef(fitPL)[1:3]
coef.mu
coef.mu_wo72 <- coef(fitPL_wo72)[1:3]</pre>
coef.mu_wo15 <- coef(fitPL_wo15)[1:3]</pre>
coef.mu_wo16 <- coef(fitPL_wo16)[1:3]</pre>
plot(Firm$indcost, Firm$firmcost,
    pch = "+",
    xlab = "indcost",
    ylab = "firmcost")
#identify(Firm$indcost, Firm$firmcost)
covariate = matrix(c(rep.int(1, 1000),
                     rep(median(Firm$sizelog), 1000),
                     seq(0, 1.22, length.out = 1000)),
                  ncol = 3)
lines(covariate[,3],
     as.vector(fitPL$link$median$linkinv(covariate%*%coef.mu)),
     type = "1")
lines(covariate[,3],
     as.vector(fitPL$link$median$linkinv(covariate%*%coef.mu_wo72)),
     type = "1", lty = 2, col = "blue")
lines(covariate[,3],
     as.vector(fitPL$link$median$linkinv(covariate%*%coef.mu_wo15)),
     type = "1", lty = 3, col = "red")
lines(covariate[,3],
     as.vector(fitPL$link$median$linkinv(covariate%*%coef.mu_wo16)),
     type = "1", lty = 4, col = "green")
```

PLregcontrol

#### Auxiliary for Controlling PL Fitting

#### Description

Parameters that control fitting of power logit regression models using PLreg.

## Usage

```
PLreg.control(
 lambda = NULL,
 method = "BFGS",
 maxit = 2000,
 trace = FALSE,
 start = NULL,
 ...
)
```

## Arguments

lambda	numeric indicating the value of the skewness parameter lambda (if NULL, lambda will be estimated).
method	character specifying the method argument passed to optim.
maxit, trace,	
	arguments passed to optim
start	an optional vector with starting values for median and dispersion submodels (starting value for lambda must not be included).

#### Details

The PLreg.control controls the fitting process of power logit models. Almost all the arguments are passed on directly to optim, which is used to estimate the parameters. Starting values for median and dispersion submodels may be supplied via start. If the estimation process is to be performed with a fixed skewness parameter, a value must be specified in lambda. If lambda = 0, a log-log regression model will be estimated.

20

#### residuals.PLreg

#### Value

A list with components named as the arguments.

#### See Also

PLreg

#### Examples

residuals.PLreg Residuals Method for PLreg Objects

#### Description

The function provides three types of residuals for power logit regression models: quantile, deviance and standardized.

### Usage

```
## S3 method for class 'PLreg'
residuals(object, type = c("quantile", "deviance", "standardized"), ...)
```

#### Arguments

object	fitted model object of class "PLreg".
type	character specifying the type of residuals to be used.
	currently not used.

#### Details

The *quantile residuals* is based on Dunn and Smyth (1996) idea. The residuals are well-defined for all the distributions in the power logit class and have, approximately, a standard normal distribution in large samples if the model is correctly specified.

The *deviance residuals* are based on the log-likelihood contributions of each observation in the sample. The distribution of this residual is unknown (both exact and asymptotic), except for the power logit normal model, which is, approximately, standard normal.

The *standardized residuals* are a standardized form of the ordinary residual. These residuals take into account the diagonal elements of the H matrix, being useful for detecting leverage observations. The distribution of the standardized residuals is unknown.

#### Value

residuals method for object of class "PLreg" returns a vector with the residuals of the type specified in the type argument.

#### References

Queiroz, F. F. and Ferrari, S. L. P. (2022). Power logit regression for modeling bounded data. *arXiv*:2202.01697.

Dunn, P. K. and Smyth, G. K. (1996) Randomized quantile residuals. *Journal of Computational and Graphical Statistics*, 5:236-244.

## See Also

PLreg, plot.PLreg, envelope, influence

## Examples

```
sandwich
```

Sandwich Variance and Covariance Matrix for PLreg Objects

## Description

The sandwich function provides an estimate for the asymptotic variance and covariance matrix of the parameter estimators of the power logit (or log-log) regression models based on de sandwich estimator (see Queiroz and Ferrari (2022)).

#### Usage

```
sandwich(object)
```

#### Arguments

object fitted model object of class "PLreg".

#### sandwich

## Value

extra.parameter returns a matrix containing the sandwich variance and covariance matrix estimate.

## References

Queiroz, F. F. and Ferrari, S. L. P. (2022). Power logit regression for modeling bounded data. *arXiv*:2202.01697.

## See Also

PLreg

## Examples

```
data("Firm")
```

# Index

\* datasets bodyfat\_Aeolus, 2 Firm,7 PeruVotes, 10 bodyfat\_Aeolus, 2 CI.lambda, 3 coef.PLreg, 16 coef.PLreg (methodsPLreg), 9 dPL (PL), 11 envelope, 4, 8, 14, 22 extra.parameter, 5 Firm, 7 glm, 16 influence, 8, 14, 22 lm, 16 logLik.PLreg (methodsPLreg), 9 methodsPLreg, 9 model.frame, 15 model.matrix.PLreg (methodsPLreg), 9 optim, 16, 20 par, <u>14</u> PeruVotes, 10 PL, 11 plot.PLreg, 8, 13, 16, 22 PLreg, 5, 6, 8, 10, 14, 15, 20-23 PLreg.control, 16, 18 PLreg.control (PLregcontrol), 20 PLreg.fit, 16 PLregcontrol, 20 pPL (PL), 11 print.PLreg (methodsPLreg), 9

print.summary.PLreg(methodsPLreg),9
qPL(PL),11
residuals.PLreg,4,5,8,9,14,16,18,21
rPL(PL),11
sandwich,22
summary,10
summary.PLreg,16,18
summary.PLreg(methodsPLreg),9
vcov,10
vcov.PLreg,16
vcov.PLreg(methodsPLreg),9