

# Package ‘MomTrunc’

January 20, 2025

**Type** Package

**Title** Moments of Folded and Doubly Truncated Multivariate Distributions

**Version** 6.1

**Date** 2024-10-17

**Author** Christian E. Galarza [aut, cre, trl]  
(<<https://orcid.org/0000-0002-4818-6006>>),  
Raymond Kan [ctb] (<<https://orcid.org/0000-0002-0578-9974>>),  
Victor H. Lachos [aut, ths] (<<https://orcid.org/0000-0002-7239-2459>>)

**Maintainer** Christian E. Galarza <cgalarza88@gmail.com>

**Description** It computes arbitrary products moments (mean vector and variance-covariance matrix), for some double truncated (and folded) multivariate distributions. These distributions belong to the family of selection elliptical distributions, which includes well known skewed distributions as the unified skew-t distribution (SUT) and its particular cases as the extended skew-t (EST), skew-t (ST) and the symmetric student-t (T) distribution. Analogous normal cases unified skew-normal (SUN), extended skew-normal (ESN), skew-normal (SN), and symmetric normal (N) are also included. Density, probabilities and random deviates are also offered for these members.

**License** GPL (>= 2)

**Depends** R (>= 3.6.0)

**Imports** Rcpp (>= 1.0.1), mvtnorm (>= 1.0.11), tlrmvnmvt (>= 1.1.0),  
hypergeo

**LinkingTo** Rcpp (>= 1.0.1), RcppArmadillo, mvtnorm

**Suggests** tmvtnorm

**NeedsCompilation** yes

**Repository** CRAN

**Date/Publication** 2024-10-28 21:40:02 UTC

## Contents

MomTrunc-package . . . . .	2
----------------------------	---

cdfFMD . . . . .	3
dprmvESN . . . . .	5
dprmvEST . . . . .	7
dprmvSN . . . . .	8
dprmvST . . . . .	10
MCmeanvarTMD . . . . .	12
meanvarFMD . . . . .	14
meanvarTMD . . . . .	16
momentsFMD . . . . .	18
momentsTMD . . . . .	20
onlymeanTMD . . . . .	22
pmvnormt . . . . .	25

<b>Index</b>	<b>27</b>
--------------	-----------

---

## Description

It computes arbitrary products moments (mean vector and variance-covariance matrix), for some double truncated (and folded) multivariate distributions. These distributions belong to the family of selection elliptical distributions, which includes well known skewed distributions as the unified skew-t distribution (SUT) and its particular cases as the extended skew-t (EST), skew-t (ST) and the symmetric student-t (T) distribution. Analogous normal cases unified skew-normal (SUN), extended skew-normal (ESN), skew-normal (SN), and symmetric normal (N) are also included. Density, probabilities and random deviates are also offered for these members.

## Details

Probabilities can be computed using the functions `pmvSN` and `pmvESN` for the normal cases SN and ESN and, `pmvST` and `pmvEST` for the t cases ST and EST respectively, which offer the option to return the logarithm in base 2 of the probability, useful when the true probability is too small for the machine precision. These functions above use methods in Genz (1992) through the `mvtnorm` package (linked directly to our C++ functions) and Cao et.al. (2019) through the package `t1rmvnmvt`. For the double truncated Student-t cases SUT, EST, ST and T, decimal degrees of freedom are supported. Computation of arbitrary moments are based in the works of Kan & Robotti (2017) and Galarza et.al. (2021,2022a,2022b). Reference for the family of selection-elliptical distributions in this package can be found in Arellano-Valle & Genton (2005).

## Author(s)

Christian E. Galarza [aut, cre, trl] (<<https://orcid.org/0000-0002-4818-6006>>), Raymond Kan [ctb] (<<https://orcid.org/0000-0002-0578-9974>>), Victor H. Lachos [aut, ths] (<<https://orcid.org/0000-0002-7239-2459>>)

Maintainer: Christian E. Galarza <[cgalarza88@gmail.com](mailto:cgalarza88@gmail.com)>

## References

- Arellano-Valle, R. B. & Genton, M. G. (2005). On fundamental skew distributions. *Journal of Multivariate Analysis*, 96, 93-116.
- Cao, J., Genton, M. G., Keyes, D. E., & Turkiyyah, G. M. (2019) "Exploiting Low Rank Covariance Structures for Computing High-Dimensional Normal and Student-t Probabilities" <<https://marcgenton.github.io/2019.CGKT.manuscript.pdf>>.
- Galarza, C. E., Lin, T. I., Wang, W. L., & Lachos, V. H. (2021). On moments of folded and truncated multivariate Student-t distributions based on recurrence relations. *Metrika*, 84(6), 825-850 <doi:10.1007/s00184-020-00802-1>.
- Galarza, C. E., Matos, L. A., Dey, D. K., & Lachos, V. H. (2022a). "On moments of folded and doubly truncated multivariate extended skew-normal distributions." *Journal of Computational and Graphical Statistics*, 1-11 <doi:10.1080/10618600.2021.2000869>.
- Galarza, C. E., Matos, L. A., Castro, L. M., & Lachos, V. H. (2022b). Moments of the doubly truncated selection elliptical distributions with emphasis on the unified multivariate skew-t distribution. *Journal of Multivariate Analysis*, 189, 104944 <doi:10.1016/j.jmva.2021.104944>.
- Genz, A., "Numerical computation of multivariate normal probabilities," *Journal of Computational and Graphical Statistics*, 1, 141-149 (1992) <doi:10.1080/10618600.1992.10477010>.
- Kan, R., & Robotti, C. (2017). On moments of folded and truncated multivariate normal distributions. *Journal of Computational and Graphical Statistics*, 26(4), 930-934.

## See Also

[onlymeanTMD](#), [meanvarTMD](#), [momentsTMD](#), [dmvSN](#), [pmvSN](#), [rmvSN](#), [dmvST](#), [pmvST](#), [rmvST](#)

## Examples

```
a = c(-0.8,-0.7,-0.6)
b = c(0.5,0.6,0.7)
mu = c(0.1,0.2,0.3)
Sigma = matrix(data = c(1,0.2,0.3,0.2,1,0.4,0.3,0.4,1),
               nrow = length(mu),ncol = length(mu),byrow = TRUE)

meanvarTMD(a,b,mu,Sigma,dist="normal") #normal case
meanvarTMD(mu = mu,Sigma = Sigma,lambda = c(-2,0,1),dist="SN") #skew normal with NO truncation
meanvarTMD(a,b,mu,Sigma,lambda = c(-2,0,1),nu = 4.87,dist = "ST") #skew t
momentsTMD(3,a,b,mu,Sigma,nu = 4,dist = "t") #t case, all moments or order <=3
```

## Description

It computes the cumulative distribution function on  $x$  for a folded p-variate Normal, Skew-normal (SN), Extended Skew-normal (ESN) and Student's t-distribution.

## Usage

```
cdfFMD(x, mu, Sigma, lambda = NULL, tau = NULL, dist, nu = NULL)
```

## Arguments

x	vector of length $p$ where the cdf is evaluated.
mu	a numeric vector of length $p$ representing the location parameter.
Sigma	a numeric positive definite matrix with dimension $p \times p$ representing the scale parameter.
lambda	a numeric vector of length $p$ representing the skewness parameter for SN and ESN cases. If $\text{lambda} == 0$ , the ESN/SN reduces to a normal (symmetric) distribution.
tau	It represents the extension parameter for the ESN distribution. If $\text{tau} == 0$ , the ESN reduces to a SN distribution.
dist	represents the folded distribution to be computed. The values are normal, SN , ESN and t for the doubly truncated Normal, Skew-normal, Extended Skew-normal and Student's t-distribution respectively.
nu	It represents the degrees of freedom for the Student's t-distribution.

## Details

Normal case by default, i.e., when  $\text{dist}$  is not provided. Univariate case is also considered, where  $\text{Sigma}$  will be the variance  $\sigma^2$ .

## Value

It returns the distribution value for a single point x.

## Note

Degrees of freedom must be a positive integer. If  $\text{nu} \geq 200$ , Normal case is considered."

## Author(s)

Christian E. Galarza <>cgalarza88@gmail.com>> and Victor H. Lachos <>hlachos@uconn.edu>>  
Maintainer: Christian E. Galarza <>cgalarza88@gmail.com>>

## References

- Galarza, C. E., Lin, T. I., Wang, W. L., & Lachos, V. H. (2021). On moments of folded and truncated multivariate Student-t distributions based on recurrence relations. *Metrika*, 84(6), 825-850 <doi:10.1007/s00184-020-00802-1>.
- Galarza, C. E., Matos, L. A., Dey, D. K., & Lachos, V. H. (2022a). "On moments of folded and doubly truncated multivariate extended skew-normal distributions." *Journal of Computational and Graphical Statistics*, 1-11 <doi:10.1080/10618600.2021.2000869>.
- Galarza, C. E., Matos, L. A., Castro, L. M., & Lachos, V. H. (2022b). Moments of the doubly truncated selection elliptical distributions with emphasis on the unified multivariate skew-t distribution. *Journal of Multivariate Analysis*, 189, 104944 <doi:10.1016/j.jmva.2021.104944>.

**See Also**

[momentsFMD](#), [meanvarFMD](#)

**Examples**

```
mu = c(0.1,0.2,0.3,0.4)
Sigma = matrix(data = c(1,0.2,0.3,0.1,0.2,1,0.4,-0.1,0.3,0.4,1,0.2,0.1,-0.1,0.2,1),
               nrow = length(mu),ncol = length(mu),byrow = TRUE)
cdfFMD(x = c(0.5,0.2,1.0,1.3),mu,Sigma,dist="normal")
cdfFMD(x = c(0.5,0.2,1.0,1.3),mu,Sigma,dist = "t",nu = 4)
cdfFMD(x = c(0.5,0.2,1.0,1.3),mu,Sigma,lambda = c(-2,0,2,1),dist = "SN")
cdfFMD(x = c(0.5,0.2,1.0,1.3),mu,Sigma,lambda = c(-2,0,2,1),tau = 1,dist = "ESN")
```

dprmvESN

*Multivariate Extended-Skew Normal Density, Probabilities and Random Deviates Generator*

**Description**

These functions provide the density function, probabilities and a random number generator for the multivariate extended-skew normal (ESN) distribution with mean vector `mu`, scale matrix `Sigma`, skewness parameter `lambda` and extension parameter `tau`.

**Usage**

```
dmvESN(x,mu=rep(0,length(lambda)),Sigma=diag(length(lambda)),lambda,tau=0)
pmvESN(lower = rep(-Inf,length(lambda)),upper=rep(Inf,length(lambda)),
       mu = rep(0,length(lambda)),Sigma,lambda,tau,log2 = FALSE)
rmvESN(n,mu=rep(0,length(lambda)),Sigma=diag(length(lambda)),lambda,tau=0)
```

**Arguments**

<code>x</code>	vector or matrix of quantiles. If <code>x</code> is a matrix, each row is taken to be a quantile.
<code>n</code>	number of observations.
<code>lower</code>	the vector of lower limits of length $p$ .
<code>upper</code>	the vector of upper limits of length $p$ .
<code>mu</code>	a numeric vector of length $p$ representing the location parameter.
<code>Sigma</code>	a numeric positive definite matrix with dimension $p \times p$ representing the scale parameter.
<code>lambda</code>	a numeric vector of length $p$ representing the skewness parameter for SN and ESN cases. If <code>lambda == 0</code> , the ESN/SN reduces to a normal (symmetric) distribution.
<code>tau</code>	It represents the extension parameter for the ESN distribution. If <code>tau == 0</code> , the ESN reduces to a SN distribution.
<code>log2</code>	a boolean variable, indicating if the log2 result should be returned. This is useful when the true probability is too small for the machine precision.

### Value

`dmvESN` gives the density, `pmvESN` gives the distribution function, and `rmvESN` generates random deviates for the Multivariate Extended-Skew Normal Distribution.

### Author(s)

Christian E. Galarza <[cgalarza88@gmail.com](mailto:cgalarza88@gmail.com)> and Victor H. Lachos <[hlachos@uconn.edu](mailto:hlachos@uconn.edu)>  
Maintainer: Christian E. Galarza <[cgalarza88@gmail.com](mailto:cgalarza88@gmail.com)>

### References

- Galarza, C. E., Lin, T. I., Wang, W. L., & Lachos, V. H. (2021). On moments of folded and truncated multivariate Student-t distributions based on recurrence relations. *Metrika*, 84(6), 825-850 <doi:10.1007/s00184-020-00802-1>.
- Galarza, C. E., Matos, L. A., Dey, D. K., & Lachos, V. H. (2022a). "On moments of folded and doubly truncated multivariate extended skew-normal distributions." *Journal of Computational and Graphical Statistics*, 1-11 <doi:10.1080/10618600.2021.2000869>.
- Galarza, C. E., Matos, L. A., Castro, L. M., & Lachos, V. H. (2022b). Moments of the doubly truncated selection elliptical distributions with emphasis on the unified multivariate skew-t distribution. *Journal of Multivariate Analysis*, 189, 104944 <doi:10.1016/j.jmva.2021.104944>.
- Galarza, C.E., Matos, L.A. and Lachos, V.H. (2022c). An EM algorithm for estimating the parameters of the multivariate skew-normal distribution with censored responses. *Metron*. <doi:10.1007/s40300-021-00227-4>.
- Genz, A., (1992) "Numerical computation of multivariate normal probabilities," *Journal of Computational and Graphical Statistics*, 1, 141-149 <doi:10.1080/10618600.1992.10477010>.

### See Also

[dmvSN](#), [pmvSN](#), [rmvSN](#), [meanvarFMD](#), [meanvarTMD](#), [momentsTMD](#)

### Examples

```
#Univariate case
dmvESN(x = -1, mu = 2, Sigma = 5, lambda = -2, tau = 0.5)
rmvESN(n = 100, mu = 2, Sigma = 5, lambda = -2, tau = 0.5)
#Multivariate case
mu = c(0.1, 0.2, 0.3, 0.4)
Sigma = matrix(data = c(1, 0.2, 0.3, 0.1, 0.2, 1, 0.4, -0.1, 0.3, 0.4, 1, 0.2, 0.1, -0.1, 0.2, 1),
               nrow = length(mu), ncol = length(mu), byrow = TRUE)
lambda = c(-2, 0, 1, 2)
tau = 2
#One observation
dmvESN(x = c(-2, -1, 0, 1), mu, Sigma, lambda, tau)
rmvESN(n = 100, mu, Sigma, lambda, tau)
#Many observations as matrix
x = matrix(rnorm(4*10), ncol = 4, byrow = TRUE)
dmvESN(x = x, mu, Sigma, lambda, tau)

lower = rep(-Inf, 4)
```

```
upper = c(-1,0,2,5)
pmvESN(lower,upper,mu,Sigma,lambda,tau)
```

dprmvEST

*Multivariate Extended-Skew t Density, Probabilities and Random Deviates Generator*

## Description

These functions provide the density function, probabilities and a random number generator for the multivariate extended-skew t (EST) distribution with mean vector `mu`, scale matrix `Sigma`, skewness parameter `lambda`, extension parameter `tau` and degrees of freedom `nu`.

## Usage

```
dmvEST(x,mu=rep(0,length(lambda)),Sigma=diag(length(lambda)),lambda,tau=0,nu)
pmvEST(lower = rep(-Inf,length(lambda)),upper=rep(Inf,length(lambda)),
       mu = rep(0,length(lambda)),Sigma,lambda,tau,nu,log2 = FALSE)
rmvEST(n,mu=rep(0,length(lambda)),Sigma=diag(length(lambda)),lambda,tau,nu)
```

## Arguments

<code>x</code>	vector or matrix of quantiles. If <code>x</code> is a matrix, each row is taken to be a quantile.
<code>n</code>	number of observations.
<code>lower</code>	the vector of lower limits of length $p$ .
<code>upper</code>	the vector of upper limits of length $p$ .
<code>mu</code>	a numeric vector of length $p$ representing the location parameter.
<code>Sigma</code>	a numeric positive definite matrix with dimension $p \times p$ representing the scale parameter.
<code>lambda</code>	a numeric vector of length $p$ representing the skewness parameter for ST and EST cases. If <code>lambda == 0</code> , the EST/ST reduces to a t (symmetric) distribution.
<code>tau</code>	It represents the extension parameter for the EST distribution. If <code>tau == 0</code> , the EST reduces to a ST distribution.
<code>nu</code>	It represents the degrees of freedom of the Student's t-distribution.
<code>log2</code>	a boolean variable, indicating if the log2 result should be returned. This is useful when the true probability is too small for the machine precision.

## Value

`dmvEST` gives the density, `pmvEST` gives the distribution function, and `rmvEST` generates random deviates for the Multivariate Extended-Skew-t Distribution.

## Author(s)

Christian E. Galarza <[cgalaz88@gmail.com](mailto:cgalaz88@gmail.com)> and Victor H. Lachos <[hlachos@uconn.edu](mailto:hlachos@uconn.edu)>  
Maintainer: Christian E. Galarza <[cgalaz88@gmail.com](mailto:cgalaz88@gmail.com)>

## References

- Galarza, C. E., Lin, T. I., Wang, W. L., & Lachos, V. H. (2021). On moments of folded and truncated multivariate Student-t distributions based on recurrence relations. *Metrika*, 84(6), 825-850 <doi:10.1007/s00184-020-00802-1>.
- Galarza, C. E., Matos, L. A., Castro, L. M., & Lachos, V. H. (2022b). Moments of the doubly truncated selection elliptical distributions with emphasis on the unified multivariate skew-t distribution. *Journal of Multivariate Analysis*, 189, 104944 <doi:10.1016/j.jmva.2021.104944>.
- Genz, A., (1992) "Numerical computation of multivariate normal probabilities," *Journal of Computational and Graphical Statistics*, 1, 141-149 <doi:10.1080/10618600.1992.10477010>.

## See Also

[dmvST](#), [pmvST](#), [rmvST](#), [meanvarFMD](#), [meanvarTMD](#), [momentsTMD](#)

## Examples

```
#Univariate case
dmvEST(x = -1, mu = 2, Sigma = 5, lambda = -2, tau = 0.5, nu=4)
rmvEST(n = 100, mu = 2, Sigma = 5, lambda = -2, tau = 0.5, nu=4)
#Multivariate case
mu = c(0.1,0.2,0.3,0.4)
Sigma = matrix(data = c(1,0.2,0.3,0.1,0.2,1,0.4,-0.1,0.3,0.4,1,0.2,0.1,-0.1,0.2,1),
               nrow = length(mu),ncol = length(mu),byrow = TRUE)
lambda = c(-2,0,1,2)
tau = 2
#One observation
dmvEST(x = c(-2,-1,0,1),mu,Sigma,lambda,tau,nu=4)
rmvEST(n = 100, mu, Sigma, lambda, tau, nu=4)
#Many observations as matrix
x = matrix(rnorm(4*10),ncol = 4,byrow = TRUE)
dmvEST(x = x, mu, Sigma, lambda, tau, nu=4)

lower = rep(-Inf,4)
upper = c(-1,0,2,5)
pmvEST(lower,upper, mu, Sigma, lambda, tau, nu=4)
```

## Description

These functions provide the density function and a random number generator for the multivariate skew normal (SN) distribution with mean vector `mu`, scale matrix `Sigma` and skewness parameter `lambda`.

## Usage

```
dmvSN(x, mu=rep(0, length(lambda)), Sigma=diag(length(lambda)), lambda)
pmvSN(lower = rep(-Inf, length(lambda)), upper=rep(Inf, length(lambda)),
      mu = rep(0, length(lambda)), Sigma, lambda, log2 = FALSE)
rmvSN(n, mu=rep(0, length(lambda)), Sigma=diag(length(lambda)), lambda)
```

## Arguments

<code>x</code>	vector or matrix of quantiles. If <code>x</code> is a matrix, each row is taken to be a quantile.
<code>n</code>	number of observations.
<code>lower</code>	the vector of lower limits of length $p$ .
<code>upper</code>	the vector of upper limits of length $p$ .
<code>mu</code>	a numeric vector of length $p$ representing the location parameter.
<code>Sigma</code>	a numeric positive definite matrix with dimension $p \times p$ representing the scale parameter.
<code>lambda</code>	a numeric vector of length $p$ representing the skewness parameter for SN and SN cases. If <code>lambda == 0</code> , the SN/SN reduces to a normal (symmetric) distribution.
<code>log2</code>	a boolean variable, indicating if the log2 result should be returned. This is useful when the true probability is too small for the machine precision.

## Value

`dmvSN` gives the density, `pmvSN` gives the distribution function, and `rmvSN` generates random deviates for the Multivariate Skew-normal Distribution.

## Author(s)

Christian E. Galarza <>cgalarza88@gmail.com<> and Victor H. Lachos <>hlachos@uconn.edu<>  
Maintainer: Christian E. Galarza <>cgalarza88@gmail.com<>

## References

- Galarza, C. E., Matos, L. A., Dey, D. K., & Lachos, V. H. (2022a). "On moments of folded and doubly truncated multivariate extended skew-normal distributions." *Journal of Computational and Graphical Statistics*, 1-11 <doi:10.1080/10618600.2021.2000869>.
- Galarza, C. E., Matos, L. A., Castro, L. M., & Lachos, V. H. (2022b). Moments of the doubly truncated selection elliptical distributions with emphasis on the unified multivariate skew-t distribution. *Journal of Multivariate Analysis*, 189, 104944 <doi:10.1016/j.jmva.2021.104944>.
- Galarza, C.E., Matos, L.A. and Lachos, V.H. (2022c). An EM algorithm for estimating the parameters of the multivariate skew-normal distribution with censored responses. *Metron*. <doi:10.1007/s40300-021-00227-4>.
- Genz, A., (1992) "Numerical computation of multivariate normal probabilities," *Journal of Computational and Graphical Statistics*, 1, 141-149 <doi:10.1080/10618600.1992.10477010>.

**See Also**

[dmvESN](#), [pmvESN](#), [rmvESN](#), [meanvarFMD](#), [meanvarTMD](#), [momentsTMD](#)

**Examples**

```
#Univariate case
dmvSN(x = -1,mu = 2,Sigma = 5,lambda = -2)
rmvSN(n = 100,mu = 2,Sigma = 5,lambda = -2)
#Multivariate case
mu = c(0.1,0.2,0.3,0.4)
Sigma = matrix(data = c(1,0.2,0.3,0.1,0.2,1,0.4,-0.1,0.3,0.4,1,0.2,0.1,-0.1,0.2,1),
               nrow = length(mu),ncol = length(mu),byrow = TRUE)
lambda = c(-2,0,1,2)
#One observation
dmvSN(x = c(-2,-1,0,1),mu,Sigma,lambda)
rmvSN(n = 100,mu,Sigma,lambda)
#Many observations as matrix
x = matrix(rnorm(4*10),ncol = 4,byrow = TRUE)
dmvSN(x = x,mu,Sigma,lambda)

lower = rep(-Inf,4)
upper = c(-1,0,2,5)
pmvSN(lower,upper,mu,Sigma,lambda)
```

**dprmvST**

*Multivariate Skew t Density, Probabilities and Random Deviates Generator*

**Description**

These functions provide the density function, probabilities and a random number generator for the multivariate skew t (EST) distribution with mean vector *mu*, scale matrix *Sigma*, skewness parameter *lambda* and degrees of freedom *nu*.

**Usage**

```
dmvST(x,mu=rep(0,length(lambda)),Sigma=diag(length(lambda)),lambda,nu)
pmvST(lower = rep(-Inf,length(lambda)),upper=rep(Inf,length(lambda)),
      mu = rep(0,length(lambda)),Sigma,lambda,nu,log2 = FALSE)
rmvST(n,mu=rep(0,length(lambda)),Sigma=diag(length(lambda)),lambda,nu)
```

**Arguments**

- x* vector or matrix of quantiles. If *x* is a matrix, each row is taken to be a quantile.
- n* number of observations.
- lower* the vector of lower limits of length *p*.
- upper* the vector of upper limits of length *p*.

<code>mu</code>	a numeric vector of length $p$ representing the location parameter.
<code>Sigma</code>	a numeric positive definite matrix with dimension $pxp$ representing the scale parameter.
<code>lambda</code>	a numeric vector of length $p$ representing the skewness parameter for ST and EST cases. If <code>lambda == 0</code> , the EST/ST reduces to a t (symmetric) distribution.
<code>nu</code>	It represents the degrees of freedom of the Student's t-distribution.
<code>log2</code>	a boolean variable, indicating if the log2 result should be returned. This is useful when the true probability is too small for the machine precision.

### Value

`dmvST` gives the density, `pmvST` gives the distribution function, and `rmvST` generates random deviates for the Multivariate Skew- $t$  Distribution.

### Author(s)

Christian E. Galarza <[cgalarza88@gmail.com](mailto:cgalarza88@gmail.com)> and Victor H. Lachos <[hlachos@uconn.edu](mailto:hlachos@uconn.edu)>  
Maintainer: Christian E. Galarza <[cgalarza88@gmail.com](mailto:cgalarza88@gmail.com)>

### References

- Galarza, C. E., Lin, T. I., Wang, W. L., & Lachos, V. H. (2021). On moments of folded and truncated multivariate Student-t distributions based on recurrence relations. *Metrika*, 84(6), 825-850 <[doi:10.1007/s00184-020-00802-1](https://doi.org/10.1007/s00184-020-00802-1)>.
- Galarza, C. E., Matos, L. A., Dey, D. K., & Lachos, V. H. (2022a). "On moments of folded and doubly truncated multivariate extended skew-normal distributions." *Journal of Computational and Graphical Statistics*, 1-11 <[doi:10.1080/10618600.2021.2000869](https://doi.org/10.1080/10618600.2021.2000869)>.
- Galarza, C. E., Matos, L. A., Castro, L. M., & Lachos, V. H. (2022b). Moments of the doubly truncated selection elliptical distributions with emphasis on the unified multivariate skew-t distribution. *Journal of Multivariate Analysis*, 189, 104944 <[doi:10.1016/j.jmva.2021.104944](https://doi.org/10.1016/j.jmva.2021.104944)>.
- Genz, A., (1992) "Numerical computation of multivariate normal probabilities," *Journal of Computational and Graphical Statistics*, 1, 141-149 <[doi:10.1080/10618600.1992.10477010](https://doi.org/10.1080/10618600.1992.10477010)>.

### See Also

[dmvST](#), [pmvST](#), [rmvST](#), [meanvarFMD](#), [meanvarTMD](#), [momentsTMD](#)

### Examples

```
#Univariate case
dmvST(x = -1, mu = 2, Sigma = 5, lambda = -2, nu=4)
rmvST(n = 100, mu = 2, Sigma = 5, lambda = -2, nu=4)
#Multivariate case
mu = c(0.1,0.2,0.3,0.4)
Sigma = matrix(data = c(1,0.2,0.3,0.1,0.2,1,0.4,-0.1,0.3,0.4,1,0.2,0.1,-0.1,0.2,1),
               nrow = length(mu), ncol = length(mu), byrow = TRUE)
lambda = c(-2,0,1,2)
#One observation
```

```

dmvST(x = c(-2,-1,0,1),mu,Sigma,lambda,nu=4)
rmvST(n = 100,mu,Sigma,lambda,nu=4)
#Many observations as matrix
x = matrix(rnorm(4*10),ncol = 4,byrow = TRUE)
dmvST(x = x,mu,Sigma,lambda,nu=4)

lower = rep(-Inf,4)
upper = c(-1,0,2,5)
pmvST(lower,upper,mu,Sigma,lambda,nu=4)

```

MCmeanvarTMD

*Monte Carlo Mean and variance for doubly truncated multivariate distributions*

## Description

It computes the Monte Carlo mean vector and variance-covariance matrix for some doubly truncated skew-elliptical distributions. Monte Carlo simulations are performed via slice Sampling. It supports the p-variate Normal, Skew-normal (SN), Extended Skew-normal (ESN) and Unified Skew-normal (SUN) as well as the Student's-t, Skew-t (ST), Extended Skew-t (EST) and Unified Skew-t (SUT) distribution.

## Usage

```
MCmeanvarTMD(lower = rep(-Inf,length(mu)),upper = rep(Inf,length(mu)),mu,Sigma,
,lambda = NULL,tau = NULL,Gamma = NULL,nu = NULL,dist,n = 10000)
```

## Arguments

lower	the vector of lower limits of length $p$ .
upper	the vector of upper limits of length $p$ .
mu	a numeric vector of length $p$ representing the location parameter.
Sigma	a numeric positive definite matrix with dimension $p \times p$ representing the scale parameter.
lambda	a numeric matrix of dimension $p \times q$ representing the skewness/shape matrix parameter for the SUN and SUT distribution. For the ESN and EST distributions ( $q = 1$ ), lambda is a numeric vector of dimension $p$ (see examples at the end of this help). If $\text{all}(\text{lambda} == 0)$ , the SUN/ESN/SN (SUT/EST/ST) reduces to a normal (t) symmetric distribution.
tau	a numeric vector of length $q$ representing the extension parameter for the SUN and SUT distribution. For the ESN and EST distributions, tau is a positive scalar ( $q = 1$ ). Furthermore, if $\text{tau} == 0$ , the ESN (EST) reduces to a SN (ST) distribution.
Gamma	a correlation matrix with dimension $qxq$ . It must be provided only for the SUN and SUT cases. For particular cases SN, ESN, ST and EST, we have that Gamma == 1 (see examples at the end of this help).

nu	It represents the degrees of freedom for the Student's t-distribution being a positive real number.
dist	represents the truncated distribution to be used. The values are normal, SN , ESN and SUN for the doubly truncated Normal, Skew-normal, Extended Skew-normal and Unified-skew normal distributions and, t, ST , EST and SUT for the for the doubly truncated Student-t, Skew-t, Extended Skew-t and Unified skew-t distributions.
n	number of Monte Carlo samples to be generated.

### Value

It returns a list with three elements:

mean	the estimate for the mean vector of length $p$
EYY	the estimate for the second moment matrix of dimensions $p \times p$
varcov	the estimate for the variance-covariance matrix of dimensions $p \times p$

### Author(s)

Christian E. Galarza <<cgalarza88@gmail.com>> and Victor H. Lachos <<hlachos@uconn.edu>>  
Maintainer: Christian E. Galarza <<cgalarza88@gmail.com>>

### References

- Arellano-Valle, R. B. & Genton, M. G. (2005). On fundamental skew distributions. *Journal of Multivariate Analysis*, 96, 93-116.
- Ho, H. J., Lin, T. I., Chen, H. Y., & Wang, W. L. (2012). Some results on the truncated multivariate t distribution. *Journal of Statistical Planning and Inference*, 142(1), 25-40.

### See Also

[meanvarTMD](#), [rmvSN](#), [rmvESN](#), [rmvST](#), [rmvEST](#)

### Examples

```
a = c(-0.8,-0.7,-0.6)
b = c(0.5,0.6,0.7)
mu = c(0.1,0.2,0.3)
Sigma = matrix(data = c(1,0.2,0.3,0.2,1,0.4,0.3,0.4,1),
               nrow = length(mu),ncol = length(mu),byrow = TRUE)

## Normal case

# Theoretical value
value1 = meanvarTMD(a,b,mu,Sigma,dist="normal")

#MC estimate
MC11 = MCmeanvarTMD(a,b,mu,Sigma,dist="normal") #by defalut n = 10000
```

```

MC12 = MCmeanvarTMD(a,b,mu,Sigma,dist="normal",n = 10^5) #more precision

## Skew-t case

# Theoretical value
value2 = meanvarTMD(a,b,mu,Sigma,lambda = c(-2,0,1),nu = 4,dist = "ST")

#MC estimate
MC21 = MCmeanvarTMD(a,b,mu,Sigma,lambda = c(-2,0,1),nu = 4,dist = "ST")

## More...

MC5 = MCmeanvarTMD(a,b,mu,Sigma,lambda = c(-2,0,1),tau = 1,dist = "ESN")
MC6 = MCmeanvarTMD(a,b,mu,Sigma,lambda = c(-2,0,1),tau = 1,nu = 4,dist = "EST")

#Skew-unified Normal (SUN) and Skew-unified t (SUT) distributions

Lambda = matrix(c(1,0,2,-3,0,-1),3,2) #A skewness matrix p times q
Gamma = matrix(c(1,-0.5,-0.5,1),2,2) #A correlation matrix q times q
tau = c(-1,2) #A vector of extension parameters of dim q

MC7 = MCmeanvarTMD(a,b,mu,Sigma,lambda = Lambda,tau = c(-1,2),Gamma = Gamma,dist = "SUN")
MC8 = MCmeanvarTMD(a,b,mu,Sigma,lambda = Lambda,tau = c(-1,2),Gamma = Gamma,nu = 1,dist = "SUT")

```

**meanvarFMD***Mean and variance for folded multivariate distributions***Description**

It computes the mean vector and variance-covariance matrix for the folded  $p$ -variate Normal, Skew-normal (SN), Extended Skew-normal (ESN) and Student's t-distribution.

**Usage**

```
meanvarFMD(mu,Sigma,lambda = NULL,tau = NULL,nu = NULL,dist)
```

**Arguments**

- |                     |   |
|---------------------|---|
| <code>mu</code>     | a numeric vector of length $p$ representing the location parameter.   |
| <code>Sigma</code>  | a numeric positive definite matrix with dimension $pxp$ representing the scale parameter.   |
| <code>lambda</code> | a numeric vector of length $p$ representing the skewness parameter for SN and ESN cases. If <code>lambda == 0</code> , the ESN/SN reduces to a normal (symmetric) distribution. |
| <code>tau</code>    | It represents the extension parameter for the ESN distribution. If <code>tau == 0</code> , the ESN reduces to a SN distribution.  |

nu	It represents the degrees of freedom for the Student's t-distribution. Must be an integer greater than 1.
dist	represents the folded distribution to be computed. The values are normal, SN , ESN and t for the doubly truncated Normal, Skew-normal, Extended Skew-normal and Student's t-distribution respectively.

## Details

Normal case by default, i.e., when dist is not provided. Univariate case is also considered, where Sigma will be the variance  $\sigma^2$ .

## Value

It returns a list with three elements:

mean	the mean vector of length $p$
EYY	the second moment matrix of dimensions $p \times p$
varcov	the variance-covariance matrix of dimensions $p \times p$

## Warning

The mean can only be provided when nu is larger than 2. On the other hand, the varcov matrix can only be provided when nu is larger than 3.

## Note

Degree of freedom must be a positive integer. If nu  $\geq 200$ , Normal case is considered."

## Author(s)

Christian E. Galarza <>cgalarza88@gmail.com>> and Victor H. Lachos <>hlachos@uconn.edu>>  
Maintainer: Christian E. Galarza <>cgalarza88@gmail.com>>

## References

- Galarza, C. E., Lin, T. I., Wang, W. L., & Lachos, V. H. (2021). On moments of folded and truncated multivariate Student-t distributions based on recurrence relations. *Metrika*, 84(6), 825-850 <doi:10.1007/s00184-020-00802-1>.
- Galarza, C. E., Matos, L. A., Dey, D. K., & Lachos, V. H. (2022a). "On moments of folded and doubly truncated multivariate extended skew-normal distributions." *Journal of Computational and Graphical Statistics*, 1-11 <doi:10.1080/10618600.2021.2000869>.
- Galarza, C. E., Matos, L. A., Castro, L. M., & Lachos, V. H. (2022b). Moments of the doubly truncated selection elliptical distributions with emphasis on the unified multivariate skew-t distribution. *Journal of Multivariate Analysis*, 189, 104944 <doi:10.1016/j.jmva.2021.104944>.

## See Also

[momentsFMD](#), [onlymeanTMD](#), [meanvarTMD](#), [momentsTMD](#), [dmvSN](#), [pmvSN](#), [rmvSN](#), [dmvESN](#), [pmvESN](#), [rmvESN](#), [dmvST](#), [pmvST](#), [rmvST](#), [dmvEST](#), [pmvEST](#), [rmvEST](#)

## Examples

```
mu = c(0.1,0.2,0.3)
Sigma = matrix(data = c(1,0.2,0.3,0.2,1,0.4,0.3,0.4,1),
               nrow = length(mu),ncol = length(mu),byrow = TRUE)
value1 = meanvarFMD(mu,Sigma,dist="normal")
value2 = meanvarFMD(mu,Sigma,nu = 4,dist = "t")
value3 = meanvarFMD(mu,Sigma,lambda = c(-2,0,1),dist = "SN")
value4 = meanvarFMD(mu,Sigma,lambda = c(-2,0,1),tau = 1,dist = "ESN")
```

meanvarTMD

*Mean and variance for doubly truncated multivariate distributions*

## Description

It computes the mean vector and variance-covariance matrix for some doubly truncated skew-elliptical distributions. It supports the  $p$ -variate Normal, Skew-normal (SN), Extended Skew-normal (ESN) and Unified Skew-normal (SUN) as well as the Student's-t, Skew-t (ST), Extended Skew-t (EST) and Unified Skew-t (SUT) distribution.

## Usage

```
meanvarTMD(lower = rep(-Inf,length(mu)),upper = rep(Inf,length(mu)),mu,Sigma
,lambda = NULL,tau = NULL,Gamma = NULL,nu = NULL,dist)
```

## Arguments

lower	the vector of lower limits of length $p$ .
upper	the vector of upper limits of length $p$ .
mu	a numeric vector of length $p$ representing the location parameter.
Sigma	a numeric positive definite matrix with dimension $p \times p$ representing the scale parameter.
lambda	a numeric matrix of dimension $p \times q$ representing the skewness/shape matrix parameter for the SUN and SUT distribution. For the ESN and EST distributions ( $q = 1$ ), lambda is a numeric vector of dimension $p$ (see examples at the end of this help). If $\text{all}(\text{lambda} == 0)$ , the SUN/ESN/SN (SUT/EST/ST) reduces to a normal (t) symmetric distribution.
tau	a numeric vector of length $q$ representing the extension parameter for the SUN and SUT distribution. For the ESN and EST distributions, tau is a positive scalar ( $q = 1$ ). Furthermore, if $\text{tau} == 0$ , the ESN (EST) reduces to a SN (ST) distribution.
Gamma	a correlation matrix with dimension $qxq$ . It must be provided only for the SUN and SUT cases. For particular cases SN, ESN, ST and EST, we have that Gamma == 1 (see examples at the end of this help).
nu	It represents the degrees of freedom for the Student's t-distribution being a positive real number.

**dist** represents the truncated distribution to be used. The values are normal, SN , ESN and SUN for the doubly truncated Normal, Skew-normal, Extended Skew-normal and Unified-skew normal distributions and, t, ST , EST and SUT for the for the doubly truncated Student-t, Skew-t, Extended Skew-t and Unified skew-t distributions.

## Details

Univariate case is also considered, where Sigma will be the variance  $\sigma^2$ . Normal case code is an R adaptation of the Matlab available function `dtnvnmom.m` from Kan & Robotti (2017) and it is used for  $p \leq 3$ . For higher dimensions we use an extension of the algorithm in Vaida (2009).

## Value

It returns a list with three elements:

<b>mean</b>	the mean vector of length $p$
<b>EYY</b>	the second moment matrix of dimensions $p \times p$
<b>varcov</b>	the variance-covariance matrix of dimensions $p \times p$

## Warning

For the  $t$  cases, the algorithm supports degrees of freedom nu  $\leq 2$ .

## Note

If nu  $\geq 300$ , Normal case is considered."

## Author(s)

Christian E. Galarza <[cgalarza88@gmail.com](mailto:cgalarza88@gmail.com)> and Victor H. Lachos <[h.lachos@uconn.edu](mailto:h.lachos@uconn.edu)>  
Maintainer: Christian E. Galarza <[cgalarza88@gmail.com](mailto:cgalarza88@gmail.com)>

## References

- Galarza, C. E., Lin, T. I., Wang, W. L., & Lachos, V. H. (2021). On moments of folded and truncated multivariate Student-t distributions based on recurrence relations. *Metrika*, 84(6), 825-850 <[doi:10.1007/s00184-020-00802-1](https://doi.org/10.1007/s00184-020-00802-1)>.
- Galarza, C. E., Matos, L. A., Dey, D. K., & Lachos, V. H. (2022a). "On moments of folded and doubly truncated multivariate extended skew-normal distributions." *Journal of Computational and Graphical Statistics*, 1-11 <[doi:10.1080/10618600.2021.2000869](https://doi.org/10.1080/10618600.2021.2000869)>.
- Galarza, C. E., Matos, L. A., Castro, L. M., & Lachos, V. H. (2022b). Moments of the doubly truncated selection elliptical distributions with emphasis on the unified multivariate skew-t distribution. *Journal of Multivariate Analysis*, 189, 104944 <[doi:10.1016/j.jmva.2021.104944](https://doi.org/10.1016/j.jmva.2021.104944)>.

## See Also

[MCmeanvarTMD](#), [momentsTMD](#), [meanvarFMD](#), [meanvarFMD](#), [momentsFMD](#), [dmvSN](#), [pmvSN](#), [rmvSN](#), [dmvESN](#), [pmvESN](#), [rmvESN](#), [dmvST](#), [pmvST](#), [rmvST](#), [dmvEST](#), [pmvEST](#), [rmvEST](#)

## Examples

```

a = c(-0.8,-0.7,-0.6)
b = c(0.5,0.6,0.7)
mu = c(0.1,0.2,0.3)
Sigma = matrix(data = c(1,0.2,0.3,0.2,1,0.4,0.3,0.4,1),
               nrow = length(mu),ncol = length(mu),byrow = TRUE)

# Theoretical value
value1 = meanvarTMD(a,b,mu,Sigma,dist="normal")

#MC estimate
MC11 = MCmeanvarTMD(a,b,mu,Sigma,dist="normal") #by defalut n = 10000
MC12 = MCmeanvarTMD(a,b,mu,Sigma,dist="normal",n = 10^5) #more precision

# Now works for for any nu>0
value2 = meanvarTMD(a,b,mu,Sigma,dist = "t",nu = 0.87)

value3 = meanvarTMD(a,b,mu,Sigma,lambda = c(-2,0,1),dist = "SN")
value4 = meanvarTMD(a,b,mu,Sigma,lambda = c(-2,0,1),nu = 4,dist = "ST")
value5 = meanvarTMD(a,b,mu,Sigma,lambda = c(-2,0,1),tau = 1,dist = "ESN")
value6 = meanvarTMD(a,b,mu,Sigma,lambda = c(-2,0,1),tau = 1,nu = 4,dist = "EST")

#Skew-unified Normal (SUN) and Skew-unified t (SUT) distributions

Lambda = matrix(c(1,0,2,-3,0,-1),3,2) #A skewness matrix p times q
Gamma = matrix(c(1,-0.5,-0.5,1),2,2) #A correlation matrix q times q
tau = c(-1,2) #A vector of extension parameters of dim q

value7 = meanvarTMD(a,b,mu,Sigma,lambda = Lambda,tau = c(-1,2),Gamma = Gamma,dist = "SUN")
value8 = meanvarTMD(a,b,mu,Sigma,lambda = Lambda,tau = c(-1,2),Gamma = Gamma,nu = 4,dist = "SUT")

#The ESN and EST as particular cases of the SUN and SUT for q=1

Lambda = matrix(c(-2,0,1),3,1)
Gamma = 1
value9 = meanvarTMD(a,b,mu,Sigma,lambda = Lambda,tau = 1,Gamma = Gamma,dist = "SUN")
value10 = meanvarTMD(a,b,mu,Sigma,lambda = Lambda,tau = 1,Gamma = Gamma,nu = 4,dist = "SUT")

round(value5$varcov,2) == round(value9$varcov,2)
round(value6$varcov,2) == round(value10$varcov,2)

```

## Description

It computes the kappa-th order moments for the folded p-variate Normal, Skew-normal (SN), Extended Skew-normal (ESN) and Student's t-distribution. It also output other lower moments involved in the recurrence approach.

## Usage

```
momentsFMD(kappa, mu, Sigma, lambda = NULL, tau = NULL, nu = NULL, dist)
```

## Arguments

kappa	moments vector of length $p$ . All its elements must be integers greater or equal to 0. For the Student's-t case, kappa can be a scalar representing the order of the moment.
mu	a numeric vector of length $p$ representing the location parameter.
Sigma	a numeric positive definite matrix with dimension $p \times p$ representing the scale parameter.
lambda	a numeric vector of length $p$ representing the skewness parameter for SN and ESN cases. If $\lambda = 0$ , the ESN/SN reduces to a normal (symmetric) distribution.
tau	It represents the extension parameter for the ESN distribution. If $\tau = 0$ , the ESN reduces to a SN distribution.
nu	It represents the degrees of freedom for the Student's t-distribution. Must be an integer greater than 1.
dist	represents the folded distribution to be computed. The values are normal, SN, ESN and t for the doubly truncated Normal, Skew-normal, Extended Skew-normal and Student's t-distribution respectively.

## Details

Univariate case is also considered, where Sigma will be the variance  $\sigma^2$ .

## Value

A data frame containing  $p + 1$  columns. The  $p$  first containing the set of combinations of exponents summing up to kappa and the last column containing the the expected value. Normal cases (ESN, SN and normal) return  $\text{prod}(\kappa) + 1$  moments while the Student's t-distribution case returns all moments of order up to kappa. See example section.

## Warning

For the Student-t cases, including ST and EST, kappa- $th$  order moments exist only for  $\kappa < \nu$ .

## Note

Degrees of freedom must be a positive integer. If  $\nu \geq 300$ , Normal case is considered."

### Author(s)

Christian E. Galarza <<cgalarza88@gmail.com>> and Victor H. Lachos <<hlachos@uconn.edu>>  
 Maintainer: Christian E. Galarza <<cgalarza88@gmail.com>>

### References

- Galarza, C. E., Lin, T. I., Wang, W. L., & Lachos, V. H. (2021). On moments of folded and truncated multivariate Student-t distributions based on recurrence relations. *Metrika*, 84(6), 825-850 <doi:10.1007/s00184-020-00802-1>.
- Galarza, C. E., Matos, L. A., Dey, D. K., & Lachos, V. H. (2022a). "On moments of folded and doubly truncated multivariate extended skew-normal distributions." *Journal of Computational and Graphical Statistics*, 1-11 <doi:10.1080/10618600.2021.2000869>.
- Galarza, C. E., Matos, L. A., Castro, L. M., & Lachos, V. H. (2022b). Moments of the doubly truncated selection elliptical distributions with emphasis on the unified multivariate skew-t distribution. *Journal of Multivariate Analysis*, 189, 104944 <doi:10.1016/j.jmva.2021.104944>.

### See Also

[meanvarFMD](#), [onlymeanTMD](#), [meanvarTMD](#), [momentsTMD](#), [dmvSN](#), [pmvSN](#), [rmvSN](#), [dmvESN](#), [pmvESN](#), [rmvESN](#), [dmvST](#), [pmvST](#), [rmvST](#), [dmvEST](#), [pmvEST](#), [rmvEST](#)

### Examples

```
mu = c(0.1,0.2,0.3)
Sigma = matrix(data = c(1,0.2,0.3,0.2,1,0.4,0.3,0.4,1),
               nrow = length(mu),ncol = length(mu),byrow = TRUE)
value1 = momentsFMD(c(2,0,1),mu,Sigma,dist="normal")
value2 = momentsFMD(3,mu,Sigma,dist = "t",nu = 7)
value3 = momentsFMD(c(2,0,1),mu,Sigma,lambda = c(-2,0,1),dist = "SN")
value4 = momentsFMD(c(2,0,1),mu,Sigma,lambda = c(-2,0,1),tau = 1,dist = "ESN")

#T case with kappa vector input
value5 = momentsFMD(c(2,0,1),mu,Sigma,dist = "t",nu = 7)
```

### Description

It computes kappa-th order moments for some doubly truncated skew-elliptical distributions. It supports the p-variate Normal, Skew-normal (SN) and Extended Skew-normal (ESN), as well as the Student's-t, Skew-t (ST) and the Extended Skew-t (EST) distribution.

### Usage

```
momentsTMD(kappa,lower = rep(-Inf,length(mu)),upper = rep(Inf,length(mu)),mu,Sigma,
lambda = NULL,tau = NULL,nu = NULL,dist)
```

## Arguments

<code>kappa</code>	moments vector of length $p$ . All its elements must be integers greater or equal to 0. For the Student's-t case, <code>kappa</code> can be a scalar representing the order of the moment.
<code>lower</code>	the vector of lower limits of length $p$ .
<code>upper</code>	the vector of upper limits of length $p$ .
<code>mu</code>	a numeric vector of length $p$ representing the location parameter.
<code>Sigma</code>	a numeric positive definite matrix with dimension $p \times p$ representing the scale parameter.
<code>lambda</code>	a numeric vector of length $p$ representing the skewness parameter for SN and ESN cases. If <code>lambda == 0</code> , the ESN/SN reduces to a normal (symmetric) distribution.
<code>tau</code>	It represents the extension parameter for the ESN distribution. If <code>tau == 0</code> , the ESN reduces to a SN distribution.
<code>nu</code>	It represents the degrees of freedom for the Student's t-distribution being a positive real number.
<code>dist</code>	represents the truncated distribution to be used. The values are <code>normal</code> , <code>SN</code> and <code>ESN</code> for the doubly truncated Normal, Skew-normal and Extended Skew-normal distributions and, <code>t</code> , <code>ST</code> and <code>EST</code> for the for the doubly truncated Student-t, Skew-t and Extended Skew-t distributions.

## Details

Univariate case is also considered, where `Sigma` will be the variance  $\sigma^2$ .

## Value

A data frame containing  $p + 1$  columns. The  $p$  first containing the set of combinations of exponents summing up to `kappa` and the last column containing the the expected value. Normal cases (ESN, SN and normal) return `prod(kappa)+1` moments while the Student's t-distribution case returns all moments of order up to `kappa`. See example section.

## Note

If `nu >= 300`, Normal case is considered."

## Author(s)

Christian E. Galarza <<[cgalarza88@gmail.com](mailto:cgalarza88@gmail.com)>> and Victor H. Lachos <<[hlachos@uconn.edu](mailto:hlachos@uconn.edu)>>  
Maintainer: Christian E. Galarza <<[cgalarza88@gmail.com](mailto:cgalarza88@gmail.com)>>

## References

Galarza, C. E., Lin, T. I., Wang, W. L., & Lachos, V. H. (2021). On moments of folded and truncated multivariate Student-t distributions based on recurrence relations. *Metrika*, 84(6), 825-850.

Galarza-Morales, C. E., Matos, L. A., Dey, D. K., & Lachos, V. H. (2022a). "On moments of folded and doubly truncated multivariate extended skew-normal distributions." *Journal of Computational and Graphical Statistics*, 1-11 <doi:10.1080/10618600.2021.2000869>.

Galarza, C. E., Matos, L. A., Castro, L. M., & Lachos, V. H. (2022b). Moments of the doubly truncated selection elliptical distributions with emphasis on the unified multivariate skew-t distribution. *Journal of Multivariate Analysis*, 189, 104944 <doi:10.1016/j.jmva.2021.104944>.

Kan, R., & Robotti, C. (2017). On moments of folded and truncated multivariate normal distributions. *Journal of Computational and Graphical Statistics*, 26(4), 930-934.

## See Also

[onlymeanTMD](#), [meanvarTMD](#), [momentsFMD](#), [meanvarFMD](#), [dmvSN](#), [pmvSN](#), [rmvSN](#), [dmvESN](#), [pmvESN](#), [rmvESN](#), [dmvST](#), [pmvST](#), [rmvST](#), [dmvEST](#), [pmvEST](#), [rmvEST](#)

## Examples

```
a = c(-0.8,-0.7,-0.6)
b = c(0.5,0.6,0.7)
mu = c(0.1,0.2,0.3)
Sigma = matrix(data = c(1,0.2,0.3,0.2,1,0.4,0.3,0.4,1),
               nrow = length(mu),ncol = length(mu),byrow = TRUE)
value1 = momentsTMD(c(2,0,1),a,b,mu,Sigma,dist="normal")
value2 = momentsTMD(c(2,0,1),a,b,mu,Sigma,dist = "t",nu = 7)
value3 = momentsTMD(c(2,0,1),a,b,mu,Sigma,lambda = c(-2,0,1),dist = "SN")
value4 = momentsTMD(c(2,0,1),a,b,mu,Sigma,lambda = c(-2,0,1),tau = 1,dist = "ESN")

#T cases with kappa scalar (all moments up to 3)
value5 = momentsTMD(3,a,b,mu,Sigma,nu = 7,dist = "t")
value6 = momentsTMD(3,a,b,mu,Sigma,lambda = c(-2,0,1),nu = 7,dist = "ST")
value7 = momentsTMD(3,a,b,mu,Sigma,lambda = c(-2,0,1),tau = 1,nu = 7,dist = "EST")
```

## Description

It computes the mean vector for some doubly truncated skew-elliptical distributions. It supports the p-variate Normal, Skew-normal (SN), Extended Skew-normal (ESN) and Unified Skew-normal (SUN) as well as the Student's-t, Skew-t (ST), Extended Skew-t (EST) and Unified Skew-t (SUT) distribution.

## Usage

```
onlymeanTMD(lower = rep(-Inf, length(mu)),upper = rep(Inf,length(mu)),mu,Sigma,
            lambda = NULL,tau = NULL,Gamma = NULL,nu = NULL,dist)
```

## Arguments

lower	the vector of lower limits of length $p$ .
upper	the vector of upper limits of length $p$ .
mu	a numeric vector of length $p$ representing the location parameter.
Sigma	a numeric positive definite matrix with dimension $p \times p$ representing the scale parameter.
lambda	a numeric vector of length $p$ representing the skewness parameter for SN and ESN cases. If $\text{lambda} == 0$ , the ESN/SN reduces to a normal (symmetric) distribution.
tau	It represents the extension parameter for the ESN distribution. If $\text{tau} == 0$ , the ESN reduces to a SN distribution.
Gamma	a correlation matrix with dimension $qxq$ . It must be provided only for the SUN and SUT cases. For particular cases SN, ESN, ST and EST, we have that $\text{Gamma} == 1$ (see examples at the end of this help).
nu	It represents the degrees of freedom for the Student's t-distribution.
dist	represents the truncated distribution to be used. The values are normal, SN , ESN and SUN for the doubly truncated Normal, Skew-normal, Extended Skew-normal and Unified-skew normal distributions and, t, ST , EST and SUT for the for the doubly truncated Student-t, Skew-t, Extended Skew-t and Unified skew-t distributions.

## Details

Univariate case is also considered, where Sigma will be the variance  $\sigma^2$ . Normal case code is an R adaptation of the Matlab available function `dtnvnmom.m` from Kan & Robotti (2017) and it is used for  $p \leq 3$ . For higher dimensions we use proposal in Galarza (2022b).

## Value

It returns the mean vector of length  $p$ .

## Note

Degrees of freedom must be a positive integer. If  $\text{nu} \geq 300$ , Normal case is considered."

## Author(s)

Christian E. Galarza <[cgalarza88@gmail.com](mailto:cgalarza88@gmail.com)> and Victor H. Lachos <[hlachos@uconn.edu](mailto:hlachos@uconn.edu)>  
Maintainer: Christian E. Galarza <[cgalarza88@gmail.com](mailto:cgalarza88@gmail.com)>

## References

Galarza, C. E., Lin, T. I., Wang, W. L., & Lachos, V. H. (2021). On moments of folded and truncated multivariate Student-t distributions based on recurrence relations. *Metrika*, 84(6), 825-850.

Galarza-Morales, C. E., Matos, L. A., Dey, D. K., & Lachos, V. H. (2022a). "On moments of folded and doubly truncated multivariate extended skew-normal distributions." Journal of Computational and Graphical Statistics, 1-11 <doi:10.1080/10618600.2021.2000869>.

Galarza, C. E., Matos, L. A., Castro, L. M., & Lachos, V. H. (2022b). Moments of the doubly truncated selection elliptical distributions with emphasis on the unified multivariate skew-t distribution. Journal of Multivariate Analysis, 189, 104944 <doi:10.1016/j.jmva.2021.104944>.

Kan, R., & Robotti, C. (2017). On moments of folded and truncated multivariate normal distributions. Journal of Computational and Graphical Statistics, 26(4), 930-934.

## See Also

[momentsTMD](#), [meanvarFMD](#), [momentsFMD](#), [dmvESN](#), [rmvESN](#)

## Examples

```
a = c(-0.8,-0.7,-0.6)
b = c(0.5,0.6,0.7)
mu = c(0.1,0.2,0.3)
Sigma = matrix(data = c(1,0.2,0.3,0.2,1,0.4,0.3,0.4,1),
               nrow = length(mu),ncol = length(mu),byrow = TRUE)
value1 = onlymeanTMD(a,b,mu,Sigma,dist="normal")

# Now works for for any nu>0
value2 = onlymeanTMD(a,b,mu,Sigma,dist = "t",nu = 0.87)

value3 = onlymeanTMD(a,b,mu,Sigma,lambda = c(-2,0,1),dist = "SN")
value4 = onlymeanTMD(a,b,mu,Sigma,lambda = c(-2,0,1),tau = 1,dist = "ESN")
value5 = onlymeanTMD(a,b,mu,Sigma,lambda = c(-2,0,1),tau = 1,nu = 4,dist = "EST")

#Skew-unified Normal (SUN) and Skew-unified t (SUT) distributions

Lambda = matrix(c(1,0,2,-3,0,-1),3,2) #A skewness matrix p times q
Gamma = matrix(c(1,-0.5,-0.5,1),2,2) #A correlation matrix q times q
tau = c(-1,2) #A vector of extension parameters of dim q

value6 = onlymeanTMD(a,b,mu,Sigma,lambda = Lambda,tau = c(-1,2),Gamma = Gamma,dist = "SUN")
value7 = onlymeanTMD(a,b,mu,Sigma,lambda = Lambda,tau = c(-1,2),Gamma = Gamma,nu = 4,dist = "SUT")

#The ESN and EST as particular cases of the SUN and SUT for q=1

Lambda = matrix(c(-2,0,1),3,1)
Gamma = 1
value8 = onlymeanTMD(a,b,mu,Sigma,lambda = Lambda,tau = 1,Gamma = Gamma,dist = "SUN")
value9 = onlymeanTMD(a,b,mu,Sigma,lambda = Lambda,tau = 1,Gamma = Gamma,nu = 4,dist = "SUT")

round(value4,2) == round(value8,2)
round(value5,2) == round(value9,2)
```

---

pmvnormt*Multivariate normal and Student-t probabilities*

---

## Description

Computation of Multivariate normal and Student-t probabilities using the classic Genz method form packages `mvtnorm` and `tlrmvnmvt` packages. In order to save computational effort, it chooses whether to use the function `pmvtnorm` (`pmvt`) from `mvtnorm`, or functions `pmvn` (`pmvt`) from the `tlrmvnmvt` package, depending of the vector size `p`, real or integer degrees of freedom `nu`.

## Usage

```
pmvnormt(lower = rep(-Inf, ncol(sigma)), upper = rep(Inf, ncol(sigma)),
          mean = rep(0, ncol(sigma)), sigma, nu = NULL, uselog2 = FALSE)
```

## Arguments

<code>lower</code>	lower integration limits, a numeric vector of length <code>p</code>
<code>upper</code>	upper integration limits, a numeric vector of length <code>p</code>
<code>mean</code>	the location parameter, a numeric vector of length <code>p</code>
<code>sigma</code>	the scale matrix, a square matrix that matches the length of ‘ <code>lower</code> ’
<code>nu</code>	degrees of freedom, a positive real number. If <code>NULL</code> , normal case is considered
<code>uselog2</code>	a boolean variable, indicating if the log2 result should be returned. This is useful when the true probability is too small for the machine precision

## Value

The estimated probability or its log2 if `uselog2 == TRUE`

## Note

If `is.null(nu)`, normal case is considered.

## Author(s)

Christian E. Galarza <<[cgalarza88@gmail.com](mailto:cgalarza88@gmail.com)>> and Victor H. Lachos <<[hlachos@uconn.edu](mailto:hlachos@uconn.edu)>>  
Maintainer: Christian E. Galarza <<[cgalarza88@gmail.com](mailto:cgalarza88@gmail.com)>>

## References

Genz, A. (1992), "Numerical computation of multivariate normal probabilities," *Journal of Computational and Graphical Statistics*, 1, 141-149.

Cao, J., Genton, M. G., Keyes, D. E., & Turkiiyah, G. M. "Exploiting Low Rank Covariance Structures for Computing High-Dimensional Normal and Student- t Probabilities" (2019) <<https://marcgenton.github.io/2019.CGK>>

**See Also**

[onlymeanTMD](#),[meanvarTMD](#),[momentsFMD](#),[momentsTMD](#),[meanvarFMD](#),[dmvSN](#),[pmvSN](#),[rmvSN](#), [dmvESN](#),[pmvESN](#),[rmvESN](#),  
[dmvST](#),[pmvST](#),[rmvST](#), [dmvEST](#),[pmvEST](#),[rmvEST](#)

**Examples**

```
a = c(-0.8,-0.7,-0.6)
b = c(0.5,0.6,0.7)
mu = c(0.1,0.2,0.3)
Sigma = matrix(data = c(1,0.2,0.3,0.2,1,0.4,0.3,0.4,1),
                nrow = length(mu),ncol = length(mu),byrow = TRUE)

pmvnormt(lower = a,upper = b,mean = mu,sigma = Sigma) #normal case
pmvnormt(lower = a,upper = b,mean = mu,sigma = Sigma,nu = 4.23) #t case
pmvnormt(lower = a,upper = b,mean = mu,sigma = Sigma,nu = 4.23,uselog2 = TRUE)
```

# Index

- \* **Extended**
  - cdfFMD, 3
  - dprmvESN, 5
  - dprmvEST, 7
  - MCmeanvarTMD, 12
  - meanvarFMD, 14
  - meanvarTMD, 16
  - momentsFMD, 18
  - momentsTMD, 20
  - MomTrunc-package, 2
  - onlymeanTMD, 22
- \* **Folded**
  - cdfFMD, 3
  - meanvarFMD, 14
  - momentsFMD, 18
- \* **Monte Carlo**
  - MCmeanvarTMD, 12
- \* **Multivariate**
  - cdfFMD, 3
  - dprmvESN, 5
  - dprmvEST, 7
  - dprmvSN, 8
  - dprmvST, 10
  - MCmeanvarTMD, 12
  - meanvarFMD, 14
  - meanvarTMD, 16
  - momentsFMD, 18
  - momentsTMD, 20
  - MomTrunc-package, 2
  - onlymeanTMD, 22
- \* **Normal**
  - cdfFMD, 3
  - dprmvESN, 5
  - dprmvSN, 8
  - MCmeanvarTMD, 12
  - meanvarFMD, 14
  - meanvarTMD, 16
  - momentsFMD, 18
  - momentsTMD, 20
- \* **MomTrunc-package**, 2
- \* **onlymeanTMD**, 22
- \* **Probability**
  - dprmvESN, 5
  - dprmvEST, 7
  - dprmvSN, 8
  - dprmvST, 10
- \* **Selection**
  - MCmeanvarTMD, 12
  - meanvarTMD, 16
  - momentsTMD, 20
  - MomTrunc-package, 2
- \* **Skew**
  - cdfFMD, 3
  - dprmvESN, 5
  - dprmvEST, 7
  - dprmvSN, 8
  - dprmvST, 10
  - MCmeanvarTMD, 12
  - meanvarFMD, 14
  - meanvarTMD, 16
  - momentsFMD, 18
  - momentsTMD, 20
  - MomTrunc-package, 2
  - onlymeanTMD, 22
- \* **Student's t**
  - cdfFMD, 3
  - MCmeanvarTMD, 12
  - meanvarFMD, 14
  - meanvarTMD, 16
  - momentsFMD, 18
  - momentsTMD, 20
  - MomTrunc-package, 2
  - onlymeanTMD, 22
- \* **Student**
  - dprmvEST, 7
  - dprmvST, 10
- \* **Truncated**
  - MCmeanvarTMD, 12

meanvarTMD, 16  
 momentsTMD, 20  
 MomTrunc-package, 2  
 onlymeanTMD, 22  
**\* Unified**  
 MCmeanvarTMD, 12  
 meanvarTMD, 16  
 momentsTMD, 20  
 MomTrunc-package, 2  
**\* t**  
 dprmvEST, 7  
 dprmvST, 10  
  
 cdfFMD, 3  
  
 dmvESN, 10, 15, 17, 20, 22, 24, 26  
 dmvESN (dprmvESN), 5  
 dmvEST, 15, 17, 20, 22, 26  
 dmvEST (dprmvEST), 7  
 dmvSN, 3, 6, 15, 17, 20, 22, 26  
 dmvSN (dprmvSN), 8  
 dmvST, 3, 8, 11, 15, 17, 20, 22, 26  
 dmvST (dprmvST), 10  
 dprmvESN, 5  
 dprmvEST, 7  
 dprmvSN, 8  
 dprmvST, 10  
  
 MCmeanvarTMD, 12, 17  
 meanvarFMD, 5, 6, 8, 10, 11, 14, 17, 20, 22, 24,  
 26  
 meanvarTMD, 3, 6, 8, 10, 11, 13, 15, 16, 20, 22,  
 26  
 momentsFMD, 5, 15, 17, 18, 22, 24, 26  
 momentsTMD, 3, 6, 8, 10, 11, 15, 17, 20, 20, 24,  
 26  
 MomTrunc (MomTrunc-package), 2  
 MomTrunc-package, 2  
  
 onlymeanTMD, 3, 15, 20, 22, 22, 26  
  
 pmvESN, 2, 10, 15, 17, 20, 22, 26  
 pmvESN (dprmvESN), 5  
 pmvEST, 2, 15, 17, 20, 22, 26  
 pmvEST (dprmvEST), 7  
 pmvnormt, 25  
 pmvSN, 2, 3, 6, 15, 17, 20, 22, 26  
 pmvSN (dprmvSN), 8  
 pmvST, 2, 3, 8, 11, 15, 17, 20, 22, 26