# Package 'BayesSampling'

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Type Package

Title Bayes Linear Estimators for Finite Population

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Description Allows the user to apply the Bayes Linear approach to finite population with the Simple Random Sampling - BLE\_SRS() - and the Stratified Simple Random Sampling design - BLE\_SSRS() - (both without replacement), to the Ratio estimator (using auxiliary information) - BLE\_Ratio() - and to categorical data - BLE\_Categorical(). The Bayes linear estimation approach is applied to a general linear regression model for finite population prediction in BLE\_Reg() and it is also possible to achieve the design based estimators using vague prior distributions. Based on Gonçalves, K.C.M, Moura, F.A.S and Migon, H.S.(2014) <a href="https://www150.statcan.gc.ca/n1/en/catalogue/12-001-X201400111886">https://www150.statcan.gc.ca/n1/en/catalogue/12-001-X201400111886</a>>.

URL https://www150.statcan.gc.ca/n1/en/catalogue/12-001-X201400111886,

https://github.com/pedrosfig/BayesSampling

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BigCity

Full Person-level Population Database

#### Description

This data set corresponds to some socioeconomic variables from 150266 people of a city in a particular year.

#### Usage

data(BigCity)

#### Format

A data.frame with 150266 rows and 12 variables:

- **HHID** The identifier of the household. It corresponds to an alphanumeric sequence (four letters and five digits).
- **PersonID** The identifier of the person within the household. NOTE it is not a unique identifier of a person for the whole population. It corresponds to an alphanumeric sequence (five letters and two digits).
- Stratum Households are located in geographic strata. There are 119 strata across the city.
- **PSU** Households are clustered in cartographic segments defined as primary sampling units (PSU). There are 1664 PSU and they are nested within strata.

**Zone** Segments clustered within strata can be located within urban or rural areas along the city. **Sex** Sex of the person.

Income Per capita monthly income.

Expenditure Per capita monthly expenditure.

Employment A person's employment status.

Poverty This variable indicates whether the person is poor or not. It depends on income.

#### Source

https://CRAN.R-project.org/package=TeachingSampling

#### References

Package 'TeachingSampling'; see BigCity

BLE\_Categorical Bayes Linear Method for Categorical Data

#### Description

Creates the Bayes Linear Estimator for Categorical Data

#### Usage

BLE\_Categorical(ys, n, N, m = NULL, rho = NULL)

#### Arguments

ys	k-vector of sample proportion for each category.
n	sample size.
Ν	total size of the population.
m	k-vector with the prior proportion of each strata. If NULL, sample proportion for each strata will be used (non-informative prior).
rho	matrix with the prior correlation coefficients between two different units within categories. It must be a symmetric square matrix of dimension k (or k-1). If NULL, non-informative prior will be used.

#### Value

A list containing the following components:

- est.prop BLE for the sample proportion of each category
- Vest.prop Variance associated with the above
- Vs.Matrix Vs matrix, as defined by the BLE method (should be a positive-definite matrix)
- R.Matrix R matrix, as defined by the BLE method (should be a positive-definite matrix)

#### Source

https://www150.statcan.gc.ca/n1/en/catalogue/12-001-X201400111886

#### References

Gonçalves, K.C.M, Moura, F.A.S and Migon, H.S. (2014). Bayes Linear Estimation for Finite Population with emphasis on categorical data. Survey Methodology, 40, 15-28.

#### Examples

```
# 2 categories
ys <- c(0.2614, 0.7386)
n <- 153
N <- 15288
m <- c(0.7, 0.3)
rho <- matrix(0.1, 1)
Estimator <- BLE_Categorical(ys,n,N,m,rho)</pre>
Estimator
ys <- c(0.2614, 0.7386)
n <- 153
N <- 15288
m <- c(0.7, 0.3)
rho <- matrix(0.5, 1)</pre>
Estimator <- BLE_Categorical(ys,n,N,m,rho)</pre>
Estimator
# 3 categories
ys <- c(0.2, 0.5, 0.3)
n <- 100
N <- 10000
m <- c(0.4, 0.1, 0.5)
mat <- c(0.4, 0.1, 0.1, 0.1, 0.2, 0.1, 0.1, 0.1, 0.6)
rho <- matrix(mat, 3, 3)</pre>
```

BLE\_Ratio

#### Ratio BLE

#### Description

Creates the Bayes Linear Estimator for the Ratio "estimator"

#### Usage

```
BLE_Ratio(ys, xs, x_nots, m = NULL, v = NULL, sigma = NULL, n = NULL)
```

#### BLE\_Ratio

#### Arguments

ys	vector of sample observations or sample mean (sigma and n parameters will be required in this case).
xs	vector with values for the auxiliary variable of the elements in the sample or sample mean.
x_nots	vector with values for the auxiliary variable of the elements not in the sample.
m	prior mean for the ratio between Y and X. If NULL, mean(ys)/mean(xs) will be used (non-informative prior).
V	prior variance of the ratio between Y and X (bigger than sigma^2). If NULL, it will tend to infinity (non-informative prior).
sigma	prior estimate of variability (standard deviation) of the ratio within the popula- tion. If NULL, sample variance of the ratio will be used.
n	sample size. Necessary only if ys and xs represent sample means (will not be used otherwise).

# Value

A list containing the following components:

- est.beta BLE of Beta
- Vest.beta Variance associated with the above
- est.mean BLE for each individual not in the sample
- Vest.mean Covariance matrix associated with the above
- est.tot BLE for the total
- Vest.tot Variance associated with the above

#### Source

https://www150.statcan.gc.ca/n1/en/catalogue/12-001-X201400111886

#### References

Gonçalves, K.C.M, Moura, F.A.S and Migon, H.S.(2014). Bayes Linear Estimation for Finite Population with emphasis on categorical data. Survey Methodology, 40, 15-28.

#### Examples

```
ys <- c(10,8,6)
xs <- c(5,4,3.1)
x_nots <- c(1,20,13,15,-5)
m <- 2.5
v <- 10
sigma <- 2
Estimator <- BLE_Ratio(ys, xs, x_nots, m, v, sigma)
Estimator</pre>
```

# Same example but informing sample means and sample size instead of sample observations
ys <- mean(c(10,8,6))
xs <- mean(c(5,4,3.1))
n <- 3
x\_nots <- c(1,20,13,15,-5)
m <- 2.5
v <- 10
sigma <- 2
Estimator <- BLE\_Ratio(ys, xs, x\_nots, m, v, sigma, n)
Estimator</pre>

BLE_Reg	General BLE case	
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# Description

Calculates the Bayes Linear Estimator for Regression models (general case)

#### Usage

BLE\_Reg(ys, xs, a, R, Vs, x\_nots, V\_nots)

#### Arguments

ys	response variable of the sample
xs	explicative variable of the sample
а	vector of means from Beta
R	covariance matrix of Beta
Vs	covariance of sample errors
x_nots	values of X for the individuals not in the sample
V_nots	covariance matrix of the individuals not in the sample

#### Value

A list containing the following components:

- est.beta BLE of Beta
- Vest.beta Variance associated with the above
- est.mean BLE of each individual not in the sample
- Vest.mean Covariance matrix associated with the above
- est.tot BLE for the total
- Vest.tot Variance associated with the above

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#### BLE\_SRS

#### Source

https://www150.statcan.gc.ca/n1/en/catalogue/12-001-X201400111886

#### References

Gonçalves, K.C.M, Moura, F.A.S and Migon, H.S. (2014). Bayes Linear Estimation for Finite Population with emphasis on categorical data. Survey Methodology, 40, 15-28.

#### Examples

```
xs <- matrix(c(1,1,1,1,2,3,5,0),nrow=4,ncol=2)
ys <- c(12,17,28,2)
x_nots <- matrix(c(1,1,1,0,1,4),nrow=3,ncol=2)
a <- c(1.5,6)
R <- matrix(c(10,2,2,10),nrow=2,ncol=2)
Vs <- diag(c(1,1,1,1))
V_nots <- diag(c(1,1,1))
Estimator <- BLE_Reg(ys, xs, a, R, Vs, x_nots, V_nots)
Estimator</pre>
```

BLE\_SRS

#### Description

Creates the Bayes Linear Estimator for the Simple Random Sampling design (without replacement)

#### Usage

BLE\_SRS(ys, N, m = NULL, v = NULL, sigma = NULL, n = NULL)

ys	vector of sample observations or sample mean (sigma and n parameters will be required in this case).
Ν	total size of the population.
m	prior mean. If NULL, sample mean will be used (non-informative prior).
V	prior variance of an element from the population (bigger than sigma^2). If NULL, it will tend to infinity (non-informative prior).
sigma	prior estimate of variability (standard deviation) within the population. If NULL, sample variance will be used.
n	sample size. Necessary only if ys represent sample mean (will not be used otherwise).

#### Value

A list containing the following components:

- est.beta BLE of Beta (BLE for every individual)
- Vest.beta Variance associated with the above
- est.mean BLE for each individual not in the sample
- Vest.mean Covariance matrix associated with the above
- est.tot BLE for the total
- Vest.tot Variance associated with the above

#### Source

https://www150.statcan.gc.ca/n1/en/catalogue/12-001-X201400111886

#### References

Gonçalves, K.C.M, Moura, F.A.S and Migon, H.S. (2014). Bayes Linear Estimation for Finite Population with emphasis on categorical data. Survey Methodology, 40, 15-28.

#### Examples

```
ys <- c(5,6,8)
N <- 5
m <- 6
v <- 5
sigma <- 1
Estimator <- BLE_SRS(ys, N, m, v, sigma)
Estimator
```

```
# Same example but informing sample mean and sample size instead of sample observations
ys <- mean(c(5,6,8))
N <- 5
n <- 3
m <- 6
v <- 5
sigma <- 1
Estimator <- BLE_SRS(ys, N, m, v, sigma, n)
Estimator
```

#### Description

Creates the Bayes Linear Estimator for the Stratified Simple Random Sampling design (without replacement)

#### Usage

BLE\_SSRS(ys, h, N, m = NULL, v = NULL, sigma = NULL)

#### Arguments

ys	vector of sample observations or sample mean for each strata (sigma parameter will be required in this case).
h	vector with number of observations in each strata.
Ν	vector with the total size of each strata.
m	vector with the prior mean of each strata. If NULL, sample mean for each strata will be used (non-informative prior).
V	vector with the prior variance of an element from each strata (bigger than sigma^2 for each strata). If NULL, it will tend to infinity (non-informative prior).
sigma	vector with the prior estimate of variability (standard deviation) within each strata of the population. If NULL, sample variance of each strata will be used.

# Value

A list containing the following components:

- est.beta BLE of Beta (BLE for the individuals in each strata)
- Vest.beta Variance associated with the above
- est.mean BLE for each individual not in the sample
- Vest.mean Covariance matrix associated with the above
- est.tot BLE for the total
- Vest.tot Variance associated with the above

# Source

https://www150.statcan.gc.ca/n1/en/catalogue/12-001-X201400111886

#### References

Gonçalves, K.C.M, Moura, F.A.S and Migon, H.S.(2014). Bayes Linear Estimation for Finite Population with emphasis on categorical data. Survey Methodology, 40, 15-28.

#### Examples

```
ys <- c(2,-1,1.5, 6,10, 8,8)
h <- c(3,2,2)
N <- c(5,5,3)
m <- c(0,9,8)
v <- c(3,8,1)
sigma <- c(1,2,0.5)
Estimator <- BLE_SSRS(ys, h, N, m, v, sigma)
Estimator
```

```
# Same example but informing sample means instead of sample observations
y1 <- mean(c(2,-1,1.5))
y2 <- mean(c(6,10))
y3 <- mean(c(8,8))
ys <- c(y1, y2, y3)
h <- c(3,2,2)
N <- c(5,5,3)
m <- c(0,9,8)
v <- c(3,8,1)
sigma <- c(1,2,0.5)
Estimator <- BLE_SSRS(ys, h, N, m, v, sigma)
Estimator
```

С

#### calculates the C factor

# Description

calculates the C factor

#### Usage

C(ys, xs, R, Vs)

#### Arguments

ys	response variable of the sample
XS	explicative variable of the sample
R	covariance matrix of Beta
Vs	covariance of sample errors

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create1

#### Description

creates vector of 1's to be used in the estimators

# Usage

create1(y)

# Arguments

y sample matrix

#### Value

vector of 1's with size equal to the number of observations in the sample

E\_beta

calculates the BLE for Beta

# Description

calculates the BLE for Beta

#### Usage

E\_beta(ys, xs, a, R, Vs)

ys	response variable of the sample
XS	explicative variable of the sample
а	vector of means from Beta
R	covariance matrix of Beta
Vs	covariance of sample errors

E\_theta\_Reg

# Description

calculates the BLE for the individuals not in the sample

# Usage

E\_theta\_Reg(ys, xs, a, R, Vs, x\_nots)

#### Arguments

ys	response variable of the sample
xs	explicative variable of the sample
а	vector of means from Beta
R	covariance matrix of Beta
Vs	covariance of sample errors
x_nots	values of X for the individuals not in the sample

calculates BLE for the total T

# Description

calculates BLE for the total T

# Usage

T\_Reg(ys, xs, a, R, Vs, x\_nots)

ys	response variable of the sample
xs	explicative variable of the sample
а	vector of means from Beta
R	covariance matrix of Beta
Vs	covariance of sample errors
x_nots	values of X for the individuals not in the sample

VT\_Reg

# Description

calculates risk matrix associated with the BLE for for the total T

#### Usage

VT\_Reg(ys, xs, a, R, Vs, x\_nots, V\_nots)

# Arguments

ys	response variable of the sample
XS	explicative variable of the sample
а	vector of means from Beta
R	covariance matrix of Beta
Vs	covariance of sample errors
x_nots	values of X for the individuals not in the sample
V_nots	covariance matrix of the individuals not in the sample

V\_beta

calculates the risk matrix associated with the BLE for Beta

# Description

calculates the risk matrix associated with the BLE for Beta

#### Usage

V\_beta(ys, xs, R, Vs)

ys	response variable of the sample
XS	explicative variable of the sample
R	covariance matrix of Beta
Vs	covariance of sample errors

V\_theta\_Reg

# Description

calculates the risk matrix associated with the BLE for the individuals not in the sample

#### Usage

V\_theta\_Reg(ys, xs, R, Vs, x\_nots, V\_nots)

ys	response variable of the sample
xs	explicative variable of the sample
R	covariance matrix of Beta
Vs	covariance of sample errors
x_nots	values of X for the individuals not in the sample
V_nots	covariance matrix of the individuals not in the sample

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