

iemisc: Open Channel Flow Examples involving Geometric Shapes with the Gauckler-Manning-Strickler Equation

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About the examples

The following examples only cover open channel flow problems using the Gauckler-Manning-Strickler equation (commonly called Manning's equation) [Wikimedia] to calculate the missing parameters and the critical depth.

Other examples using the Gauckler-Manning-Strickler equation can be found at [Open Channel Flow Examples using the Gauckler-Manning-Strickler equation](#) written by the author.

Examples

rectangular cross-section

```
install.load::load_package("iemisc", "iemiscdata", "rivr", "pander")
# load needed packages using the load_package function from the install.load
# package (it is assumed that you have already installed these packages)
```

```
# 1) Practice Problem 14.10 from Mott (pages 391-392)
```

```

# What is the Q (discharge) for this cross-section?

# See nchannel in iemiscdata for the Manning's n table that the following
# example uses Use the normal Manning's n value for Natural streams - minor
# streams (top width at floodstage < 100 ft), Lined or Constructed Channels,
# Concrete, and unfinished.

# The 1st heading is 'Manning's n for Channels' The 2nd heading is 'Natural
# streams - minor streams (top width at floodstage < 100 ft)' The 3rd heading
# is 'Lined or Constructed Channels,' The 4th heading is 'Concrete' The 5th
# heading is 'unfinished'

data(nchannel)
# load the data set nchannel from iemiscdata

nlocation <- grep("unfinished", nchannel$"Type of Channel and Description")
# search for the term 'unfinished' in the 'Type of Channel and Description'
# column in the nchannel data set

nlocation

## [1] 72

n <- nchannel[nlocation, 3] # 3 for column 3 - Normal n
# the value of n will be found in column 3 at the location specified by
# nlocation

n

## [1] 0.017

Q <- Manningrect(b = 3.5, y = 2, Sf = 0.1/100, n = n, units = "SI")

##
## Flow IS in the rough turbulent zone so the Gauckler-Manning-Strickler equation
## is acceptable to use.
##
##
## This is subcritical flow.

# b = 3.5 m, y = 2 m, Sf = 0.1 percent m/m, n = 0.017, units = SI units This
# will solve for Q since it is missing and Q will be in m3/s

# Note: Q (discharge), velocity (V), area (A), wetted perimeter (P), R
# (hydraulic radius), Re (Reynolds number), and Fr (Froude number) are returned
# as a R list

Q

## $Q
## [1] 12.4358
##
## $V
## [1] 1.776542
##

```

```

## $A
## [1] 7
##
## $P
## [1] 7.5
##
## $R
## [1] 0.9333333
##
## $B
## [1] 3.5
##
## $D
## [1] 2
##
## $Re
## [1] 1651619
##
## $Fr
## [1] 0.401144
# What is the critical depth for this given discharge?

critical_depth(Q$Q, 2, 9.80665, 3.5, 0)

## [1] 1.087836
# 2) Problem 1 from Hauser (page 88)

# What is the Sf (slope) for this cross-section?

Sf <- Manningrect(Q = 6.25 * 8 * 14.9, b = 8, y = 6.25, n = 0.01, units = "Eng")

##
## Flow IS in the rough turbulent zone so the Gauckler-Manning-Strickler equation
## is acceptable to use.
##
##
## This is supercritical flow.
# Q = 6.25 ft * 8 ft * 14.9 ft/sec, b = 8 ft, y = 6.25 ft, n = 0.01, units =
# Eng units This will solve for Sf since it is missing and Sf will be in ft/ft

# Note: Sf (slope), velocity (V), area (A), wetted perimeter (P), R (hydraulic
# radius), Re (Reynolds number), and Fr (Froude number) are returned as a R
# list

Sf

## $Sf
## [1] 0.003062629
##
## $V
## [1] 14.9
##
## $A

```

```
## [1] 50
##
## $P
## [1] 20.5
##
## $R
## [1] 2.439024
##
## $B
## [1] 8
##
## $D
## [1] 6.25
##
## $Re
## [1] 3363024
##
## $Fr
## [1] 1.050737
# What is the critical depth for this given discharge?

critical_depth(6.25 * 8 * 14.9, 6.25, 9.80665 * (3937/1200), 8, 0)

## [1] 6.459654
```

trapezoidal cross-section

```
install.load::load_package("iemisc", "iemiscdata", "rivr", "pander")
# load needed packages using the load_package function from the install.load
# package (it is assumed that you have already installed these packages)

# 3) Practice Problem 14.17 from Mott (page 392)

# What is the y (flow depth) for this cross-section?

# See nchannel in iemiscdata for the Manning's n table that the following
# example uses Use the normal Manning's n value for Natural streams - minor
# streams (top width at floodstage < 100 ft), Lined or Constructed Channels,
# Concrete, and unfinished.

# The 1st heading is 'Manning's n for Channels' The 2nd heading is 'Natural
# streams - minor streams (top width at floodstage < 100 ft)' The 3rd heading
# is 'Lined or Constructed Channels,' The 4th heading is 'Concrete' The 5th
# heading is 'unfinished'

data(nchannel)
# load the data set nchannel from iemiscdata

nlocation <- grep("unfinished", nchannel$"Type of Channel and Description")
```

```

# search for the term 'unfinished' in the 'Type of Channel and Description'
# column in the nchannel data set

nlocation

## [1] 72

n <- nchannel[nlocation, 3] # 3 for column 3 - Normal n
# the value of n will be found in column 3 at the location specified by
# nlocation

n

## [1] 0.017

m <- 1/0.8390996

y <- Manningtrap(Q = 15, b = 3, m = m, Sf = 0.1/100, n = n, units = "SI", type = "symmetrical",
  output = "data.table")

##
## Flow IS in the rough turbulent zone so the Gauckler-Manning-Strickler equation
## is acceptable to use.
##
##
## This is subcritical flow.

# Q = 15, b = 3 m, m = 1 / tand(40), Sf = 0.1 percent m/m, n = 0.017, units =
# SI units This will solve for y since it is missing and y will be in m

# Note: Flow depth (y), Flow area (A), Wetted Perimeters (P), Top Width (B),
# Bottom width (b), Hydraulic Radius (R), Hydraulic Depth (D), Flow Mean
# Velocity (V), Flow Discharge (Q), Manning's roughness coefficient (n), Slope
# (Sf), Temperature, Absolute Temperature, Saturated Liquid Density, Absolute
# or Dynamic Viscosity, Kinematic Viscosity, Froude number (Fr), Reynolds
# number (Re), symmetric side slope (m), non-symmetric side slope (m1),
# non-symmetric side slope (m2), Wetted Length (w), Wetted Length for a
# non-symmetric trapezoid (w1), Wetted Length for a non-symmetric trapezoid
# (w2), Section Factor (Z), conveyance (K), Specific Energy (E), Velocity Head
# (Vel_Head), Maximum Shear Stress (taud), Average Shear Stress (tau0) along
# with the associated units are returned in a data.table.

pander(y, missing = "")

```

| Parameters | Normal Value | Units |
|-------------------------------------|--------------|-------------------|
| Flow depth (y) | 1.632 | m |
| Flow area (A) | 8.069 | m ² |
| Wetted Perimeters (P) | 8.077 | m |
| Top Width (B) | 6.89 | m |
| Bottom width (b) | 3 | m |
| Hydraulic Radius (R) | 0.999 | m |
| Hydraulic Depth (D) | 1.171 | m |
| Flow Mean Velocity (V) | 1.859 | m/s |
| Flow Discharge (Q) | 15 | m ³ /s |
| Manning's roughness coefficient (n) | 0.017 | dimensionless |
| Slope (Sf) | 0.001 | m/m |

| Parameters | Normal Value | Units |
|--|--------------|----------------------------|
| Temperature | 20 | degrees Celsius |
| Absolute Temperature | 293.1 | Kelvin |
| Saturated Liquid Density | 998.2 | kg/m ³ |
| Absolute or Dynamic Viscosity | 0.001002 | Pa * s or kg/m*s |
| Kinematic Viscosity | 1.004e-06 | m ² /s |
| Froude number (Fr) | 0.5485 | dimensionless |
| Reynolds number (Re) | 1849747 | dimensionless |
| symmetric side slope (m) | 1.192 | m/m |
| non-symmetric side slope (m1) | | m/m |
| non-symmetric side slope (m2) | | m/m |
| Wetted Length (w) | 2.539 | m |
| Wetted Length for a non-symmetric trapezoid (w1) | | m |
| Wetted Length for a non-symmetric trapezoid (w2) | | m |
| Section Factor (Z) | 8.064 | m |
| conveyance (K) | 474.3 | m ³ /s |
| Specific Energy (E) | 1.808 | m |
| Velocity Head (Vel_Head) | 0.1762 | m |
| Maximum Shear Stress (taud) | 0.01597 | pascal (N/m ²) |
| Average Shear Stress (tau0) | 0.009779 | pascal (N/m ²) |

```
# list for y_list$y access
y_list <- Manningtrap(Q = 15, b = 3, m = m, Sf = 0.1/100, n = n, units = "SI", type = "symmetrical",
  output = "list")

##
## Flow IS in the rough turbulent zone so the Gauckler-Manning-Strickler equation
## is acceptable to use.
##
##
## This is subcritical flow.
# What is the critical depth for this given discharge?

y_c <- Manningtrap_critical(Q = 15, b = 3, m = m, Sf = 0.1/100, n = n, units = "SI",
  type = "symmetrical", critical = "accurate", output = "data.table")

##
## Flow IS in the rough turbulent zone so the Gauckler-Manning-Strickler equation
## is acceptable to use.
##
##
## This is subcritical flow.
# Q = 15, b = 3 m, m = 1 / tand(40), Sf = 0.1 percent m/m, n = 0.017, units =
# SI units This will solve for y since it is missing and y will be in m

# Note: Flow depth (y), Flow area (A), Wetted Perimeters (P), Top Width (B),
# Bottom width (b), Hydraulic Radius (R), Hydraulic Depth (D), Flow Mean
# Velocity (V), Flow Discharge (Q), Manning's roughness coefficient (n), Slope
# (Sf), Temperature, Absolute Temperature, Saturated Liquid Density, Absolute
# or Dynamic Viscosity, Kinematic Viscosity, Froude number (Fr), Reynolds
```

```
# number (Re), symmetric side slope (m), non-symmetric side slope (m1),
# non-symmetric side slope (m2), Wetted Length (w), Wetted Length for a
# non-symmetric trapezoid (w1), Wetted Length for a non-symmetric trapezoid
# (w2), Section Factor (Z), conveyance (K), Specific Energy (E), Velocity Head
# (Vel_Head), Maximum Shear Stress (taud), Average Shear Stress (tau0) along
# with the associated units are returned in a data.table.
```

```
pander(y_c, missing = "")
```

| Parameters | Normal Value | Critical Value | Units |
|--|--------------|----------------|----------------------------|
| Flow depth (y) | 1.632 | 1.366 | m |
| Flow area (A) | 8.069 | 6.321 | m ² |
| Wetted Perimeters (P) | 8.077 | 7.25 | m |
| Top Width (B) | 6.89 | 6.256 | m |
| Bottom width (b) | 3 | | m |
| Hydraulic Radius (R) | 0.999 | 0.872 | m |
| Hydraulic Depth (D) | 1.171 | 1.01 | m |
| Flow Mean Velocity (V) | 1.859 | 3.66 | m/s |
| Flow Discharge (Q) | 15 | 27.347 | m ³ /s |
| Manning's roughness coefficient (n) | 0.017 | | dimensionless |
| Slope (Sf) | 0.001 | 0.002 | m/m |
| Temperature | 20 | | degrees Celsius |
| Absolute Temperature | 293.15 | | Kelvin |
| Saturated Liquid Density | 998.158 | | kg/m ³ |
| Absolute or Dynamic Viscosity | 0.001002078 | | Pa * s or kg/m*s |
| Kinematic Viscosity | 1.003928e-06 | | m ² /s |
| Froude number (Fr) | 0.548 | 1 | dimensionless |
| Reynolds number (Re) | 1849747 | | dimensionless |
| symmetric side slope (m) | 1.192 | | m/m |
| non-symmetric side slope (m1) | | | m/m |
| non-symmetric side slope (m2) | | | m/m |
| Wetted Length (w) | 2.539 | | m |
| Wetted Length for a non-symmetric trapezoid (w1) | | | m |
| Wetted Length for a non-symmetric trapezoid (w2) | | | m |
| Section Factor (Z) | 8.064 | 8.733 | m |
| conveyance (K) | 474.341 | | m ³ /s |
| Specific Energy (E) | 1.808 | 1.653 | m |
| Velocity Head (Vel_Head) | 0.176 | | m |
| Maximum Shear Stress (taud) | 0.016 | | pascal (N/m ²) |
| Average Shear Stress (tau0) | 0.01 | | pascal (N/m ²) |

```
# This can also be done with the critical_depth function from the rivr package
# (below)
```

```
critical_depth(Q = 15, yopt = y_list$y, g = 9.80665, B = 3, SS = m)
```

```
## [1] 1.16226
```

```
# 4) Example 2 from FHWA
```

```
# What is the y (flow depth) for this cross-section?
```

```

y <- Manningtrap(Q = 150, b = 4, m = 2, Sf = 2/100, n = 0.03, units = "Eng", type = "symmetrical",
  output = "data.table")

##
## Flow IS in the rough turbulent zone so the Gauckler-Manning-Strickler equation
## is acceptable to use.
##
##
## This is supercritical flow.
# Q = 150 cfs, b = 4 ft, m = 2, Sf = 2/100 ft/ft, n = 0.030, units = Eng units
# This will solve for y since it is missing and y will be in ft

# Note: Flow depth (y), Flow area (A), Wetted Perimeters (P), Top Width (B),
# Bottom width (b), Hydraulic Radius (R), Hydraulic Depth (D), Flow Mean
# Velocity (V), Flow Discharge (Q), Manning's roughness coefficient (n), Slope
# (Sf), Temperature, Absolute Temperature, Saturated Liquid Density, Absolute
# or Dynamic Viscosity, Kinematic Viscosity, Froude number (Fr), Reynolds
# number (Re), symmetric side slope (m), non-symmetric side slope (m1),
# non-symmetric side slope (m2), Wetted Length (w), Wetted Length for a
# non-symmetric trapezoid (w1), Wetted Length for a non-symmetric trapezoid
# (w2), Section Factor (Z), conveyance (K), Specific Energy (E), Velocity Head
# (Vel_Head), Maximum Shear Stress (taud), Average Shear Stress (tau0) along
# with the associated units are returned in a data.table.

pander(y, missing = "")

```

| Parameters | Normal Value | Units |
|--|--------------|----------------------------|
| Flow depth (y) | 2.152 | ft |
| Flow area (A) | 17.87 | ft ² |
| Wetted Perimeters (P) | 13.62 | ft |
| Top Width (B) | 12.61 | ft |
| Bottom width (b) | 4 | ft |
| Hydraulic Radius (R) | 1.312 | ft |
| Hydraulic Depth (D) | 1.417 | ft |
| Flow Mean Velocity (V) | 8.393 | ft/sec (fps) |
| Flow Discharge (Q) | 150 | ft ³ /sec (cfs) |
| Manning's roughness coefficient (n) | 0.03 | dimensionless |
| Slope (Sf) | 0.02 | ft/ft |
| Temperature | 68 | degrees Fahrenheit |
| Absolute Temperature | 293.2 | Kelvin |
| Saturated Liquid Density | 1.937 | slug/ft ³ |
| Absolute or Dynamic Viscosity | 2.093e-05 | slug/ft*s |
| Kinematic Viscosity | 1.081e-05 | ft ² /s |
| Froude number (Fr) | 1.243 | dimensionless |
| Reynolds number (Re) | 1018833 | dimensionless |
| symmetric side slope (m) | 2 | ft/ft |
| non-symmetric side slope (m1) | | ft/ft |
| non-symmetric side slope (m2) | | ft/ft |
| Wetted Length (w) | 4.812 | ft |
| Wetted Length for a non-symmetric trapezoid (w1) | | ft |

| Parameters | Normal Value | Units |
|--|--------------|----------------------------|
| Wetted Length for a non-symmetric trapezoid (w2) | | ft |
| Section Factor (Z) | 21.41 | ft |
| conveyance (K) | 1061 | ft ³ /sec (cfs) |
| Specific Energy (E) | 3.247 | ft |
| Velocity Head (Vel_Head) | 1.095 | ft |
| Maximum Shear Stress (taud) | 2.682 | lb/ft ² |
| Average Shear Stress (tau0) | 1.635 | lb/ft ² |

```
# list for y_cc_list$y access
y_cc_list <- Manningtrap(Q = 15, b = 3, m = m, Sf = 0.1/100, n = n, units = "SI",
  type = "symmetrical", output = "list")

##
## Flow IS in the rough turbulent zone so the Gauckler-Manning-Strickler equation
## is acceptable to use.
##
##
## This is subcritical flow.
# What is the critical depth for this given discharge?

y_cc <- Manningtrap_critical(Q = 150, b = 4, m = 2, Sf = 2/100, n = 0.03, units = "Eng",
  type = "symmetrical", critical = "accurate", output = "data.table")

##
## Flow IS in the rough turbulent zone so the Gauckler-Manning-Strickler equation
## is acceptable to use.
##
##
## This is supercritical flow.
# Q = 15, b = 3 m, m = 1 / tand(40), Sf = 0.1 percent m/m, n = 0.017, units =
# SI units This will solve for y since it is missing and y will be in m

# Note: Flow depth (y), Flow area (A), Wetted Perimeters (P), Top Width (B),
# Bottom width (b), Hydraulic Radius (R), Hydraulic Depth (D), Flow Mean
# Velocity (V), Flow Discharge (Q), Manning's roughness coefficient (n), Slope
# (Sf), Temperature, Absolute Temperature, Saturated Liquid Density, Absolute
# or Dynamic Viscosity, Kinematic Viscosity, Froude number (Fr), Reynolds
# number (Re), symmetric side slope (m), non-symmetric side slope (m1),
# non-symmetric side slope (m2), Wetted Length (w), Wetted Length for a
# non-symmetric trapezoid (w1), Wetted Length for a non-symmetric trapezoid
# (w2), Section Factor (Z), conveyance (K), Specific Energy (E), Velocity Head
# (Vel_Head), Maximum Shear Stress (taud), Average Shear Stress (tau0) along
# with the associated units are returned in a data.table.

pander(y_cc, missing = "")
```

| Parameters | Normal Value | Critical Value |
|-----------------------|--------------|----------------|
| Flow depth (y) | 2.152 | 3.502 |
| Flow area (A) | 17.871 | 38.533 |
| Wetted Perimeters (P) | 13.624 | 19.661 |

| Parameters | Normal Value | Critical Value |
|--|--------------|----------------|
| Top Width (B) | 12.608 | 18.007 |
| Bottom width (b) | 4 | |
| Hydraulic Radius (R) | 1.312 | 1.96 |
| Hydraulic Depth (D) | 1.417 | 2.14 |
| Flow Mean Velocity (V) | 8.393 | 10.615 |
| Flow Discharge (Q) | 150 | 120.685 |
| Manning's roughness coefficient (n) | 0.03 | |
| Slope (Sf) | 0.02 | 0.003 |
| Temperature | 68 | |
| Absolute Temperature | 293.15 | |
| Saturated Liquid Density | 1.937 | |
| Absolute or Dynamic Viscosity | 2.092885e-05 | |
| Kinematic Viscosity | 1.080619e-05 | |
| Froude number (Fr) | 1.243 | 1 |
| Reynolds number (Re) | 1018833 | |
| symmetric side slope (m) | 2 | |
| non-symmetric side slope (m1) | | |
| non-symmetric side slope (m2) | | |
| Wetted Length (w) | 4.812 | |
| Wetted Length for a non-symmetric trapezoid (w1) | | |
| Wetted Length for a non-symmetric trapezoid (w2) | | |
| Section Factor (Z) | 21.415 | 21.276 |
| conveyance (K) | 1060.675 | |
| Specific Energy (E) | 3.247 | 3.737 |
| Velocity Head (Vel_Head) | 1.095 | |
| Maximum Shear Stress (taud) | 2.682 | |
| Average Shear Stress (tau0) | 1.635 | |

| Units |
|----------------------------|
| ft |
| ft ² |
| ft |
| ft |
| ft |
| ft |
| ft |
| ft/sec (fps) |
| ft ³ /sec (cfs) |
| dimensionless |
| ft/ft |
| degrees Fahrenheit |
| Kelvin |
| slug/ft ³ |
| slug/ft*s |
| ft ² /s |
| dimensionless |
| dimensionless |
| ft/ft |
| ft/ft |

| Units |
|----------------------------|
| ft/ft |
| ft |
| ft |
| ft |
| ft |
| ft ³ /sec (cfs) |
| ft |
| ft |
| lb/ft ² |
| lb/ft ² |

```
# This can also be done with the critical_depth function from the rivr package
# (below)

critical_depth(150, y_cc_list$y, 9.80665 * (3937/1200), 4, 2)

## [1] 2.40582

# 5) Example 2 -- Example Problem 4.5 from the Introduction to Highway
# Hydraulics: Hydraulic Design Series Number 4 Reference

# 'Determine the critical depth in a trapezoidal shaped swale with z = 1, given
# a discharge of 9.2 m3/s and a bottom width, B = 6 m. Also, determine the
# critical velocity.

# What is the critical depth and critical velocity for this cross-section?

y_c45 <- Manningtrap_critical(Q = 9.2, b = 6, m = 1, Sf = 2/100, n = 0.03, units = "SI",
  type = "symmetrical", critical = "accurate", output = "data.table")

##
## Flow IS in the rough turbulent zone so the Gauckler-Manning-Strickler equation
## is acceptable to use.
##
##
## This is supercritical flow.

# Q = 15, b = 3 m, m = 1 / tand(40), Sf = 0.1 percent m/m, n = 0.017, units =
# SI units This will solve for y since it is missing and y will be in m

# Note: Flow depth (y), Flow area (A), Wetted Perimeters (P), Top Width (B),
# Bottom width (b), Hydraulic Radius (R), Hydraulic Depth (D), Flow Mean
# Velocity (V), Flow Discharge (Q), Manning's roughness coefficient (n), Slope
# (Sf), Temperature, Absolute Temperature, Saturated Liquid Density, Absolute
# or Dynamic Viscosity, Kinematic Viscosity, Froude number (Fr), Reynolds
# number (Re), symmetric side slope (m), non-symmetric side slope (m1),
# non-symmetric side slope (m2), Wetted Length (w), Wetted Length for a
# non-symmetric trapezoid (w1), Wetted Length for a non-symmetric trapezoid
# (w2), Section Factor (Z), conveyance (K), Specific Energy (E), Velocity Head
# (Vel_Head), Maximum Shear Stress (taud), Average Shear Stress (tau0) along
# with the associated units are returned in a data.table.

pander(y_c45, missing = "")
```

| Parameters | Normal Value | Critical Value | Units |
|--|--------------|----------------|----------------------------|
| Flow depth (y) | 0.512 | 0.621 | m |
| Flow area (A) | 3.335 | 4.11 | m ² |
| Wetted Perimeters (P) | 7.448 | 7.756 | m |
| Top Width (B) | 7.024 | 7.242 | m |
| Bottom width (b) | 6 | | m |
| Hydraulic Radius (R) | 0.448 | 0.53 | m |
| Hydraulic Depth (D) | 0.475 | 0.568 | m |
| Flow Mean Velocity (V) | 2.759 | 2.467 | m/s |
| Flow Discharge (Q) | 9.2 | 7.196 | m ³ /s |
| Manning's roughness coefficient (n) | 0.03 | | dimensionless |
| Slope (Sf) | 0.02 | 0.011 | m/m |
| Temperature | 20 | | degrees Celsius |
| Absolute Temperature | 293.15 | | Kelvin |
| Saturated Liquid Density | 998.158 | | kg/m ³ |
| Absolute or Dynamic Viscosity | 0.001002078 | | Pa * s or kg/m*s |
| Kinematic Viscosity | 1.003928e-06 | | m ² /s |
| Froude number (Fr) | 1.279 | 1 | dimensionless |
| Reynolds number (Re) | 1230324 | | dimensionless |
| symmetric side slope (m) | 1 | | m/m |
| non-symmetric side slope (m1) | | | m/m |
| non-symmetric side slope (m2) | | | m/m |
| Wetted Length (w) | 0.724 | | m |
| Wetted Length for a non-symmetric trapezoid (w1) | | | m |
| Wetted Length for a non-symmetric trapezoid (w2) | | | m |
| Section Factor (Z) | 1.952 | 2.298 | m |
| conveyance (K) | 65.058 | | m ³ /s |
| Specific Energy (E) | 0.9 | 0.876 | m |
| Velocity Head (Vel_Head) | 0.388 | | m |
| Maximum Shear Stress (taud) | 0.1 | | pascal (N/m ²) |
| Average Shear Stress (tau0) | 0.088 | | pascal (N/m ²) |

```
# Using a trial and error solution, the critical depth is 0.6 m with a critical
# velocity of 2.3 m/s.
```

triangular cross-section

```
install.load::load_package("iemisc", "rivr", "pander")
# load needed packages using the load_package function from the install.load
# package (it is assumed that you have already installed these packages)

# 6) Problem 17 from Hauser (page 89)

# What is the Q (discharge) for this cross-section?

Q <- Manningtri(y = 6, m = 4, Sf = 0.006, n = 0.025, units = "Eng")
```

```

##
## Flow IS in the rough turbulent zone so the Gauckler-Manning-Strickler equation
## is acceptable to use.
##
##
## This is subcritical flow.
# y = 6 ft, m = 4 ft/ft, Sf = 0.006 ft/ft, n = 0.025, units = Eng units This
# will solve for Q since it is missing and Q will be in ft3/s

# Note: Q (discharge), velocity (V), area (A), wetted perimeter (P), R
# (hydraulic radius), Re (Reynolds number), and Fr (Froude number) are returned
# as a R list

Q

## $Q
## [1] 1351.443
##
## $V
## [1] 9.385019
##
## $A
## [1] 144
##
## $P
## [1] 49.47727
##
## $R
## [1] 2.910428
##
## $B
## [1] 48
##
## $D
## [1] 3
##
## $Re
## [1] 2527665
##
## $Fr
## [1] 0.9552611
# What is the critical depth for this given discharge?

critical_depth(Q$Q, 6, 9.80665 * (3937/1200), 0, 4)

## [1] 5.89115
# 7) Example 2 from FHWA

# What is the y (flow depth) for this cross-section?

y <- Manningtri(Q = 150, m = 2, Sf = 2/100, n = 0.03, units = "Eng")

##

```

```

## Flow IS in the rough turbulent zone so the Gauckler-Manning-Strickler equation
## is acceptable to use.
##
##
## This is supercritical flow.
# Q = 150 cfs, m = 2, Sf = 2/100 ft/ft, n = 0.030, units = Eng units This will
# solve for y since it is missing and y will be in ft

# Note: y (flow depth), velocity (V), area (A), wetted perimeter (P), R
# (hydraulic radius), Re (Reynolds number), and Fr (Froude number) are returned
# as a R list

y

## $y
## [1] 2.975079
##
## $V
## [1] 8.473527
##
## $A
## [1] 17.70219
##
## $P
## [1] 13.30496
##
## $R
## [1] 1.330496
##
## $B
## [1] 11.90032
##
## $D
## [1] 1.48754
##
## $Re
## [1] 1043290
##
## $Fr
## [1] 1.224835
# What is the critical depth for this given discharge?

critical_depth(150, y$y, 9.80665 * (3937/1200), 4, 2)

## [1] 2.40582

```

circular cross-section

```
library("iemisc")
```

8) Modified Practice Problem 14.32/14.34 from Mott (page 393)

What is the Q (discharge) for this cross-section?

```
Q <- Manningcirc(d = 375 / 1000, y = 225 / 1000, Sf = 0.12 / 100, n = 0.015, units = "SI")
```

```
##
```

```
## Flow IS in the rough turbulent zone so the Gauckler-Manning-Strickler equation  
## is acceptable to use.
```

```
##
```

```
##
```

```
## This is subcritical flow.
```

```
# d = 375/1000 m, y = 225/1000 m, Sf = 0.12/100 m/m, n = 0.015, units = SI units
```

```
# This will solve for Q since it is missing and Q will be in m3/s
```

```
# Note: Q (discharge), velocity (V), area (A), wetted perimeter (P), R (hydraulic radius), Re (Reynolds
```

```
Q
```

```
## $Q
```

```
## [1] 0.03536432
```

```
##
```

```
## $V
```

```
## [1] 0.5111079
```

```
##
```

```
## $A
```

```
## [1] 0.06919149
```

```
##
```

```
## $P
```

```
## [1] 0.6645578
```

```
##
```

```
## $R
```

```
## [1] 0.1041166
```

```
##
```

```
## $Re
```

```
## [1] 53006.61
```

```
##
```

```
## $Fr
```

```
## [1] 0.3761052
```

```
# 9) Problem 18 from Hauser (page 89)
```

```
# What is the Q (discharge) for this cross-section?
```

```
Q <- Manningcirc(d = 10 / 12, y = 3 / 12, Sf = 2 / 100, n = 0.025, units = "Eng")
```

```
##
```

```
## Flow IS in the rough turbulent zone so the Gauckler-Manning-Strickler equation  
## is acceptable to use.
```

```
##
```

```
##
```

```
## This is subcritical flow.
```

```
# d = 10/12 ft, y = 3/12 ft, Sf = 2/100 ft/ft, n = 0.025, units = Eng units
```

```
# This will solve for Q since it is missing and Q will be in ft
```

```

# Note: Q (discharge), velocity (V), area (A), wetted perimeter (P), R (hydraulic radius), Re (Reynolds
Q

## $Q
## [1] 0.3155138
##
## $V
## [1] 2.292697
##
## $A
## [1] 0.1376169
##
## $P
## [1] 0.9660662
##
## $R
## [1] 0.1424508
##
## $Re
## [1] 30223.1
##
## $Fr
## [1] 0.9522204

```

parabolic cross-section

```

library("iemisc")

# 10) Modified Exercise 4.3 from Sturm (page 153)

# What is the B1 ("bank-full width") for this cross-section?

B1 <- Manningpara(Q = 32.2, y = 8, y1 = 5.1, Sf = 0.0092, n = 0.025, units = "SI")

##
## Flow IS in the rough turbulent zone so the Gauckler-Manning-Strickler equation
## is acceptable to use.
##
##
## This is subcritical flow.
# Q = 32.2 m3/s, y = 8 m, y1 = 5.1 m, Sf = 0.0092 m/m, n = 0.025, units = SI units
# This will solve for B1 since it is missing and B1 will be in m

# Note: B1 ("bank-full width"), velocity (V), area (A), wetted perimeter (P), R (hydraulic radius), Re

B1

## $B1
## [1] 0.982228

```



```
##
## $V
## [1] 4.907778
##
## $A
## [1] 6.561014
##
## $P
## [1] 16.10527
##
## $R
## [1] 0.407383
##
## $B
## [1] 1.23019
##
## $D
## [1] 5.333333
##
## $Re
## [1] 1991523
##
## $Fr
## [1] 0.6786177
```

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