

# MLML2R package User's Guide

Samara F. Kiihl and Maria Tellez-Plaza

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## Abstract

We present a guide to the *R* package [MLML2R](#). The package provides computational efficient maximum likelihood estimates of DNA methylation and hydroxymethylation proportions when data from the DNA processing methods bisulfite conversion (BS), oxidative bisulfite conversion (ox-BS), and Tet-assisted bisulfite conversion (TAB) are available. Estimates can be obtained when data from all the three methods are available or when any combination of only two of them are available. The package does not depend on other *R* packages, allowing the user to read and preprocess the data with any given software, to import the results into *R* in matrix format, to obtain the maximum likelihood 5-hmC and 5-mC estimates and use them as input for other packages traditionally used in genomic data analysis, such as [minfi](#), [sva](#) and [limma](#).

**Package version:** MLML2R

## Contents

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<b>1</b>	<b>Introduction</b>	<b>1</b>
<b>2</b>	<b>Worked examples</b>	<b>3</b>
2.1	Publicly available data: oxBS and BS methods . . . . .	3
2.2	Publicly available data: TAB and BS methods . . . . .	5
2.3	Simulated data . . . . .	7
	<b>References</b>	<b>12</b>

## 1 Introduction

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In a given CpG site from a single cell we will either have a *C* or a *T* after DNA processing conversion methods, with a different interpretation for each of the available methods. This is a binary outcome and we assume a Binomial model and use the maximum likelihood estimation method to obtain the estimates for hydroxymethylation and methylation proportions.

*T* reads are referred to as converted cytosine and *C* reads are referred to as unconverted cytosine. Conventionally, *T* counts are also referred to as unmethylated counts, and *C* counts as methylated counts. In case of Infinium Methylation arrays, we have intensities representing the methylated (M) and unmethylated (U) channels that are proportional to the number of unconverted and converted cytosines (*C* and *T*, respectively). The most used summary from these experiments is the proportion  $\beta = \frac{M}{M+U}$ , commonly referred to as *beta-value*, which reflects the methylation level at a CpG site. Naïvely using the difference between betas from BS and oxBS as an estimate of 5-hmC (hydroxymethylated cytosine), and the difference between betas from BS and TAB as an estimate of 5-mC (methylated cytosine) can many times provide negative proportions and instances where the sum of 5-C (unmodified cytosine), 5-mC and 5-hmC proportions is greater than one due to measurement errors.

[MLML2R](#) package allows the user to jointly estimate hydroxymethylation and methylation consistently and efficiently.

The function `MLML` takes as input the data from the different methods and returns the estimated proportion of methylation, hydroxymethylation and unmethylation for a given CpG site. Table 1 presents the arguments of the `MLML` and Table 2 lists the results returned by the function.

The function assumes that the order of the rows and columns in the input matrices are consistent. In addition, all the input matrices must have the same dimension. Usually, rows represent CpG loci and columns are the samples.

Table 1: MLML function and random variable notation.

Arguments	Description
<code>G.matrix</code>	Unmethylated channel (Converted cytosines/ T counts) from TAB-conversion (reflecting 5-C + 5-mC).
<code>H.matrix</code>	Methylated channel (Unconverted cytosines/ C counts) from TAB-conversion (reflecting True 5-hmC).
<code>L.matrix</code>	Unmethylated channel (Converted cytosines/ T counts) from oxBS-conversion (reflecting 5-C + 5-hmC).
<code>M.matrix</code>	Methylated channel (Unconverted cytosines/ C counts) from oxBS-conversion (reflecting True 5-mC).
<code>T.matrix</code>	Methylated channel (Unconverted cytosines/ C counts) from standard BS-conversion (reflecting 5-mC+5-hmC).
<code>U.matrix</code>	Unmethylated channel (Converted cytosines/ T counts) from standard BS-conversion (reflecting True 5-C).

Table 2: Results returned from the MLML function

Value	Description
<code>mC</code>	maximum likelihood estimate for the 5-mC proportion
<code>hmC</code>	maximum likelihood estimate for the 5-hmC proportion
<code>C</code>	maximum likelihood estimate for the 5-mC proportion
<code>methods</code>	the conversion methods used to produce the MLE

## 2 Worked examples

### 2.1 Publicly available data: oxBS and BS methods

We will use the dataset from Field (2015), which consists of eight DNA samples from the same DNA source treated with oxBS-BS and hybridized to the Infinium 450K array.

When data is obtained through Infinium Methylation arrays, we recommend the use of the [minfi](#) package (Aryee et al. 2014), a well-established tool for reading, preprocessing and analysing DNA methylation data from these platforms. Although our example relies on [minfi](#) and other *Bioconductor* tools, [MLML2R](#) does not depend on any packages. Thus, the user is free to read and preprocess the data using any software of preference and then import the intensities (or *T* and *C* counts) for the methylated and unmethylated channel (or converted and unconverted cytosines) into *R* in matrix format.

To start this example we will need the following packages:

```
library(MLML2R)
library(minfi)
## Warning: package 'GenomicRanges' was built under R version 3.3.3
## Warning: package 'S4Vectors' was built under R version 3.3.3
## Warning: package 'IRanges' was built under R version 3.3.3
## Warning: package 'XVector' was built under R version 3.3.3
library(GEOquery)
```

It is usually best practice to start the analysis from the raw data, which in the case of the 450K array is a .IDAT file.

The raw files are deposited in GEO and can be downloaded by using the `getGEOSuppFiles`. There are two files for each replicate, since the 450k array is a two-color array. The .IDAT files are downloaded in compressed format and need to be uncompressed before they are read by the `read.metharray.exp` function.

```
getGEOSuppFiles("GSE63179")
untar("GSE63179/GSE63179_RAW.tar", exdir = "GSE63179/idad")

list.files("GSE63179/idad", pattern = "idad")
files <- list.files("GSE63179/idad", pattern = "idad.gz$", full = TRUE)
sapply(files, gunzip, overwrite = TRUE)
```

The .IDAT files can now be read:

```
rgSet <- read.metharray.exp("GSE63179/idad")
```

To access phenotype data we use the `pData` function. The phenotype data is not yet available from the `rgSet`.

```
pData(rgSet)
```

In this example the phenotype is not really relevant, since we have only one sample: male, 25 years old. What we do need is the information about the conversion method used in each replicate: BS or oxBS. We will access this information automatically from GEO:

```
if (!file.exists("GSE63179/GSE63179_series_matrix.txt.gz"))
download.file(
  "https://ftp.ncbi.nlm.nih.gov/geo/series/GSE63nnn/GSE63179/matrix/GSE63179_series_matrix.txt.gz",
  "GSE63179/GSE63179_series_matrix.txt.gz")

geoMat <- getGEO(filename="GSE63179/GSE63179_series_matrix.txt.gz",getGPL=FALSE)
pD.all <- pData(geoMat)

#Another option
#geoMat <- getGEO("GSE63179")
#pD.all <- pData(geoMat[[1]])

pD <- pD.all[, c("title", "geo_accession", "characteristics_ch1.1",
  "characteristics_ch1.2", "characteristics_ch1.3")]
pD
```

This phenotype data needs to be merged into the methylation data. The following commands guarantee we have the same replicate identifier in both datasets before merging.

```
sampleNames(rgSet) <- sapply(sampleNames(rgSet),function(x)
  strsplit(x,"_")[[1]][1])
rownames(pD) <- pD$geo_accession
pD <- pD[sampleNames(rgSet),]
pData(rgSet) <- as(pD,"DataFrame")
rgSet
```

The `rgSet` object is a class called *RGChannelSet* used for two color data (green and a red channel). The input in the MLML function is *MethylSet*, which contains the methylated and unmethylated signals. The most basic way to construct a *MethylSet* is using the function `preprocessRaw`. Here we chose the function `preprocessNoob` (Triche et al. 2013) for background correction and construction of the *MethylSet*.

```
MSet.noob<- preprocessNoob(rgSet)
```

After the preprocessed steps we can use MLML from the [MLML2R](#) package.

The BS replicates are in columns 1, 3, 5, and 6 (information from `pD$title`). The remaining columns are from the oxBS treated replicates.

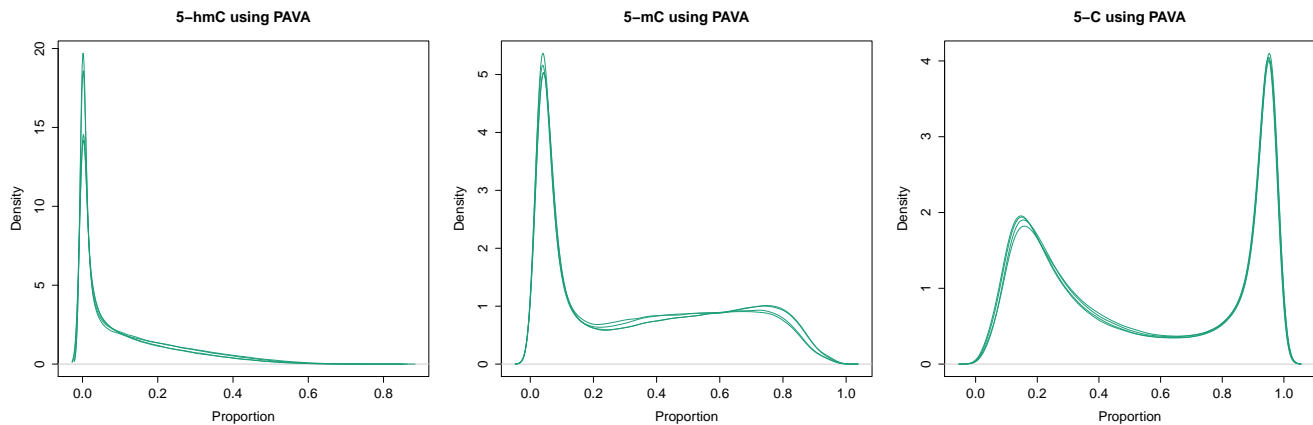


Figure 1: Estimated proportions of hydroxymethylation, methylation and unmethylation for the CpGs in the dataset using the MLML function with default options.

```
MethylatedBS <- getMeth(MSet.noob)[,c(1,3,5,6)]
UnMethylatedBS <- getUnmeth(MSet.noob)[,c(1,3,5,6)]
MethylatedOxBS <- getMeth(MSet.noob)[,c(7,8,2,4)]
UnMethylatedOxBS <- getUnmeth(MSet.noob)[,c(7,8,2,4)]
```

When only two methods are available, the default option of MLML function returns the exact constrained maximum likelihood estimates using the the pool-adjacent-violators algorithm (PAVA) (Ayer et al. 1955).

```
results_exact <- MLML(T.matrix = MethylatedBS , U.matrix = UnMethylatedBS,
                      L.matrix = UnMethylatedOxBS, M.matrix = MethylatedOxBS)
```

Maximum likelihood estimate via EM-algorithm approach (Qu et al. 2013) is obtained with the option `iterative=TRUE`. In this case, the default (or user specified) `tol` is considered in the iterative method.

```
results_em <- MLML(T.matrix = MethylatedBS , U.matrix = UnMethylatedBS,
                  L.matrix = UnMethylatedOxBS, M.matrix = MethylatedOxBS,
                  iterative = TRUE)
```

The estimates are very similar for both methods:

```
all.equal(results_exact$hmC, results_em$hmC, scale=1)
```

## 2.2 Publicly available data: TAB and BS methods

We will use the dataset from Thienpont et al. (2016), which consists of 24 DNA samples treated with TAB-BS and hybridized to the Infinium 450K array from newly diagnosed and untreated non-small-cell lung cancer patients (12 normoxic and 12 hypoxic tumours). The dataset is deposited under GEO accession number [GSE71398](https://www.ncbi.nlm.nih.gov/geo/query/acc.cgi?acc=GSE71398).

Obtaining the data:

```
getGEOSuppFiles("GSE71398")
untar("GSE71398/GSE71398_RAW.tar", exdir = "GSE71398/idad")

list.files("GSE71398/idad", pattern = "idad")
files <- list.files("GSE71398/idad", pattern = "idad.gz$", full = TRUE)
sapply(files, gunzip, overwrite = TRUE)
```

Reading the .IDAT files:

```
rgSet <- read.metharray.exp("GSE71398/idat")
```

The phenotype data is not yet available from the rgSet.

```
pData(rgSet)
```

We need to correctly identify the 24 DNA samples: 12 normoxic and 12 hypoxic non-small-cell lung cancer. We also need the information about the conversion method used in each replicate: BS or TAB. We will access this information automatically from GEO:

```
if (!file.exists("GSE71398/GSE71398_series_matrix.txt.gz"))
  download.file(
    "https://ftp.ncbi.nlm.nih.gov/geo/series/GSE71nnn/GSE71398/matrix/GSE71398_series_matrix.txt.gz",
    "GSE71398/GSE71398_series_matrix.txt.gz")

geoMat <- getGEO(filename="GSE71398/GSE71398_series_matrix.txt.gz",getGPL=FALSE)
pD.all <- pData(geoMat)
pD <- pD.all[, c("title", "geo_accession", "source_name_ch1")]
pD$method <- sapply(pD$source_name_ch1,function(x) strsplit(as.character(x),",")[[1]][3])
pD$group <- sapply(pD$source_name_ch1,function(x) strsplit(as.character(x),",")[[1]][2])
pD$sample <- as.numeric(substr(as.character(pD$title),start=7,stop=8))
```

This phenotype data needs to be merged into the methylation data. The following commands guarantee we have the same replicate identifier in both datasets before merging.

```
sampleNames(rgSet) <- sapply(sampleNames(rgSet),function(x) strsplit(x,"_")[[1]][1])
rownames(pD) <- as.character(pD$geo_accession)
pD <- pD[sampleNames(rgSet),]
pData(rgSet) <- as(pD,"DataFrame")
rgSet
```

The input in the MLML function is *MethylSet*, which contains the methylated and unmethylated signals. We chose the function preprocessNoob (Triche et al. 2013) for background correction and construction of the *MethylSet*.

```
MSet.noob<- preprocessNoob(rgSet)
```

We can now use MLML from the *MLML2R* package.

One needs to carefully check if the columns across the different input matrices represent the same replicate. In this example, all matrices have the samples consistently represented in the columns: sample 1 in the first column, sample 2 in the second, and so forth.

```
BSindex <- which(pD$method == " BS-chip")
TABindex <- which(pD$method == " TAB-chip")
MethylatedBS <- getMeth(MSet.noob)[,BSindex]
UnMethylatedBS <- getUnmeth(MSet.noob)[,BSindex]
MethylatedTAB <- getMeth(MSet.noob)[,TABindex]
UnMethylatedTAB <- getUnmeth(MSet.noob)[,TABindex]
```

When only two methods are available, the default option of MLML function returns the exact constrained maximum likelihood estimates using the the pool-adjacent-violators algorithm (PAVA) (Ayer et al. 1955).

```
results_exact <- MLML(T.matrix = MethylatedBS , U.matrix = UnMethylatedBS,
                     G.matrix = UnMethylatedTAB, H.matrix = MethylatedTAB)
```

Maximum likelihood estimate via EM-algorithm approach (Qu et al. 2013) is obtained with the option `iterative=TRUE`. In this case, the default (or user specified) `tol` is considered in the iterative method.

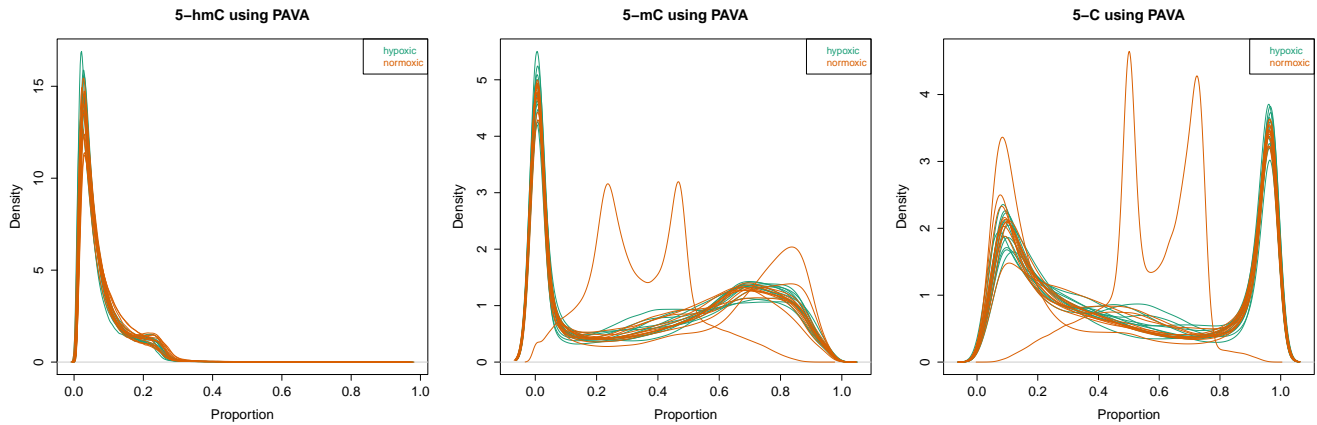


Figure 2: Estimated proportions of hydroxymethylation, methylation and unmethylation for the CpGs in the dataset using the MLML function with default options.

```
results_em <- MLML(T.matrix = MethylatedBS , U.matrix = UnMethylatedBS,
                  G.matrix = UnMethylatedTAB, H.matrix = MethylatedTAB,
                  iterative = TRUE)
```

The estimates for 5-hmC proportions are very similar for both methods:

```
all.equal(results_exact$hmC, results_em$hmC, scale=1)
```

The estimates for 5-mC proportions are very similar for both methods:

```
all.equal(results_exact$mC, results_em$mC, scale=1)
```

## 2.3 Simulated data

To illustrate the package when all the three methods are available or when any combination of only two of them are available, we will simulate a dataset.

We will use a sample of the estimates of 5-mC, 5-hmC and 5-C of the previous oxBS+BS example as the true proportions, as shown in Figure 3.

Two replicate samples with 1000 CpGs will be simulated. For CpG  $i$  in sample  $j$ :

$$T_{i,j} \sim \text{Binomial}(n = c_{i,j}, p = p_m + p_h)$$

$$M_{i,j} \sim \text{Binomial}(n = c_{i,j}, p = p_m)$$

$$H_{i,j} \sim \text{Binomial}(n = c_{i,j}, p = p_h)$$

$$U_{i,j} = c_{i,j} - T_{i,j}$$

$$L_{i,j} = c_{i,j} - M_{i,j}$$

$$G_{i,j} = c_{i,j} - H_{i,j}$$

where the random variables are defined in Table 1, and  $c_{i,j}$  represents the coverage for CpG  $i$  in sample  $j$ .

The following code produce the simulated data:

```

set.seed(112017)

index <- sample(1:dim(results_exact$mC)[1],1000,replace=FALSE) # 1000 CpGs

Coverage <- round(MethylatedBS+UnMethylatedBS)[index,1:2] # considering 2 samples

temp1 <- data.frame(n=as.vector(Coverage),
                    p_m=c(results_exact$mC[index,1],results_exact$mC[index,1]),
                    p_h=c(results_exact$hmC[index,1],results_exact$hmC[index,1]))

MethylatedBS_temp <- c()
for (i in 1:dim(temp1)[1])
{
  MethylatedBS_temp[i] <- rbinom(n=1, size=temp1$n[i], prob=(temp1$p_m[i]+temp1$p_h[i]))
}

UnMethylatedBS_sim2 <- matrix(Coverage - MethylatedBS_temp,ncol=2)
MethylatedBS_sim2 <- matrix(MethylatedBS_temp,ncol=2)

MethylatedOxBS_temp <- c()
for (i in 1:dim(temp1)[1])
{
  MethylatedOxBS_temp[i] <- rbinom(n=1, size=temp1$n[i], prob=temp1$p_m[i])
}

UnMethylatedOxBS_sim2 <- matrix(Coverage - MethylatedOxBS_temp,ncol=2)
MethylatedOxBS_sim2 <- matrix(MethylatedOxBS_temp,ncol=2)

MethylatedTAB_temp <- c()
for (i in 1:dim(temp1)[1])
{
  MethylatedTAB_temp[i] <- rbinom(n=1, size=temp1$n[i], prob=temp1$p_h[i])
}

UnMethylatedTAB_sim2 <- matrix(Coverage - MethylatedTAB_temp,ncol=2)
MethylatedTAB_sim2 <- matrix(MethylatedTAB_temp,ncol=2)

true_parameters_sim2 <- data.frame(p_m=results_exact$mC[index,1],p_h=results_exact$hmC[index,1])
true_parameters_sim2$p_u <- 1-true_parameters_sim2$p_m-true_parameters_sim2$p_h

```

### 2.3.1 BS and oxBS methods

When only two methods are available, the default option returns the exact constrained maximum likelihood estimates using the the pool-adjacent-violators algorithm (PAVA) (Ayer et al. 1955).

```

library(MLML2R)
results_exactB01 <- MLML(T.matrix = MethylatedBS_sim2 , U.matrix = UnMethylatedBS_sim2,
L.matrix = UnMethylatedOxBS_sim2, M.matrix = MethylatedOxBS_sim2)

```



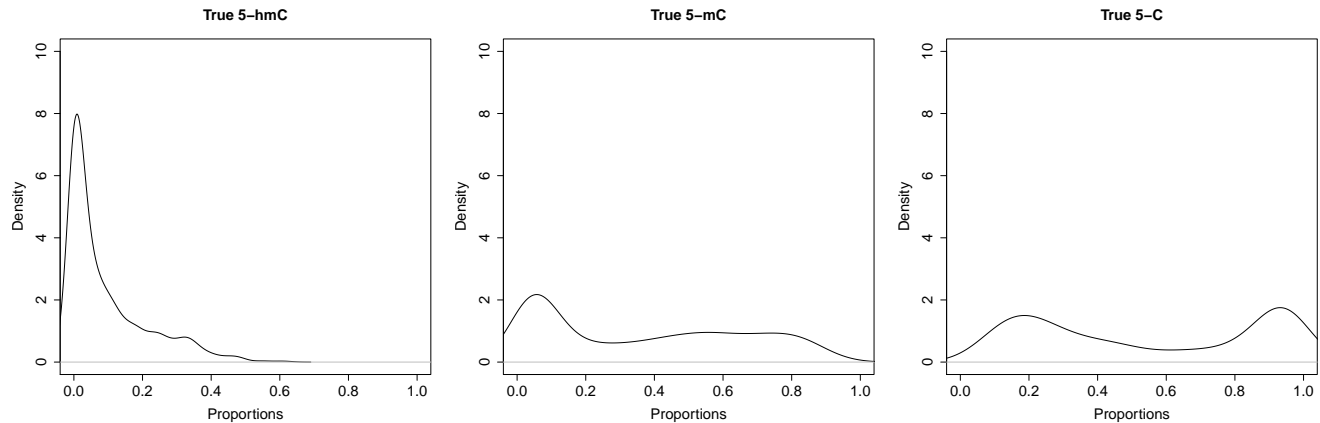


Figure 3: True proportions of hydroxymethylation, methylation and unmethylation for the CpGs used to generate the datasets.

Maximum likelihood estimate via EM-algorithm approach (Qu et al. 2013) is obtained with the option `iterative=TRUE`. In this case, the default (or user specified) `tol` is considered in the iterative method.

```
results_emB01 <- MLML(T.matrix = MethylatedBS_sim2 , U.matrix = UnMethylatedBS_sim2,
  L.matrix = UnMethylatedOxBS_sim2, M.matrix = MethylatedOxBS_sim2, iterative=TRUE)
```

When only two methods are available, we highly recommend the default option `iterative=FALSE` since the difference in the estimates obtained via EM and exact constrained is very small, but the former requires more computational effort:

```
all.equal(results_emB01$hmC, results_exactB01$hmC, scale=1)
## [1] "Mean absolute difference: 9.581949e-05"
```

```
library(microbenchmark)
mbmB01 = microbenchmark(
  EXACT = MLML(T.matrix = MethylatedBS_sim2 , U.matrix = UnMethylatedBS_sim2,
    L.matrix = UnMethylatedOxBS_sim2, M.matrix = MethylatedOxBS_sim2),
  EM = MLML(T.matrix = MethylatedBS_sim2, U.matrix = UnMethylatedBS_sim2,
    L.matrix = UnMethylatedOxBS_sim2, M.matrix = MethylatedOxBS_sim2,
    iterative=TRUE),
  times=10)
mbmB01
## Unit: microseconds
##      expr      min       lq      mean      median       uq      max neval
##  EXACT    557.001   588.011   943.3079   651.1895   1019.18  2866.982    10
##    EM 16573.236 17872.148 18566.2652 18839.3445 19344.45 20122.348    10
##  cld
##    a
##    b
```

Comparison between approximate exact constrained and true hydroxymethylation proportion used in simulation:

```
all.equal(true_parameters_sim2$p_h, results_exactB01$hmC[,1], scale=1)
## [1] "Mean absolute difference: 0.01165593"
```

Comparison between EM-algorithm and true hydroxymethylation proportion used in simulation:

```
all.equal(true_parameters_sim2$p_h, results_emB01$hmC[,1], scale=1)
## [1] "Mean absolute difference: 0.01011952"
```

### 2.3.2 BS and TAB methods

Using PAVA:

```
results_exactBT1 <- MLML(T.matrix = MethylatedBS_sim2 , U.matrix = UnMethylatedBS_sim2,
G.matrix = UnMethylatedTAB_sim2, H.matrix = MethylatedTAB_sim2)
```

Using EM-algorithm:

```
results_emBT1 <- MLML(T.matrix = MethylatedBS_sim2 , U.matrix = UnMethylatedBS_sim2,
G.matrix = UnMethylatedTAB_sim2, H.matrix = MethylatedTAB_sim2,iterative=TRUE)
```

Comparison between PAVA and EM:

```
all.equal(results_emBT1$hmC,results_exactBT1$hmC,scale=1)
## [1] "Mean absolute difference: 7.675267e-07"
```

```
mbmBT1 = microbenchmark(
  EXACT = MLML(T.matrix = MethylatedBS_sim2, U.matrix = UnMethylatedBS_sim2,
    G.matrix = UnMethylatedTAB_sim2, H.matrix = MethylatedTAB_sim2),
  EM = MLML(T.matrix = MethylatedBS_sim2, U.matrix = UnMethylatedBS_sim2,
    G.matrix = UnMethylatedTAB_sim2, H.matrix = MethylatedTAB_sim2,
    iterative=TRUE),
  times=10)
mbmBT1
## Unit: microseconds
##      expr      min       lq      mean   median      uq      max neval
##  EXACT    450.216   459.185   519.5418  492.41    527.612   774.361    10
##    EM  16032.102 17114.401 54801.9136 18420.10 19465.222 384796.990    10
##  cld
##    a
##    a
```

Comparison between approximate exact constrained and true hydroxymethylation proportion used in simulation:

```
all.equal(true_parameters_sim2$p_h,results_exactBT1$hmC[,1],scale=1)
## [1] "Mean absolute difference: 0.00644861"
```

Comparison between EM-algorithm and true hydroxymethylation proportion used in simulation:

```
all.equal(true_parameters_sim2$p_h,results_emBT1$hmC[,1],scale=1)
## [1] "Mean absolute difference: 0.004719911"
```

### 2.3.3 oxBS and TAB methods

Using PAVA:

```
results_exactOT1 <- MLML(L.matrix = UnMethylatedOxBS_sim2, M.matrix = MethylatedOxBS_sim2,
G.matrix = UnMethylatedTAB_sim2, H.matrix = MethylatedTAB_sim2)
```

Using EM-algorithm:

```
results_emOT1 <- MLML(L.matrix = UnMethylatedOxBS_sim2, M.matrix = MethylatedOxBS_sim2,
G.matrix = UnMethylatedTAB_sim2, H.matrix = MethylatedTAB_sim2,iterative=TRUE)
```

Comparison between PAVA and EM:

```
all.equal(results_emOT1$hmC,results_exactOT1$hmC,scale=1)
## [1] "Mean absolute difference: 2.019638e-07"
```

```
mbmOT1 = microbenchmark(
  EXACT = MLML(L.matrix = UnMethylatedOxBS_sim2, M.matrix = MethylatedOxBS_sim2,
    G.matrix = UnMethylatedTAB_sim2, H.matrix = MethylatedTAB_sim2),
  EM = MLML(L.matrix = UnMethylatedOxBS_sim2, M.matrix = MethylatedOxBS_sim2,
    G.matrix = UnMethylatedTAB_sim2, H.matrix = MethylatedTAB_sim2,
    iterative=TRUE),
  times=10)
mbmOT1
## Unit: microseconds
##   expr      min       lq     mean  median      uq      max neval cld
##  EXACT  420.224  460.652 1219.874  718.39 2622.592 2713.364    10   a
##    EM 4946.912 5352.074 6849.189 7181.70 7742.440 8402.259    10   b
```

Comparison between approximate exact constrained and true 5-hmC proportion used in simulation:

```
all.equal(true_parameters_sim2$p_h, results_exactOT1$hmC[,1], scale=1)
## [1] "Mean absolute difference: 0.006451817"
```

Comparison between EM-algorithm and true 5-hmC proportion used in simulation:

```
all.equal(true_parameters_sim2$p_h, results_emOT1$hmC[,1], scale=1)
## [1] "Mean absolute difference: 0.00645154"
```

### 2.3.4 BS, oxBS and TAB methods

When data from the three methods are available, the default option in the MLML function returns the constrained maximum likelihood estimates using an approximated solution for Lagrange multipliers method.

```
results_exactBOT1 <- MLML(T.matrix = MethylatedBS_sim2, U.matrix = UnMethylatedBS_sim2,
  L.matrix = UnMethylatedOxBS_sim2, M.matrix = MethylatedOxBS_sim2,
  G.matrix = UnMethylatedTAB_sim2, H.matrix = MethylatedTAB_sim2)
```

Maximum likelihood estimate via EM-algorithm approach (Qu et al. 2013) is obtained with the option `iterative=TRUE`. In this case, the default (or user specified) `tol` is considered in the iterative method.

```
results_emBOT1 <- MLML(T.matrix = MethylatedBS_sim2, U.matrix = UnMethylatedBS_sim2,
  L.matrix = UnMethylatedOxBS_sim2, M.matrix = MethylatedOxBS_sim2,
  G.matrix = UnMethylatedTAB_sim2, H.matrix = MethylatedTAB_sim2, iterative=TRUE)
```

We recommend the default option `iterative=FALSE` since the difference in the estimates obtained via EM and the approximate exact constrained is very small, but the former requires more computational effort:

```
all.equal(results_emBOT1$hmC, results_exactBOT1$hmC, scale=1)
## [1] "Mean absolute difference: 1.627884e-06"
```

```
mbmBOT1 = microbenchmark(
  EXACT = MLML(T.matrix = MethylatedBS_sim2, U.matrix = UnMethylatedBS_sim2,
    L.matrix = UnMethylatedOxBS_sim2, M.matrix = MethylatedOxBS_sim2,
    G.matrix = UnMethylatedTAB_sim2, H.matrix = MethylatedTAB_sim2),
  EM = MLML(T.matrix = MethylatedBS_sim2, U.matrix = UnMethylatedBS_sim2,
    L.matrix = UnMethylatedOxBS_sim2, M.matrix = MethylatedOxBS_sim2,
    G.matrix = UnMethylatedTAB_sim2, H.matrix = MethylatedTAB_sim2,
    iterative=TRUE),
  times=10)
mbmBOT1
## Unit: milliseconds
```

```
##      expr      min      lq      mean      median      uq      max      neval      cld
## EXACT 1.244414 1.265674 1.329783 1.312158 1.322188 1.504171      10      a
##      EM 2.362101 2.380585 3.602897 4.354667 4.376102 4.565958      10      b
```

Comparison between approximate exact constrained and true hydroxymethylation proportion used in simulation:

```
all.equal(true_parameters_sim2$p_h, results_exactBOT1$hmC[,1], scale=1)
## [1] "Mean absolute difference: 0.005664222"
```

Comparison between EM-algorithm and true hydroxymethylation proportion used in simulation:

```
all.equal(true_parameters_sim2$p_h, results_emBOT1$hmC[,1], scale=1)
## [1] "Mean absolute difference: 0.004146021"
```

## References

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