# Package 'CollocInfer'

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| <b>Description</b> These functions implement collocation-inference for continuous-time and discrete-time stochastic processes.  They provide model-based smoothing, gradient-matching, generalized profiling and forwards prediction error methods. |
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# Description

Functions carry out collocation inference method for nonlinear continuous-time dynamic systems. These are based on basis-expansion representations for the state of the system. Gradient-matching, profiling and EM algorithms are supported.

# **Details**

Package: CollocInfer
Type: Package
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Date: 2009-08-19
License: GPL-2
LazyLoad: yes

# Author(s)

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## References

Ramsay, James O., Giles Hooker, Jiguo Cao and David Campbell (2007), "Parameter Estimation in Ordinary Differential Equations: A Generalized Smoothing Approach", *Journal of the Royal Statistical Society*, 69

Ramsay, James O., and Silverman, Bernard W. (2006), *Functional Data Analysis*, 2nd ed., Springer, New York.

ChemoData

Chemostat Example Data

# Description

Five-species Chemostat Model

#### Usage

ChemoData

## **Format**

- ChemoData A 61 by 2 matrix of data observed in a chemostat.
- ChemoTime A vector of 61 observation times corresponding to ChemoData.
- ChemoPars Named parameter vector as a starting point for estimation ChemoData.
- ChemoVarnames c('N','C1','C2','B','S'): the state variable names for the chemostat system.
- ChemoParnames parameter names for the chemostat system.

## **Source**

Yoshida, T., L. E. Jones, S. P. Ellner, G. F. Fussmann and N. G. Hairston, 2003, "Rapid evolution drives ecological dynamics in a predator-prey system", Nature, 424, pp. 303-306.

ChemoRMData

Rosenzweig-MacArthur Model Applied to Chemostat Data

# **Description**

Two-Species Rosenzweig-MacArthur Model

# Usage

ChemoRMData

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## **Format**

- ChemoRMData A 108 by 2 matrix of data observed in a chemostat.
- ChemoRMPars Named parameter vector as a starting point for estimation in ChemoRMData.
- ChemoRMTime A vector of 108 observation times corresponding to ChemoData.
- RMparnames parameter names for the Rosenzweig-MacArthur system.
- RMvarnames the state variable names for the Rosenzweig-MacArthur system.

#### **Source**

Becks, L., S. P. Ellner, L. E. Jones, and N. G. Hairston, 2010, "Reduction of adaptive genetic diversity radically alters eco-evolutionary community dynamics", Ecology Letters, 13, pp. 989-997.

# **Description**

Diagnostic Plots on the Results of CollocInfer

## Usage

# **Arguments**

| coefs      | Vector giving the current estimate of the coefficients.  |
|------------|--|
| pars       | Vector of estimated parameters.  |
| lik        | lik object defining the observation process.   |
| proc       | proc object defining the state process.  |
| times      | Vector observation times for the data.   |
| data       | Matrix of observed data values.  |
| cols       | Optional vector specifying a color for each state variable.  |
| datacols   | Optional vector specifying a color for each observation dimension.   |
| datanames  | Optional character vector specifying a glyph to plot the data. Taken from the column-names of data if not given. |
| ObsPlot    | Should a plot of predictions and observations be given?  |
| DerivPlot  | Should derivative diagnostics be produced?   |
| DerivResid | Should a plot of the difference between $Dx$ and $f(x)$ be produced?   |

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| newplot  | Should plots be opened in new devices? Note if this is FALSE, DerivePlot will overwrite ObsPlot. |
|----------|--|
| cex.axis | Axis font size.  |
| cex.lab  | Label font size.   |
| cex      | Plotting point font size   |
| lwd      | Plotting line width  |

#### **Details**

Timevec is taken to be the quadrature values. Three plots can be produced:

If ObsPlot=TRUE a plot is given of the predicted values of the observations along with the observations themselves (if given).

If DerivPlot=TRUE two plots are produced. The first gives the value of the derivative of the estimated trajectory (dashed) and the value of the right-hand-side of the ordinary differential equation in proc (hence the predicted derivative) (solid). The second plot gives their difference in the first panel as well as the estimated trajectory in the second panel.

#### Value

A list containing elements used in plotting:

| timevec | Times at which the trajectories etc were evaluated.         |
|---------|---|
| traj    | Estimated value of the trajectory.                          |
| dtraj   | Derivative of the estimated trajectory.                     |
| ftraj   | Value of the derivative of the trajectory predicted by proc |
| otraj   | Predicted values of the observations from lik.              |
|         |   |

| FhNdata | FitzHugh-Nagumo data |  |
|---------|----------------------|--|
|         |                      |  |

## **Description**

Data generated for FitzHugh-Nagumo Examples

# Usage

FhNdata

#### **Format**

- FhNdata A 41 by 2 matrix of data generated from the FitzHugh Nagumo equations.
- FhNtimes A vector of 41 observation times corresponding to FhNdata.
- FhNpars Named parameter vector used to generate FhNdata.
- FhNvarnames c('V', 'R'): the state variable names for the FitzHugh Nagumo system.
- FhNparnames c('a', 'b', 'c') parameter names for the FitzHugh Nagumo system.

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## **Source**

James Ramsay, Giles Hooker David Campbell and Jiguo Cao, 2007. "Parameter Estimation for Differential Equations: A Generalized Smoothing Approach". Journal of the Royal Statistical Society Vol 69 No 5.

FhNest

Estimated Parameters for FitzHugh-Nagumo data

# **Description**

Parameters Estimated for FhN Data – used to speed up examples

# Usage

FhNest

#### **Format**

- FhNestPars Estimated parameters for the FhN Data example.
- FhNestCoefs Estimated coefficients for the FhN Data example.

#### **Source**

James Ramsay, Giles Hooker David Campbell and Jiguo Cao, 2007. "Parameter Estimation for Differential Equations: A Generalized Smoothing Approach". Journal of the Royal Statistical Society Vol 69 No 5.

FitMatch

Estimating Hidden States

## Description

Estimating hidden states to maximize agreement with the process.

## Usage

```
FitMatchOpt(coefs,which,pars,proc,meth='nlminb',control=list())
FitMatchErr(coefs,allcoefs,which,pars,proc,sgn=1)
FitMatchDC(coefs,allcoefs,which,pars,proc,sgn=1)
FitMatchDC2(coefs,allcoefs,which,pars,proc,sgn=1)
FitMatchList(coefs,allcoefs,which,pars,proc,sgn=1)
```

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## **Arguments**

| coefs    | Vector giving the current estimate of the coefficients for the hidden states.        |
|----------|--|
| allcoefs | Matrix giving the coefficients of all the states including initial values for coefs. |
| which    | Vector of indices of states to be estimated.   |
| pars     | Parameters to be used for the processes.   |
| proc     | proc object defining the state process.  |
| sgn      | Is the minimizing (1) or maximizing (0)?   |
| meth     | Optimization function currently one of 'nlminb', 'MaxNR', 'optim' or 'trust'.        |
| control  | Control object for optimization function.  |

## **Details**

These routines allow the values of coefficients for some states to be optimized relative to the others. That is, the objective defined by proc is minimized over those states specified in which leaving the others constant. This would be typically done, for example, a smooth is taken to estimate some states non-parametrically, but data is not available on all of them.

A number of optimization routines have been implemented in FitMatchOpt, some experimentation is advised.

#### Value

| FitMatchOpt  | A list containing  |
|--------------|--|
|              | <ul> <li>coefs The optimized coefficients for all states.</li> </ul>   |
|              | • res The output of the optimization routine.  |
| FitMatchErr  | The value of the process likelihood at the current estimated states.   |
| FitMatchDC   | The derivative of FitMatchErr with respect to the elements coefs for the states being estimated.                         |
| FitMatchDC2  | The second derivative of FitMatchErr with respect to the elements coefs for the states being estimated.                  |
| FitMatchList | Returns a list with elements value, gradient and hessian given by the output of FitMatchErr, FitMatchDC and FitMatchDC2. |

# See Also

```
ParsMatchErr, SplineCoefsErr, inneropt
```

# **Examples**

```
##################################
 #### Basis Object ######
 knots = seq(0,20,0.2)
 norder = 3
 nbasis = length(knots) + norder - 2
 range = c(0,20)
 bbasis = create.bspline.basis(range=range(FhNtimes),nbasis=nbasis,
 norder=norder,breaks=knots)
 # Initial values for coefficients will be obtained by smoothing
 fd.data = FhNdata[,1]
 DEfd = smooth.basis(FhNtimes,fd.data,fdPar(bbasis,1,0.5))
 coefs = cbind(DEfd$fd$coefs,rep(0,nbasis))
 colnames(coefs) = FhNvarnames
 ### If We Only Observe One State, We Can Re-Smooth Others ###
 profile.obj = LS.setup(pars=FhNpars,coefs=coefs,fn=make.fhn(),
                   basisvals=bbasis,lambda=1000,times=FhNtimes)
 lik = profile.obj$lik
 proc= profile.obj$proc
 # DD = Matrix(diag(1,200),sparse=TRUE)
 # tDD = t(DD)
 fres = FitMatchOpt(coefs=coefs,which=2,pars=FhNpars,proc)
 plot(fd(fres$coefs,bbasis))
forward.prediction.error
```

## **Description**

Forward prediction error objective for choice of lambda in square error criteria.

forward.prediction.error

# Usage

```
forward.prediction.error(times,data,coefs,lik,proc,pars,whichtimes=NULL)
```

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## **Arguments**

| times      | Vector observation times for the data.                                |
|------------|---|
| data       | Matrix of observed data values.                                       |
| coefs      | Vector giving the current estimate of the coefficients in the spline. |
| lik        | lik object defining the observation process.                          |
| proc       | proc object defining the state process.                               |
| pars       | Initial values of parameters to be estimated processes.               |
| whichtimes | Specifies the start and end times for forward prediction, given by    |

times. This can be one of

• A list, each element of the list is itself a list of length 2; the first element gives the starting time to use and the second is a vector giving the prediction

indeces of

• A matrix, the first column giving the starting times and the second giving the ending times.

If left NULL, whichtimes defaults to predicting one observation ahead from each observation.

## **Details**

Forward prediction error can be used to choose values of lambda in the profiled estimation routines. The ordinary differential equation is solved starting from the starting times specified in whichtimes and measured at the corresponding measurement times. The error is then recorded. This should then be minimized by a grid search.

#### Value

The forwards prediction error from the estimates.

## See Also

ProfileSSE, outeropt

| inneropt | Inner Optimization Functions |
|----------|------------------------------|
|          |                              |

# **Description**

Estmates coefficients given parameters.

# Usage

```
inneropt(data,times,pars,coefs,lik,proc,in.meth='nlminb',control.in=list())
```

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# **Arguments**

| data       | Matrix of observed data values.   |
|------------|---|
| times      | Vector observation times for the data.  |
| pars       | Initial values of parameters to be estimated processes.   |
| coefs      | Vector giving the current estimate of the coefficients in the spline.   |
| lik        | lik object defining the observation process.  |
| proc       | proc object defining the state process.   |
| in.meth    | Inner optimization function currently one of 'nlminb', 'maxNR', 'optim', 'trust' or 'SplineEst'. The last calls $SplineEst.NewtRaph$ . This is fast but has poor convergence. |
| control.in | Control object for inner optimization function.   |

# **Details**

This minimizes the objective function defined by the addition of the lik and proc objectives with respect to the coefficients. A number of generic optimization routines can be used and some experimentation is recommended.

#### Value

A list with elements

coefs A matrix giving he optimized coefficients.

res The results of the inner optimization function.

# See Also

```
outeropt, Smooth.LS,LS.setup, multinorm.setup, SplineCoefsErr
```

# **Examples**

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IntegrateForward

**IntegrateForward** 

# Description

Solves a differential equation going forward based on a proc object.

# Usage

IntegrateForward(y0,ts,pars,proc,more)

## **Arguments**

| y0   | Initial conditions to start from.   |
|------|---|
| ts   | Vector of time points at which to report values of the differential equation solution.  |
| pars | Initial values of parameters to be estimated processes.   |
| proc | Object defining the state process. This can either be a function evaluating the right hand side of the differential equation or a proc object. If a proc object is given, proc\$more\$fn is assumed to give the right hand side of the differential equation. |
| more | If proc is a function, this contains a list of additional inputs.   |
|      |   |

#### Value

Returns the output from solving the differential equation using the 1soda routines. Specifically, it returns a list with elements

- times The output times.
- states The output states.

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## See Also

```
Profile.LS, Profile.multinorm
```

# **Examples**

```
proc = make.SSEproc()
proc$more = make.fhn()
proc$more$names = c('V','R')

y0 = c(-1,1)
names(y0) = c('V','R')

pars = c(0.2,0.2,3)
names(pars) = c('a','b','c')

ts = seq(0,20,0.5)

value = IntegrateForward(y0,ts,pars,proc)

matplot(value$times,value$states)
```

make.findif

Finite Difference Functions

# **Description**

Returns a list of functions that calculate finite difference derivatives.

# Usage

```
make.findif.ode()
make.findif.loglik()
make.findif.var()
```

#### **Details**

All these functions require the sepcification of more\$eps to give the size of the finite differencing step. They also require more to specify the original object (ODE right hand side functions, definitions of lik and proc objects).

# Value

A list of functions that calculate the derivatives via finite differencing schemes.

```
make.findif.ode
```

calculates finite differences of a transform.

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```
make.findif.loglik
```

returns the finite differences to a calculated log likelihood; used within lik objects, or as more arguments to Cproc or Dproc.

make.findif.var

finite difference approximations to variances; mostly used in the Multinorm functions.

## See Also

```
LS.setup, multinorm.setup
```

# **Examples**

```
# Sum of squared errors with finite differencing to get right-hand-side derivatives
proc = make.SSEproc()
proc$more = make.findif.ode()

# Finite differencing for the log likelihood
lik = make.findif.loglik()
lik$more = make.SSElik()

# Multivariate normal transitions with finite differencing for mean and variance functions
lik = make.multinorm()
lik$more = c(make.findif.ode,make.findif.var)

# Finite differencing for transition density of a discrete time system
proc = make.Dproc()
proc$more = make.findif.loglik()
```

make.lik

Observation Process Distribution Function

# Description

Returns a list of functions that calculate the observation process distribution and its derivatives; designed to be used with the collocation inference functions.

## Usage

```
make.SSElik()
make.multinorm()
```

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#### **Details**

These functions require more to be a list with elements:

- fn The transform function of the states to observations, or to their derivatives.
- dfdx The derivative of fn with respect to states.
- dfdp The derivative of fn with respect to parameters.
- d2fdx2 The second derivative of fn with respect to states.
- d2fdxdp The cross derivative of fn with respect to states and parameters.

make.Multinorm further requires:

- var. fn The variance given in terms of states and parameters.
- var.dfdx The derivative of var.fn with respect to states.
- var.dfdp The derivative of var.fn with respect to parameters.
- var.d2fdx2 The second derivative of var.fn with respect to states.
- var.d2fdxdp The cross derivative of var.fn with respect to states and parameters.

make. SSElik further requres weights giving weights to each observation.

#### Value

A list of functions that calculate the log observation distribution and its derivatives.

```
make. SSElik calculates weighted squared error between predictions (given by fn in more) and observations
```

make.Multinorm calculates a multivariate normal distribution.

#### See Also

```
LS. setup, multinorm. setup
```

# Examples

```
# Straightforward sum of squares:
lik = make.SSElik()
lik$more = make.id()

# Multivariate normal about an exponentiated state with constant variance
lik = make.multinorm()
lik$more = c(make.exp(), make.cvar())
```

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| make.logtrans | Log Transforms |  |
|---------------|----------------|--|
|---------------|----------------|--|

# **Description**

Functions to modify liklihood, transform, 1ik and proc objects so that the operate with the state defined on a log scale.

# Usage

```
make.logtrans()
make.exptrans()
make.logstate.lik()
make.exp.Cproc()
make.exp.Dproc()
```

## **Details**

All functions require more to specify the original object (ODE right hand side functions, definitions of lik and proc objects).

# Value

A list of functions that calculate log transforms and derivatives in various contexts.

```
make.logtrans modifies the right hand side of a differential equation and its derivatives for a loged state vector.

make.exptrans modifies a map from states to observations to a map from logged states to observations along with its derivatives.

make.logstate.lik modifies a lik object for state vectors given on the log scale.

make.exp.Cproc Cproc with the state given on the log scale.

make.exp.Dproc Dproc with the state given on the log scale.
```

## See Also

```
LS.setup, make.Cproc, make.Dproc
```

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## **Examples**

```
# Model the log of an SEIR process
proc = make.SSEproc()
proc$more = make.logtrans()
proc$more$more = make.SEIR()

# Observe a linear combination of
lik = make.logstate.lik()
lik$more = make.SSElik()
lik$more$more = make.genlin()

# SEIR Model with multivariate transition densities
proc = make.exp.Cproc()
proc$more = make.multinorm()
proc$more$more = c(make.SEIR(),make.cvar())
```

make.proc

Process Distributions

# **Description**

Functions to define process distributions in the collocation inference package.

## Usage

```
make.Dproc()
make.Cproc()
make.SSEproc()
```

## **Details**

All functions require more to specify this distribution. This should be a list containing

- fn The distribution specified.
- dfdx The derivative of fn with respect to states.
- dfdp The derivative of fn with respect to parameters.
- d2fdx2 The second derivative of fn with respect to states.
- d2fdxdp The cross derivative of fn with respect to states and parameters.

For Cproc and Dproc this should specify the distribution; for SSEproc it should specify the right hand side of a differential equation.

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# Value

A list of functions that the process distribution

make. Cproc creates functions to evaluate the distribution of the derivative of the state vector

given the current state for continuous-time systems.

make.Dproc creates functions to evaluate the distribution of the next time point of the state

vector given the current state for discrete-state systems.

make. SSEproc treats the distribution of the derivative as an independent gaussian and cacluates

weighted sums of squared errors between derivatives and the prediction from

the current state.

## See Also

```
LS.setup, multinorm.setup
```

# **Examples**

```
# FitzHugh-Nagumo Equations

proc = make.SSEproc()
proc$more = make.fhn()

# Henon Map

proc = make.Dproc()
proc$more = make.Henon

# SEIR with multivariate normal transitions

proc = make.Cproc()
proc$more = make.multinorm()
proc$more$more = c(make.SEIR(),make.var.SEIR())
```

make.transfer

Transfer Functions

# **Description**

Returns a list of functions that calculate the transform and its derivatives.

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## Usage

```
make.id()
make.exp()
make.exptrans()
make.genlin()
make.fhn()
make.Henon()
make.SEIR()
make.NS()
chemo.fun(times,y,p,more=NULL)
```

## **Arguments**

All the functions created by make... functions, require the arguments needed

by chemo.fun

Evaluation times

yimes Values of the state at the evaluation times

p Parameters to be used

more A list of additional arguments, in this case NULL, for pomp. sekelton and pomp. dmeasure,

more should be a list containing a pomp object in the element pomp.obj.

## **Details**

make.genlin requires the specification of further elements in the list. In particular the element more should be a list containing

- mat a matrix defining the linear transform before any parameters are added. This may be all zero, but it may also specify fixed elements, if desired.
- sub a k-by-3 matrix indicating which parameters should be entered into which elements of mat. Each row is a triple giving the row and colum of mat to be specified and the element of the parameter vector that should be substituted. sub over-rides any values in mat.
- force if input functions are given, these are given as a list.
- force.mat specifying the influence of the elements of force on the state variables. Defined as in mat.
- force.sub defined as in sub, over-rides the elements of force.mat with parameter values.

make.diagnostics estimates forcing-function diagnostics as in Hooker, 2009 for goodness-of-fit assessment. It requires

make.transfer 19

- psi Values of a basis expansion for forcing functions at the quadrature points.
- which Which states are to be forced?
- fn, dfdx, d2fdx2 Functions and derivatives as would be used to estimate parameters for the original equations.
- pars Parameters to go into more\$fn.

make. SEIR estimates parameters and a seasonal variation in the infection rate in an SEIR model. It requires the specification of the seasonal change rate in more by a list with objects

- beta. fun A function to calculate beta, it should have arguments t, p and betadef and return a matrix giving the value of beta at times t with parameters p.
- beta.dfdp Should calculate the derivative of beta.fun with respect to p, at times t returning a matrix. The matrix should be of size length(t) by length(p) where p is the entire parameter vector.
- betadef Additional inputs (eg bases) to beta. fun and beta. dfdp.

make.NS provides functions for the North Shore example. This is a possibly time-varying forced linear system of one dimension. It requires more to specify betabasis to describe the autoregressive coefficient, and alphabasis to provide a contant in front of the functional data object rainfd.

chemo.fun Is a five-state predator-prey-resources model used as an example. It stands alone as a function and should be used with the findif.ode functions.

#### Value

A list of functions that calculate the transform and its derivatives, in a form compatible with the collocation inference functions.

```
make.id returns the identity transform.

make.exp returns the exponential transform.

make.genlin returns a linear combination transform – see details section below.

make.fhn returns the FitzHugh-Nagumo equations.

make.Henon reutrns the Henon map.

make.SEIR returns SEIR equations for estimating the shape of a seasonal forcing component.

make.diagnostics
```

functions to perform forcing function diagnostics.

#### See Also

```
LS.setup, multinorm.setup
```

# Examples

```
# Observe the FitzHugh-Nagumo equations
proc = make.SSEproc()
proc$more = make.fhn()
```

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```
lik = make.SSElik()
lik$more = make.id()
# Observe an unknown scalar transform of each component of a Henon map, given
# in the first two elements of the parameter vector:
proc = make.Dproc()
proc$more = make.multinorm()
proc$more$more = c(make.Henon,make.cvar)
lik = make.multinorm()
lik$more = c(make.genlin,make.cvar)
likmoremore = list(mat = matrix(0,2,2),sub=matrix(c(1,1,1,2,2,2),2,3,byrow=TRUE))
# Model SEIR equations on the log scale and then exponentiate
lik = make.SSElik()
lik$more = make.exp()
proc = make.SSEproc()
proc$more = make.logtrans()
proc$more$more = make.SEIR()
```

make.variance

Variance Functions

## **Description**

Returns a list of functions that calculate a (possibly state and parameter dependent) variance.

# Usage

```
make.cvar()
make.var.SEIR()
```

#### **Details**

make.cvar requires the specification of further elements in the list. In particular the element more should be a list containing

# Value

A list of functions that calculate a variance function and its derivatives, in a form compatible with the collocation inference functions.

make.cvar returns a variance that is constant but may depend on parameters

make.var.SEIR returns a state-dependent transition covariance matrix calculated for the SEIR

equations.

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# See Also

```
make.multinorm
```

# **Examples**

```
# Multivariate normal observation of the state vector.
lik = make.multinorm()
lik$more = c(make.id(),make.cvar())
```

NSdata

North Shore data

# **Description**

Groundwater Data from Vancouver's North Shore

# Usage

NSgroundwater

#### **Format**

- NSgroundwater A 315 by 1 matrix of data on groundwater level collected in vancouver.
- NStimes A vector of 315 observation times corresponding to NSgroundwater.
- NSrainfall Rainfall as a covariate to NSgroundwater; this quantity is lagged by 3 days.

outeropt

Outer Optimization Functions

# **Description**

Outer optimization; performs profiled estimation.

# Usage

```
outeropt(data,times,pars,coefs,lik,proc,
    in.meth='nlminb',out.meth='nlminb',
    control.in=list(),control.out=list(),active=1:length(pars))
```

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#### **Arguments**

data Matrix of observed data values.

times Vector observation times for the data.

pars Initial values of parameters to be estimated processes.

coefs Vector giving the current estimate of the coefficients in the spline.

lik lik object defining the observation process.

proc object defining the state process.

in.meth Inner optimization function currently one of 'nlminb', 'maxNR', 'optim' or

'SplineEst'. The last calls SplineEst.NewtRaph. This is fast but has poor

convergence.

out . meth Outer optimization function to be used, one of 'optim' (defaults to BFGS routine

in optim unless control.out\$meth specifies otherwise), 'nlminb', 'maxNR' #, 'trust' or 'subplex'. When squared error is being used, 'ProfileGN' and 'nls' can also be given. The former of these calls Profile.GausNewt, a fast but

naive Gauss-Newton solver.

control.in Control object for inner optimization function.
control.out Control object for outer optimization function.

active Indices indicating which parameters of pars should be estimated; defaults to all

of them.

#### **Details**

The outer optimization for parameters looks only at the objective defined by the lik object. For every parameter value, coefs are optimized by inneropt and then the value of lik for these coefficients is computed.

A number of optimization routines can be used here, some experimentation is recommended. Libraries for these optimization routines are not pre-loaded. Where these functions take options as explicit arguments instead of a list, they should be listed in control.out and will be called by their names.

The routine creates temporary files 'curcoefs.tmp' and 'optcoefs.tmp' to update coefficients as pars evolves. These overwrite existing files of those names and are deleted before the function terminates.

## Value

## A list containing

pars Optimized parameters

coefs Optimized coefficients at pars
res The result of the outer optimization.

counter A set of parameters and objective values for each successful iteration.

#### See Also

inneropt, Profile.LS, ProfileSSE, ProfileErr, LS.setup, multinorm.setup

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## **Examples**

```
## Not run:
data(FhNdata)
knots = seq(0,20,0.2)
                              # Create a basis
norder = 3
nbasis = length(knots) + norder - 2
range = c(0,20)
bbasis = create.bspline.basis(range=range,nbasis=nbasis,norder=norder,breaks=knots)
lambda = 10000
                             # Penalty value
DEfd = smooth.basis(FhNtimes,FhNdata,fdPar(bbasis,1,0.5)) # Smooth to estimate
                                                            # coefficients first
coefs = DEfd$fd$coefs
colnames(coefs) = FhNvarnames
profile.obj = LS.setup(pars=FhNpars,coefs=coefs,fn=make.fhn(),basisvals=bbasis,
      lambda=lambda,times=FhNtimes)
lik = profile.obj$lik
proc= profile.obj$proc
res = outeropt(data=FhNdata,times=FhNtimes,pars=FhNpars,coefs=coefs,lik=lik,proc=proc,
    in.meth="nlminb",out.meth="nlminb",control.in=NULL,control.out=NULL)
plot(res$coefs,main='outeropt')
print(blah)
## End(Not run)
```

ParsMatch

Estimate of Parameters from Smooth

## **Description**

Objective function and derivatives to estimate parameters with a fixed smooth.

# Usage

```
ParsMatchOpt(pars,coefs,proc,active=1:length(pars),meth='nlminb',control=list())
ParsMatchErr(pars,coefs,proc,active=1:length(pars),allpars,sgn=1)
ParsMatchDP(pars,coefs,proc,active=1:length(pars),allpars,sgn=1)
ParsMatchList(pars,coefs,proc,active=1:length(pars),allpars,sgn=1)
```

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# **Arguments**

| pars    | Initial values of parameters to be estimated processes.                                     |
|---------|---|
| coefs   | Vector giving the current estimate of the coefficients in the spline.                       |
| proc    | proc object defining the state process.   |
| active  | Incides indicating which parameters of allpar should be estimated; defaults to all of them. |
| allpars | Vector of all parameters, the assignment allpar[active]=pars is made initially.             |
| sgn     | Is the minimizing (1) or maximizing (0)?  |
| meth    | Optimization function currently one of 'nlminb', 'MaxNR', 'optim' or 'trust'.               |
| control | Control object for optimization function.   |

## **Details**

These routines fix the estimated states at the value given by coefs and estimate pars to maximize agreement between the fixed state and the objective given by the proc object.

A number of optimization routines have been implemented in FitMatchOpt, some experimentation is advised.

#### Value

| ParsMatchOpt  | A list containing:   |
|---------------|--|
|               | • parsThe entire parameter vector after optimization.  |
|               | • resThe output of the optimization routine.   |
| ParsMatchErr  | The value of the process likelihood at the current estimated states.                                     |
| ParsMatchDP   | The derivative fo ParsMatchErr with respect to pars[active].   |
| ParsMatchList | A list with entries value and gradient given by the output of ParsMatchErr and ParsMatchDP respectively. |

# See Also

```
FitMatchErr, SplineCoefsErr, inneropt
```

# **Examples**

Profile.covariance 25

```
bbasis = create.bspline.basis(range=range(FhNtimes),nbasis=nbasis,
norder=norder,breaks=knots)
# Initial values for coefficients will be obtained by smoothing
DEfd = smooth.basis(FhNtimes,FhNdata,fdPar(bbasis,1,0.5)) # Smooth to estimate
                                                      # coefficients first
coefs = DEfd$fd$coefs
colnames(coefs) = FhNvarnames
### Initial Parameter Guesses ###
profile.obj = LS.setup(pars=FhNpars,coefs=coefs,fn=make.fhn(),basisvals=bbasis,
   lambda=1000, times=FhNtimes)
lik = profile.obj$lik
proc= profile.obj$proc
pres = ParsMatchOpt(FhNpars,coefs,proc)
npars = pres$pars
```

Profile.covariance

Profile.covariance

# Description

Newey-West estimate of covariance of parameter estimates from profiling.

# Usage

# Arguments

| pars   | Initial values of parameters to be estimated processes.                                   |
|--------|---|
| active | Incides indicating which parameters of pars should be estimated; defaults to all of them. |
| times  | Vector observation times for the data.  |
| data   | Matrix of observed data values.   |
| coefs  | Vector giving the current estimate of the coefficients in the spline.                     |
| lik    | lik object defining the observation process.  |

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| proc    | proc object defining the state process.                                    |
|---------|--|
| in.meth | Inner optimization function currently one of 'nlminb', 'MaxNR', 'optim' or |

'house'. The last calls SplineEst.NewtRaph. This is fast but has poor con-

vergence.

control.in Control object for inner optimization functions.

eps Step-size for finite difference estimate of second derivatives.

GN Indicator of whether a Gauss-Newton approximation for the Hessian should be

employed. Only valid for least-squares methods.

## **Details**

Currently assumes a lag-5 auto-correlation among observation vectors.

## Value

Returns a Newey-West estimate of the covariance matrix of the parameter estimates.

#### See Also

```
ProfileErr, ProfileSSE, Profile.LS, Profile.multinorm
```

## **Examples**

```
# See example in Profile.LS
```

ProfileObjective

Profile Estimation with Collocation Inference

## Description

Profile estimation and objective functions for collocation estimation of parameters in continuoustime stochastic processes.

## **Usage**

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# Arguments

| pars       | Initial values of parameters to be estimated processes.   |
|------------|---|
| allpars    | Full parameter vector including pars. Assignment allpars[active] = pars is always made.   |
| times      | Vector observation times for the data.  |
| data       | Matrix of observed data values.   |
| coefs      | Vector giving the current estimate of the coefficients in the spline.   |
| lik        | lik object defining the observation process.  |
| proc       | proc object defining the state process.   |
| in.meth    | Inner optimization function currently one of 'nlminb', 'MaxNR', 'optim' or 'house'. The last calls SplineEst.NewtRaph. This is fast but has poor convergence. |
| control.in | Control object for inner optimization function.   |
| sgn        | Is the minimizing (1) or maximizing (0)?  |
| active     | Incides indicating which parameters of pars should be estimated; defaults to all of them.   |
| oldpars    | Starting parameter values for the Q-function in the EM algorithm.   |
| dcdp       | Estimate for the gradient of the optimized coefficients with respect to parameters; used internally.  |
| use.nls    | In ProfileSSE, is 'nls' being used in the outer-optimization?   |
| sumlik     | In ProfileDP and ProfileDP.AllPar; should the gradient be given for each observation, or summed over them?  |
| control    | A list giving control parameters for Newton-Raphson optimization. It should contain   |

- reltol Relative tollerance criterion for the gradient and improvement before termination.
- maxit Maximum number of iterations.
- maxtry Maximum number of halving-steps to try before declaring no improvement is possible.
- trace How much iteration history to output; 0 surpresses all output, a positive value outputs parameters and improvement at each iteration.

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#### **Details**

Profile. Gaus Newt provides a simple implementation of Gauss-Newton optimization and may not result in optimized values that are as good as other optimizers in R.

When Profile.GausNewt is not being used, ProfileSEE and ProfileERR create the following temporary files:

- counter.tmpThe number of halving-steps taken on the current optimization step.
- curcoefs.tmpThe current estimates of the coefficients.
- optcoefs.tmpThe optimal estimates of the coefficients in the iteration history.

These need to be removed manually when the optimization is finished. optcoefs. tmp will contain the optimal value of coefs for plotting the estimated trajectories.

#### Value

Profile.GausNewt

Output of a simple Gaus-Newton iteration to optimizing the objective function when the observation likelihood takes the form of a sum of squared errors. Returns a list with the following elements:

- pars The optimized value of the parameters.
- in.res The result of the inner optimization.
- value The value of the optimized sum of squared errors.

ProfileSSE

Output for the outer optimization when the observation likelihood is given by squared error. This is a list with the following elements

- value The value of the outer optimization criterion.
- gradient The derivative of f with respect to pars.
- coefs The optimized value of coefs for the current value of pars.
- dcdp The derivative of the optimized value of coefs at the current value of pars.

ProfileErr

The outer optimization criterion in the general case: the value of the observation likelihood at the profiled estimates of coefs.

ProfileDP

The derivative of ProfileErr with respect to allpars[active].

ProfileList

Returns the results of ProfileErr and ProfileDP as a list with elements value and gradient

#### See Also

outeropt, Profile.LS, Profile.multinorm, LS.setup, multinorm.setup

Profiling Routines

Profile Estimation Functions

#### **Description**

These functions are wrappers that create lik and proc functions and run generalized profiling.

# Usage

# **Arguments**

fn

A function giving the right hand side of a differential/difference equation. The function should have arguments

- times The times at which the RHS is being evaluated.
- x The state values at those times.
- p Parameters to be entered in the system.
- more An object containing additional inputs to fn

It should return a matrix of the same dimension of x giving the right hand side values.

If fn is given as a single function, its derivatives are estimated by finite-differencing with stepsize eps. Alternatively, a list can be supplied with elements:

- fn Function to calculate the right hand side should accept a matrix of state values at .
- dfdx Function to calculate the derivative with respect to x
- dfdp Function to calculate the derivative with respect to p
- d2fdx2 Function to calculate the second derivative with respect to x
- d2fdxdp Function to calculate the second derivative with respect to x and p

These functions take the same arguments as fn and should output multidimensional arrays with the dimensions ordered according to time, state, deriv1, deriv2; here derivatives with respect to x always precede derivatives with respect to p.

data Matrix of observed data values.

times Vector observation times for the data.

pars Initial values of parameters to be estimated processes.

coefs Vector giving the current estimate of the coefficients in the spline.

basisvals Values of the collocation basis to be used. This can either be a basis object from

the fda package, or a list elements:

• bvals.obs A matrix giving the values of the basis at the observation times

• bvals A matrix giving the values of the basis at the quadrature times

• dbvals A matrix giving the derivative of the basis at the quadrature times

lambda (Profile.LS only) Penalty value trading off fidelity to data with fidelity to dif-

ferential equations.

var (profile.Cproc or profile.Dproc) A vector of length 2, giving

fd.obj (Optional) A functional data object; if this is non-null, coefs and basisvals is

extracted from here.

more An object specifying additional arguments to fn.

weights (Profile.LS only)

quadrature Quadrature points, should contain two elements (if not NULL)

• qpts Quadrature points; defaults to midpoints between knots

• qwts Quadrature weights; defaults to normalizing by the length of qpts.

in.meth Inner optimization function to be used, currently one of 'nlminb', 'MaxNR',

'optim' or 'house'. The last calls SplineEst.NewtRaph. This is fast but has

poor convergence.

out.meth Outer optimization function to be used, depending on the type of method

• Profile.LS One of 'nls' or 'ProfileGN'; the latter calls Profile. GausNewt which is fast but may have poor convergence.

• Profile.multinorm One of 'optim' (defaults to BFGS routine in optim

unless control.out\$meth specifies otherwise), 'nlminb', or 'maxNR'.

control.in Control object for inner optimization function.

control.out Control object for outer optimization function.

eps Finite differencing step size, if needed.

active Incides indicating which parameters of pars should be estimated; defaults to all

of them.

posproc Should the state vector be constrained to be positive? If this is the case, the state

is represented by an exponentiated basis expansion in the proc object.

poslik Should the state be exponentiated before being compared to the data? When

the state is represented on the log scale (posproc=TRUE), this is an alternative to

taking the log of the data.

discrete Is this a discrete-time or a continuous-time system? If discrete, the derivative is

instead taken to be the value at the next time point.

names The names of the state variables if not given by the column names of coefs.

| sparse  | Should sparse matrices be used for basis values? This option can save memory when ProfileGausNewt and SplineEstNewtRaph are called. Otherwise sparse matrices will be converted to full matrices and this can slow the code down.   |
|---------|---|
| likfn   | Defines a map from the trajectory to the observations. This should be in the same form as fn. If a function is given, derivatives are estimated by finite differencing, otherwise a list is expected to provide the same derivatives as fn. If poslik=TRUE, the states are exponentiated before the likfn is evaluated and the derivatives are updated to account for this. Defaults to the identity transform. |
| likmore | A list containing additional inputs to likfn if needed, otherwise set to NULL   |

#### **Details**

These functional all carry out the profiled optimization method of Ramsay et al 2007. Profile.LS uses a sum of squared errors criteria for both fit to data and the fit of the derivatives to a differential equation. Profile.multinorm uses multivariate normal approximations. discrete changes the system to a discrete-time difference equation with the right hand side function giving the transition function.

Note that these all call outeropt, which creates temporary files 'curcoefs.tmp' and 'optcoefs.tmp' to update coefficients as pars evolves. These overwrite existing files of those names and are deleted before the function terminates.

# Value

#### A list with elements

| pars  | Optimized parameters                                    |
|-------|---|
| coefs | Optimized coefficients at pars                          |
| lik   | The lik object generated                                |
| proc  | The proc item generated                                 |
| data  | The data used in doing the fitting.                     |
| times | The vector of times at which the observations were made |

#### See Also

```
outeropt, ProfileErr, ProfileSSE, LS. setup, multinorm. setup
```

# **Examples**

```
knots = seq(0,20,0.2)
norder = 3
nbasis = length(knots) + norder - 2
range = c(0,20)
bbasis = create.bspline.basis(range=range(FhNtimes), nbasis=nbasis,
norder=norder,breaks=knots)
#### Start from pre-estimated values to speed up optimization
data(FhNest)
spars = FhNestPars
coefs = FhNestCoefs
lambda = 10000
res1 = Profile.LS(make.fhn(),data=FhNdata,times=FhNtimes,pars=spars,coefs=coefs,
 basisvals=bbasis,lambda=lambda,in.meth='nlminb',out.meth='nls')
Covar = Profile.covariance(pars=res1$pars,times=FhNtimes,data=FhNdata,
 coefs=res1$coefs,lik=res1$lik,proc=res1$proc)
## Not run:
## Alternative, starting from perturbed coefficients -- takes too long for
# automatic checks in CRAN
# Initial values for coefficients will be obtained by smoothing
DEfd = smooth.basis(FhNtimes,FhNdata,fdPar(bbasis,1,0.5)) # Smooth to estimate
                                                         # coefficients first
coefs = DEfd$fd$coefs
colnames(coefs) = FhNvarnames
####
        Optimization ###
spars = c(0.25, 0.15, 2.5)
                                # Perturbed parameters
names(spars)=FhNparnames
lambda = 10000
res1 = Profile.LS(make.fhn(),data=FhNdata,times=FhNtimes,pars=spars,coefs=coefs,
 basisvals=bbasis,lambda=lambda,in.meth='nlminb',out.meth='nls')
par(mfrow=c(2,1))
plotfit.fd(FhNdata,FhNtimes,fd(res1$coefs,bbasis))
## End(Not run)
```

SEIRdata 33

SEIRdata

SEIR data

# **Description**

Data generated for SEIR Examples

#### Usage

SEIRdata

#### **Format**

- SEIRdata A 261 by 1 matrix of data generated from the SEIR Gillespie process run over 5 years.
- SEIRtimes A vector of 261 observation times corresponding to SEIRdata.
- SEIRpars Named parameter vector used to generate SEIRdata.
- SEIRvarnames c('V', 'R'): the state variable names for the SEIR system.
- SEIRparnames parameter names for the SEIR system.

## **Source**

Giles Hooker, Stephen P. Ellner, David Earn and Laura Roditi, 2010. "Parameterizing State-space Models for Infectious Disease Dynamics by Generalized Profiling: Measles in Ontario", Technical Report, Cornell University.

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setup

Setup Functions for proc and lik objects

## **Description**

These functions set up lik and proc objects of squared error and multinormal processes.

# Usage

#### **Arguments**

pars

Initial values of parameters to be estimated processes.

coefs

Vector giving the current estimate of the coefficients in the spline.

fn

A function giving the right hand side of a differential/difference equation. The function should have arguments

- times The times at which the RHS is being evaluated.
- x The state values at those times.
- p Parameters to be entered in the system.
- more An object containing additional inputs to fn

It should return a matrix of the same dimension of x giving the right hand side values.

If fn is given as a single function, its derivatives are estimated by finite-differencing with stepsize eps. Alternatively, a list can be supplied with elements:

- fn Function to calculate the right hand side should accept a matrix of state values at .
- dfdx Function to calculate the derivative with respect to x
- dfdp Function to calculate the derivative with respect to p
- d2fdx2 Function to calculate the second derivative with respect to x
- d2fdxdp Function to calculate the second derivative with respect to x and p

These functions take the same arguments as fn and should output multidimensional arrays with the dimensions ordered according to time, state, deriv1, deriv2; here derivatives with respect to x always precede derivatives with respect to p.

fn can also be given as a pomp object (see the pomp package), in which case it is interfaced to CollocInfer through pomp. skeleton using a finite differencing.

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basisvals

Values of the collocation basis to be used. This can either be a basis object from the fda package, or a list elements:

- bvals.obs A matrix giving the values of the basis at the observation times
- bvals A matrix giving the values of the basis at the quadrature times
- dbvals A matrix giving the derivative of the basis at the quadrature times

For discrete systems, it may also be specified as a matrix, in which case bvals\$bvals is obtained by deleting the last row and bvals\$dbvals is obtained by deleting the first/

If left as NULL, it is taken from fd.obj for discrete=FALSE and defaults to an identity matrix of the same dimension as the number of observations for discrete=TRUE systems.

lambda (LS. setup only) Penalty value trading off fidelity to data with fidelity to differ-

ential equations.

(profile.Cproc or profile.Dproc) A vector of length 2, giving

(Optional) A functional data object; if this is non-null, coefs and basisvals is fd.obj

extracted from here.

more An object specifying additional arguments to fn.

data The data to be used, this can be a matrix, or a three-dimensional array. If the

latter, the middle dimension is taken to be replicates. The data are returned, if

replicated they are returned in a concatenated form.

weights (LS. setup only)

times Vector observation times for the data. If the data are replicated, times are re-

turned in a concatenated form.

Quadrature points, should contain two elements (if not NULL) quadrature

• qpts Quadrature points; defaults to midpoints between knots

• qwts Quadrature weights; defaults to normalizing by the length of qpts.

Finite differencing step size, if needed. eps

Should the state vector be constrained to be positive? If this is the case, the state posproc

is represented by an exponentiated basis expansion in the proc object.

Should the state be exponentiated before being compared to the data? When the poslik

state is represented on the log scale TRUE, this is an alternative to taking the log

of the data.

discrete Is this a discrete or continuous-time system?

The names of the state variables if not given by the column names of coefs. names

Should sparse matrices be used for basis values? This option can save memory

when ProfileGausNewt and SplineEstNewtRaph are called. Otherwise sparse

matrices will be converted to full matrices and this can slow the code down.

likfn Defines a map from the trajectory to the observations. This should be in the

> same form as fn. If a function is given, derivatives are estimated by finite differencing, otherwise a list is expected to provide the same derivatives as fn. If poslik=TRUE, the states are exponentiated before the likfn is evaluated and the derivatives are updated to account for this. Defaults to the identity transform.

likmore A list containing additional inputs to likfn if needed, otherwise set to NULL

var

sparse

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## **Details**

These functions provide basic setup utilities for the collocation inference methods. They define lik and proc objects for sum of squared errors and multivariate normal log likelihoods with nonlinear transfer functions describing the evolution of the state vector.

- LS.setup Creates sum of squares functions
- multinorm.setup Creates multinormal log likelihoods for a continuous-time system.

#### Value

A list with elements

| coefs | Starting values for coefs  |
|-------|--|
| lik   | The lik object generated   |
| proc  | The proc item generated  |
| data  | The data matrix, concatenated if from a 3d array.                    |
| times | The vector of observation times, concatenated if data is a 3d array. |

## See Also

```
inneropt, outeropt, Profile.LS, Profile.multinorm, Smooth.LS, Smooth.multinorm
```

## **Examples**

```
# FitzHugh-Nagumo
t = seq(0,20,0.05)
                              # Observation times
pars = c(0.2, 0.2, 3)
                              # Parameter vector
names(pars) = c('a', 'b', 'c')
knots = seq(0,20,0.2)
                              # Create a basis
norder = 3
nbasis = length(knots) + norder - 2
range = c(0,20)
bbasis = create.bspline.basis(range=range,nbasis=nbasis,norder=norder,breaks=knots)
lambda = 10000
                             # Penalty value
coefs = matrix(0,nbasis,2) # Coefficient matrix
profile.obj = LS.setup(pars=pars,coefs=coefs,fn=make.fhn(),basisvals=bbasis,
                       lambda=lambda,times=t)
# Using multinorm
var = c(1,0.01)
```

Smooth.LS

Model-Based Smoothing Functions

# **Description**

Perform the inner optimization to estimate coefficients given parameters.

## Usage

## **Arguments**

fn

A function giving the right hand side of a differential/difference equation. The function should have arguments

- times The times at which the RHS is being evaluated.
- x The state values at those times.
- p Parameters to be entered in the system.
- more An object containing additional inputs to fn

It should return a matrix of the same dimension of x giving the right hand side values.

If fn is given as a single function, its derivatives are estimated by finite-differencing with stepsize eps. Alternatively, a list can be supplied with elements:

 fn Function to calculate the right hand side should accept a matrix of state values at .

- dfdx Function to calculate the derivative with respect to x
- dfdp Function to calculate the derivative with respect to p
- d2fdx2 Function to calculate the second derivative with respect to x
- d2fdxdp Function to calculate the second derivative with respect to x and p

These functions take the same arguments as fn and should output multidimensional arrays with the dimensions ordered according to time, state, deriv1, deriv2; here derivatives with respect to x always precede derivatives with respect to p.

data Matrix of observed data values.

times Vector observation times for the data.

pars Initial values of parameters to be estimated processes.

coefs Vector giving the current estimate of the coefficients in the spline.

basisvals Values of the collocation basis to be used. This can either be a basis object from

the fda package, or a list elements:

• byals.obs A matrix giving the values of the basis at the observation times

• bvals A matrix giving the values of the basis at the quadrature times

• dbvals A matrix giving the derivative of the basis at the quadrature times

lambda (Smooth.LS only) Penalty value trading off fidelity to data with fidelity to dif-

ferential equations.

var (Smooth.multinorm) A vector of length 2, giving

fd.obj (Optional) A functional data object; if this is non-null, coefs and basisvals is

extracted from here.

more An object specifying additional arguments to fn.

weights (Smooth.LS only)

quadrature Quadrature points, should contain two elements (if not NULL)

• qpts Quadrature points; defaults to midpoints between knots

• qwts Quadrature weights; defaults to normalizing by the length of qpts.

in.meth Inner optimization function to be used, currently one of 'nlminb', 'MaxNR',

'optim' or 'SplineEst'. The last calls SplineEst.NewtRaph. This is fast but has

poor convergence.

control.in Control object for inner optimization function.

eps Finite differencing step size, if needed.

posproc Should the state vector be constrained to be positive? If this is the case, the state

is represented by an exponentiated basis expansion in the proc object.

poslik Should the state be exponentiated before being compared to the data? When

the state is represented on the log scale (posproc=TRUE), this is an alternative to

taking the log of the data.

discrete Is this a discrete or continuous-time system?

names The names of the state variables if not given by the column names of coefs.

| sparse  | Should sparse matrices be used for basis values? This option can save memory when ProfileGausNewt and SplineEstNewtRaph are called. Otherwise sparse matrices will be converted to full matrices and this can slow the code down.   |
|---------|---|
| likfn   | Defines a map from the trajectory to the observations. This should be in the same form as fn. If a function is given, derivatives are estimated by finite differencing, otherwise a list is expected to provide the same derivatives as fn. If poslik=TRUE, the states are exponentiated before the likfn is evaluated and the derivatives are updated to account for this. Defaults to the identity transform. |
| likmore | A list containing additional inputs to likfn if needed, otherwise set to NULL   |

## **Details**

These routines create lik and proc objects and call inneropt.

# Value

## A list with elements

| coefs | Optimized coefficients at pars                          |
|-------|---|
| lik   | The lik object generated                                |
| proc  | The proc item generated                                 |
| res   | The result of the optimization method                   |
| data  | The data used in doing the fitting.                     |
| times | The vector of times at which the observations were made |

## See Also

```
inneropt, LS.setup, multinorm.setup, SplineCoefsErr
```

# **Examples**

```
#### Start from pre-estimated values to speed up optimization
data(FhNest)
spars = FhNestPars
coefs = FhNestCoefs
lambda = 10000
res1 = Smooth.LS(make.fhn(),data=FhNdata,times=FhNtimes,pars=spars,coefs=coefs,
  basisvals=bbasis,lambda=lambda,in.meth='nlminb')
## Not run:
# Henon system
hpars = c(1.4,0.3)
                                # Parameters
t = 1:200
x = c(-1,1)
                                # Create some dataa
X = matrix(0,200+20,2)
X[1,] = x
for(i in 2:(200+20)){ X[i,] = make.Henon() \cdot (i,X[i-1,],hpars,NULL) }
X = X[20+1:200,]
Y = X + 0.05*matrix(rnorm(200*2),200,2)
basisvals = diag(rep(1,200))  # Basis is just identiy
coefs = matrix(0,200,2)
# For sum of squared errors
lambda = 10000
res1 = Smooth.LS(make.Henon(),data=Y,times=t,pars=hpars,coefs,basisvals=basisvals,
  lambda=lambda,in.meth='nlminb',discrete=TRUE)
## End(Not run)
## Not run:
# For multinormal transitions
var = c(1,0.01)
res2 = Smooth.multinorm(make.Henon(),data=Y,t,pars=hpars,coefs,basisvals=NULL,
  var=var,in.meth='nlminb',discrete=TRUE)
```

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```
## End(Not run)
```

## **Description**

Model-based smoothing; estimation, objective criterion and derivatives.

#### Usage

# **Arguments**

| coets   | Vector giving the current estimate of the coefficients in the spline.               |  |
|---------|---|--|
| times   | Vector observation times for the data.  |  |
| data    | Matrix of observed data values.   |  |
| lik     | lik object defining the observation process.  |  |
| proc    | proc object defining the state process.   |  |
| pars    | Parameters to be used for the processes.  |  |
| sgn     | Is the minimizing (1) or maximizing (0)?  |  |
| control | A list giving control parameters for Newton-Raphson optimization. It should contain |  |

- reltol Relative tollerance criterion for the gradient and improvement before termination.
- maxit Maximum number of iterations.
- maxtry Maximum number of halving-steps to try before declaring no improvement is possible.
- trace How much iteration history to output; 0 surpresses all output, a positive value outputs parameters and improvement at each iteration.

SplineEst SplineEst

## **Details**

SplineEst.NewtRaph performs a simple Newton-Raphson estimate for the optimal value of the coefficients. This estimate lacks the convergence checks of other estimation packages, but may yeild a fast solution when needed.

#### Value

SplineEst.NewtRaph

Returns a list that is the result of the optimization with elements

- value The final objective criterion.
- coefs The optimizing value of the coefficients.
- g The gradient at the optimizing value.
- H The Hessian at the optimizing value.

SplineCoefsList

Collates the gradient calculations and returns a list with elements

- value Output of SplineCoefsErr
- gradient Output of SplineCoefsDC
- Hessian Output of SplineCoefsDC2

SplineCoefsErr The complete data log likelihood for the smooth; the inner optimization objective.

SplineCoefsDC The derivative of SplineCoefsErr with respect to coefs.

SplineCoefsDP The derivative of SplineCoefsErr with respect to pars.

SplineCoefsDC2 The second derivative of SplineCoefsErr with respect to coefs.

SplineCoefsDCDP

The second derivative of SplineCoefsErr with respect to coefs and pars.

The output of gradients is in terms of an array with dimensions corresponding to derivatives. Derivatives with with respect to coefficients are given in dimensions before those that give derivatives with respect to parameters.

#### See Also

inneropt, Smooth.LS

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